

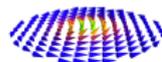
# Pushing Domain Walls with Spin Polarized Currents in Cylindrical Nanowires

M. Franchin, A. Knittel, M. Albert, D. Chernyshenko,  
T. Fischbacher, and H. Fangohr

School of Engineering Sciences, University of Southampton (UK)

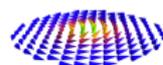
e-mail: [franchin@soton.ac.uk](mailto:franchin@soton.ac.uk)

MMM 2010 - Atlanta, 16<sup>th</sup> Nov 2010



# Outline of the talk

- motion of DWs through potential barriers,
- cylindrical nanowires with small diameter,
- rotational symmetry deeply affects the DW properties,
- depending on how the barrier pins the magnetization the critical current density changes of a factor 130.



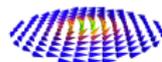
## DWs in cylindrical nanowires/nanopillars:

can be used as:

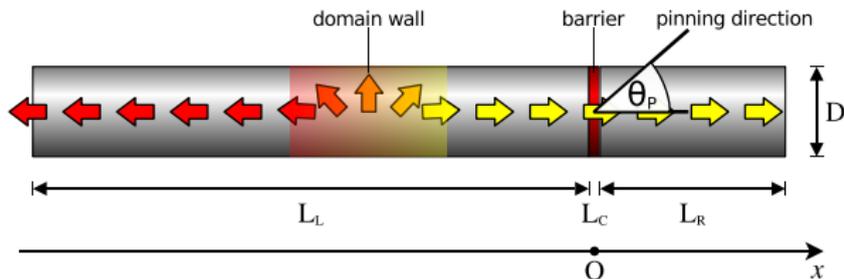
- **nano oscillators:** [PRB 78, 054447 (2008); Appl. Phys. Expr. 1, 061301 (2008)]
- **as better behaved DWs:** no walker breakdown, zero depinning current [PRL 104, 057201 (2010); PRB 82, 144430 (2010)]

**Problem:** need very small nanowires. (for Permalloy  $\varnothing \lesssim 50$  nm)  
Experimental difficulties in building such systems!

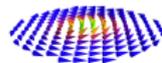
**Why?** Transition Transverse DW  $\Rightarrow$  Vortex DW



# The idea



- Long cylindrical nanowire. Small diameter,  $D \lesssim 50$  nm,
- Barrier: region with extra anisotropy which pins magnetisation
- DW sitting on the left, pushed using applied field/electric current
- Determine  $H_{\text{crit}}$ ,  $j_{\text{crit}}$  as function of the pinning angle  $\theta_P$



# The method

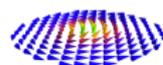
Dynamics from the Landau Lifshitz equation extended with STT effects [PRL 93, 127204 (2004)]

$$\frac{d\vec{M}}{dt} = -\gamma \vec{M} \times \vec{H} + \frac{\alpha}{M_s} \vec{M} \times \frac{d\vec{M}}{dt} + v \frac{d\vec{M}}{dx} - \frac{\xi v}{M_s} \vec{M} \times \frac{d\vec{M}}{dx}$$

Barrier modeled as localized uniaxial anisotropy which **pins the magnetization on the barrier**:

$$U_{\text{barrier}} = -K_1 (\vec{m} \cdot \vec{a})^2$$

$\vec{m} = \frac{\vec{M}}{M_s}$ ,  $\vec{a}$  is the pinning direction,  $K_1$  the pinning strength.  
Discretized using finite element method (unreleased version of Nmag, <http://nmag.soton.ac.uk>)



Determine  $H_{\text{crit}}$  and  $j_{\text{crit}}$  in **two stages**:

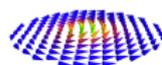
## **PREPARATION:**

the DW is relaxed and pushed weakly towards the barrier using a field/current

## **MAIN SIMULATION:**

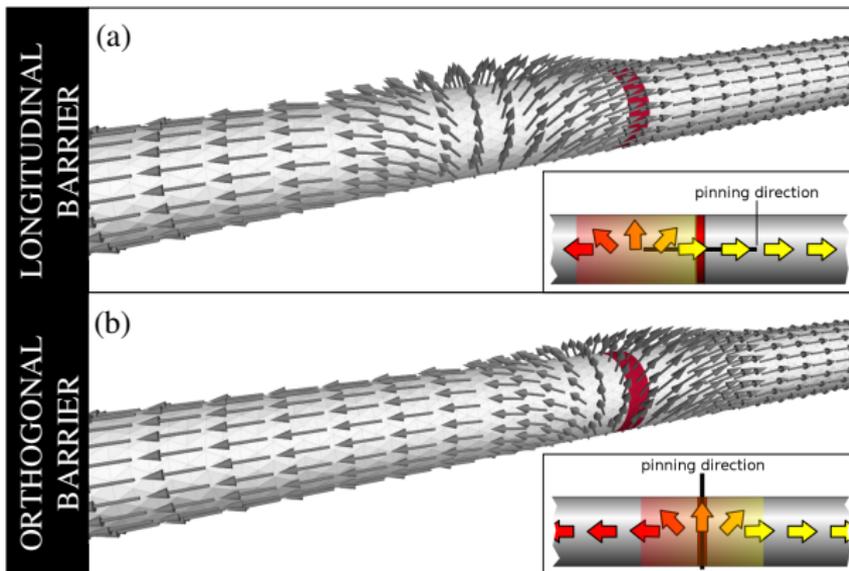
the field/current is gradually increased until the DW passes through the barrier

The dynamics of the DW is studied by looking at the average magnetization...

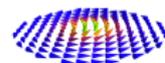


# Prepared states

When pushing a DW towards the barrier...

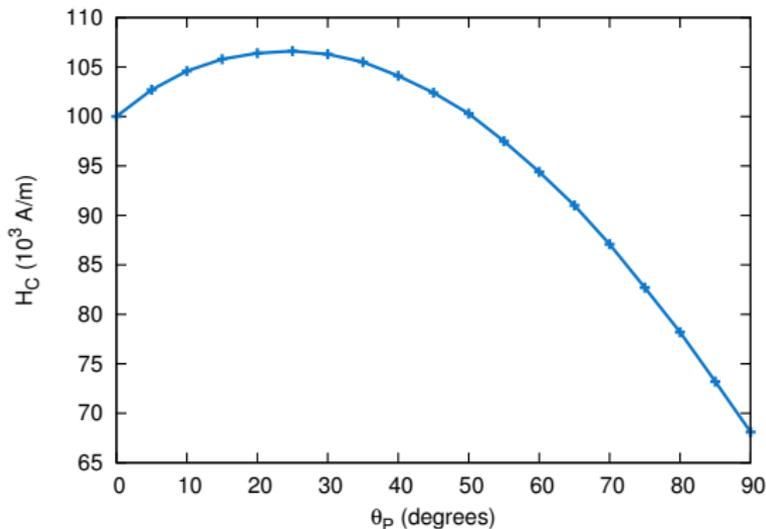


These are the initial states in the two cases.

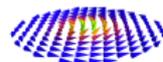


# Field-driven DW pushing

The field,  $H_{\text{crit}}$ , required to push the DW through the barrier as function of the pinning angle in the barrier.

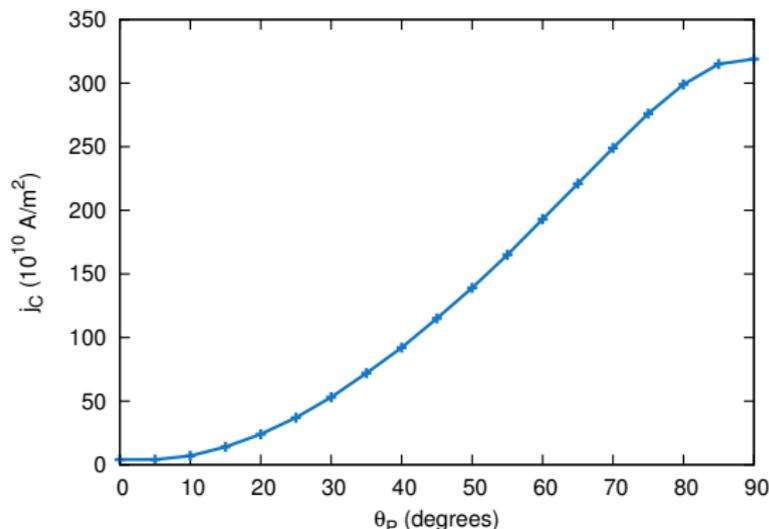


- $H_{\text{crit}}$  varies between 68.05 and 106.65 KA/m
- minimum for  $\theta_P = 90^\circ$
- maximum for  $\theta_P = 0^\circ$
- **reduced** by 36% when going from  $0^\circ$  to  $90^\circ$  (likely due to magnetostatic field)

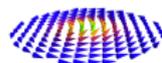


# Current-driven DW pushing

The current density,  $j_{\text{crit}}$ , required to push the DW through the barrier as function of the pinning angle in the barrier.



- $j_{\text{crit}}$  varies between 0.0239 and  $3.185 \times 10^{12}$  A/m<sup>2</sup>
- minimum for  $\theta_P = 0^\circ$
- maximum for  $\theta_P = 90^\circ$
- **increased** by a factor **130** when going from  $0^\circ$  to  $90^\circ$

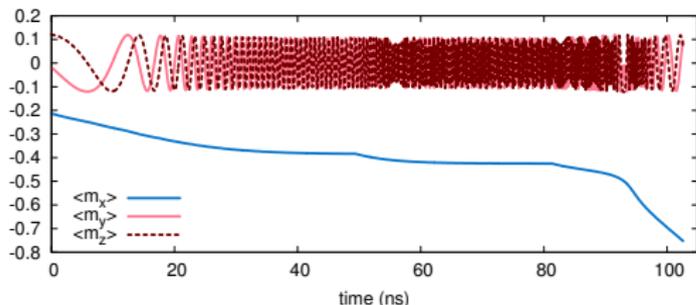


# Comparison of dynamics for $\theta_P = 0^\circ$ and $\theta_P = 20^\circ$

We analyze the dynamics of the normalized magnetization  $\langle \vec{m} \rangle$ .

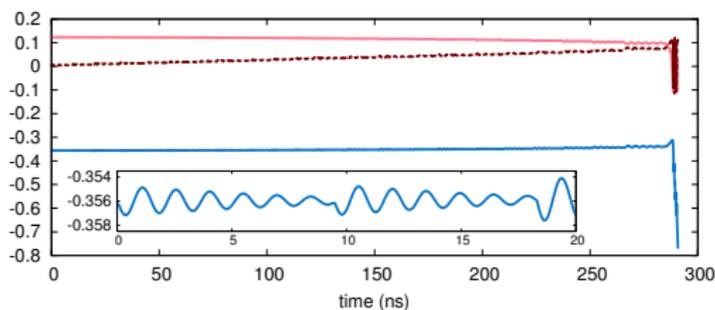
$\langle m_x \rangle \Rightarrow$  DW position (-0.5 at barrier)

$\langle m_y \rangle, \langle m_z \rangle \Rightarrow$  DW rotation



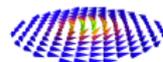
$\theta_P = 0^\circ$

- magnetization is **free to rotate**,
- **gradual and steady** compression
- accumulation of STT effect!



$\theta_P = 20^\circ$

- magnetization rotationally bound,
- $\langle m_x \rangle$  **oscillates quickly** (inset),
- but is constant on a large scale,
- sudden switching



# Instant VS accumulated

$$\frac{1}{\gamma} \frac{d\vec{m}}{dt} = - \overbrace{\vec{m} \times \vec{H}}^{\text{Precession}} - \overbrace{\alpha \vec{m} \times (\vec{m} \times \vec{H})}^{\text{Damping}}$$
$$+ \underbrace{\frac{1 + \alpha \xi}{\gamma} v \frac{d\vec{m}}{dx}}_{\text{Adiabatic STT}} - \underbrace{\frac{\xi - \alpha}{\gamma} v \vec{m} \times \frac{d\vec{m}}{dx}}_{\text{Non-adiabatic STT}}$$

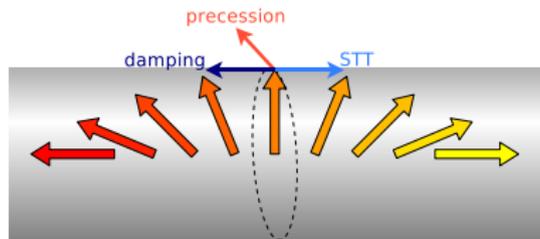
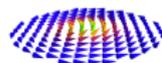


Figure: Time-evolution of the precession frequency.



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$$+ \underbrace{\frac{1 + \alpha \xi}{\gamma} v \frac{d\vec{m}}{dx}}_{\lesssim 50 \text{ KA/m}} - \underbrace{\frac{\xi - \alpha}{\gamma} v \vec{m} \times \frac{d\vec{m}}{dx}}_{\lesssim 0.5 \text{ KA/m}}$$

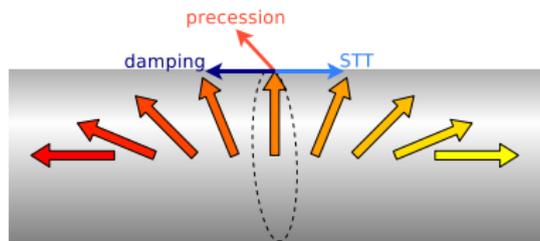
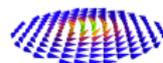


Figure: Time-evolution of the precession frequency.



# Instant VS accumulated

$$\frac{1}{\gamma} \frac{d\vec{m}}{dt} = - \underbrace{\vec{m} \times \vec{H}}_{300 \text{ KA/m}} - \underbrace{\alpha \vec{m} \times (\vec{m} \times \vec{H})}_{3 \text{ KA/m}} + \underbrace{\frac{1 + \alpha \xi}{\gamma} v \frac{d\vec{m}}{dx}}_{\lesssim 50 \text{ KA/m}} - \underbrace{\frac{\xi - \alpha}{\gamma} v \vec{m} \times \frac{d\vec{m}}{dx}}_{\lesssim 0.5 \text{ KA/m}}$$

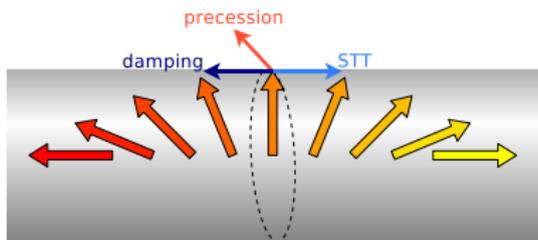
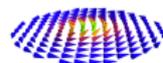


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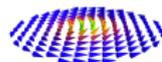


# Summary

- Current/field driven transverse DWs in cylindrical nanowires,
- Key role of rotational freedom/cylindrical symmetry,
- The symmetry reduces the critical current by a factor 130,
- While the critical field doesn't care about symmetry,
- Theoretical studies so far motivate experimental investigations.

**Acknowledgement:** The research leading to these results has received funding from the European Community's Seventh Framework Programme (FP7/2007-2013) under Grant Agreement n° 233552, and from EPSRC (EP/E040063/1)

Thank you!

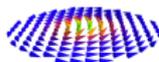


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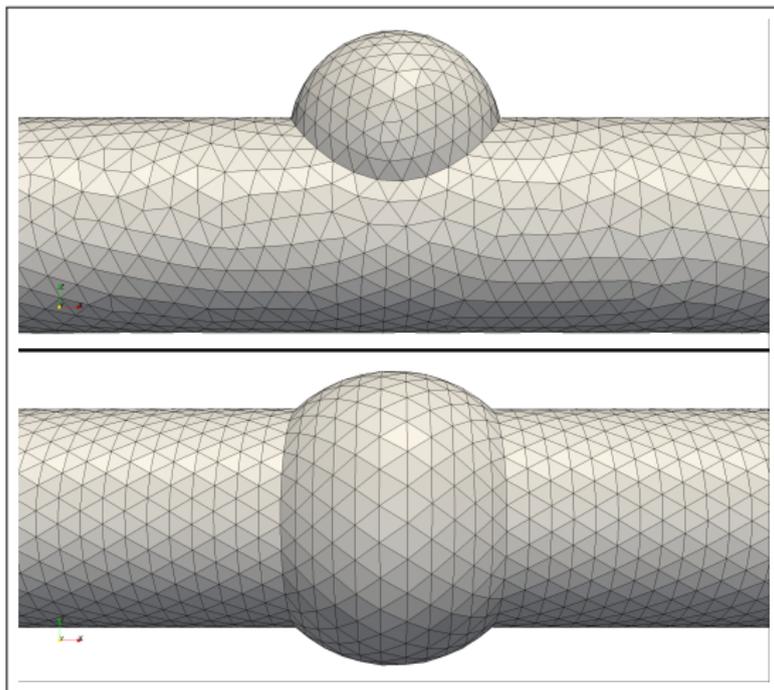
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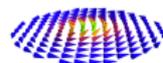
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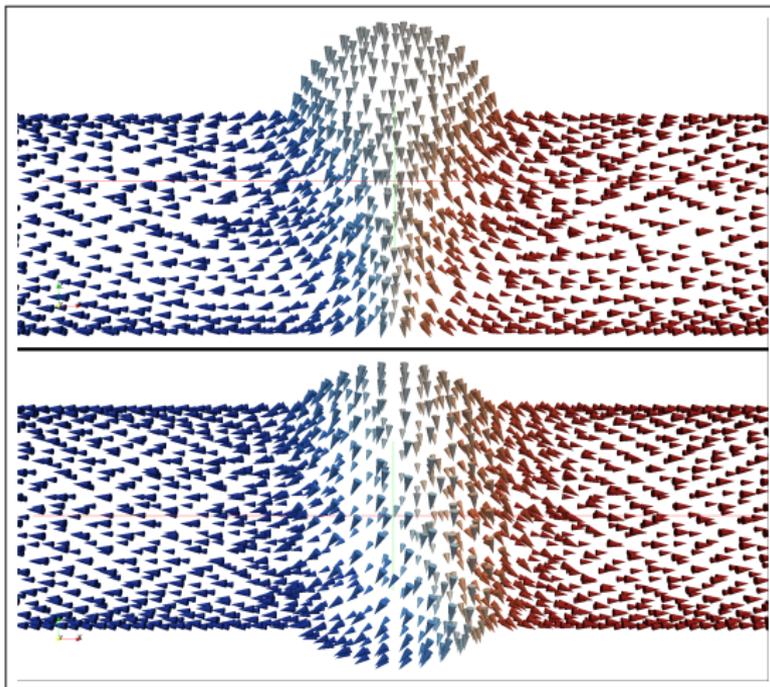
# Concrete examples



Examples of symmetric and asymmetric barriers.



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Examples of symmetric and asymmetric barriers.

