

## ELEC3026 MODEM: Brief Notes

# Coherent and Non-coherent Receivers

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## Coherent Receiver

### (a) **Carrier recovery** for demodulation

- Receiver signal  $\hat{S}(t) = A \cos(\omega_c t + \varphi) + N(t)$
- Local carrier  $\cos(\omega_c t + \bar{\varphi})$
- Carrier recovery (e.g. phase lock loop) circuit

$$\Delta\varphi = \varphi - \bar{\varphi} \rightarrow 0 \quad \text{i.e.} \quad \bar{\varphi} \rightarrow \varphi$$

- Demodulation leads to recovered baseband signal

$$Y(t) = X(t + \tau) + N(t)$$

where  $X(t)$  is transmitted baseband signal

### (b) **Timing recovery** for sampling

- Align receiver clock with transmitter clock, so that sampling  $\Rightarrow$  no ISI

$$Y_k = X_k + N_k$$

where  $X_k$  are transmitted symbols, and  $N_K$  noise samples



## Non-coherent Receiver

### (a) No carrier recovery for demodulation

- Receiver signal  $\hat{S}(t) = A \cos(\omega_c t + \varphi) + N(t)$
- Local carrier  $\cos(\omega_c t + \bar{\varphi})$
- No carrier recovery,

$$\phi = \Delta\varphi = \varphi - \bar{\varphi} \neq 0 \quad \text{i.e.} \quad \bar{\varphi} \neq \varphi$$

- Demodulation leads to recovered baseband signal

$$Y(t) = X(t + \tau)e^{j\phi} + N(t)$$

### (b) Timing recovery for sampling

- Align receiver clock with transmitter clock, sampling results in

$$Y_k = X_k e^{j\phi} + N_k$$

Could not recover transmitted symbols properly from  $Y_k$  !



# Differential Detection

## (a) Differential encoding for transmission

- Symbols  $\{C_k\} \Rightarrow \{X_k\}$  for transmission

$$X_k = C_k \cdot X_{k-1}$$

- As  $X_k \cdot X_{k-1}^* = C_k \cdot (X_{k-1} \cdot X_{k-1}^*)$ ,

$$C_k = \frac{X_k \cdot X_{k-1}^*}{|X_{k-1}|^2} \quad (1)$$

## (b) Non-coherent detection

- Receiver samples

$$Y_k = X_k \cdot |H| \cdot e^{j\phi} + N_k$$

$|H|$ : magnitude of combined channel tap,  $\phi \neq 0$ : unknown phase

- Differential decoding

$$\hat{C}_k = \frac{Y_k \cdot Y_{k-1}^*}{|Y_{k-1}|^2} \quad (2)$$



## Differential Detection (derivation)

$$\begin{aligned}
 Y_k \cdot Y_{k-1}^* &= (X_k \cdot |H| \cdot e^{j\phi} + N_k) \cdot (X_{k-1}^* \cdot |H| \cdot e^{-j\phi} + N_{k-1}^*) \\
 &= X_k \cdot X_{k-1}^* \cdot |H|^2 \cdot e^{j(\phi-\phi)} \\
 &\quad + N_k \cdot N_{k-1}^* + X_k \cdot |H| \cdot e^{j\phi} \cdot N_{k-1}^* + N_k \cdot X_{k-1}^* \cdot |H| \cdot e^{-j\phi}
 \end{aligned}$$

$$\begin{aligned}
 |Y_{k-1}|^2 &= X_{k-1} \cdot X_{k-1}^* \cdot |H|^2 + N_{k-1} \cdot N_{k-1}^* \\
 &\quad + X_{k-1} \cdot |H| \cdot e^{j\phi} \cdot N_{k-1}^* + N_{k-1} \cdot X_{k-1}^* \cdot |H| \cdot e^{-j\phi}
 \end{aligned}$$

When noise  $N_k$  is very small

$$Y_k \cdot Y_{k-1}^* \approx X_k \cdot X_{k-1}^* \cdot |H|^2 \quad \text{and} \quad |Y_{k-1}|^2 \approx |X_{k-1}|^2 \cdot |H|^2$$

- Thus,

$$\hat{C}_k = \frac{Y_k \cdot Y_{k-1}^*}{|Y_{k-1}|^2} \approx C_k + \bar{N}_k$$

where power of enhanced noise  $\bar{N}_k$  is **larger** than that of  $N_k$

- Note that influence of channel phase  $\phi$  has been removed



# Comparison

- Coherent detection
  - Require expensive and complex carrier recovery circuit
  - Better bit error rate of detection

$$\hat{X}_k = X_k + N_k$$

- Non-coherent detection
  - Do not require expensive and complex carrier recovery circuit
  - Poorer bit error rate of detection

$$\hat{C}_k = C_k + \bar{N}_k$$

- Differential systems have important advantages and are widely used in practice

