

ELEC3028 (EL334) Digital Transmission

Half of the unit:

- **Information Theory**
- **MODEM** (modulator and demodulator)

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Lecture notes from: Course Office ([ECS Student Services](#))
or Download from:

<http://www.ecs.soton.ac.uk/~sqc/EL334N/>

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Other half: **CODEC** (source coding, channel coding) by Prof. Lajos Hanzo



What's **New** (Should be **Old**) in Communications

- Imagine a few scenarios:
 - In holiday, use your fancy mobile phone to take picture and send it to a friend
 - In airport waiting for boarding, switch on your laptop and go to your favourite web side
 - Or watch World Cup with your mobile phone
- Do you know these words:
CDMA, multicarrier, OFDM, space-time processing, MIMO, turbo coding, LTE

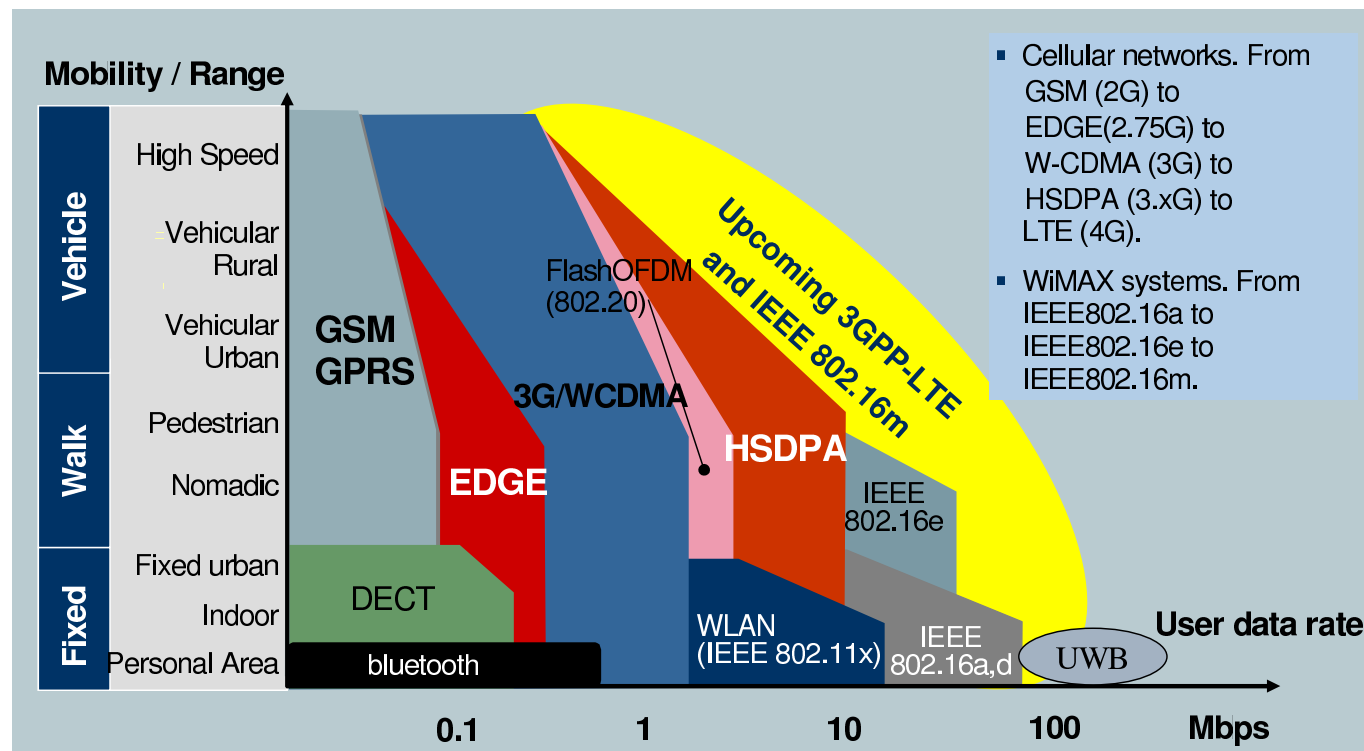
Broadband, WiFi, WiMAX, intelligent network, smart antenna, IP telephone
- In this introductory course, we should go through some A B C ... of **Digital Communication**



Wireless and Mobile Networks

- Past/current/future: 2G, 3G, B3G or 4G

Current Wireless Technology Positioning



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Some improved 2G, HSCSD: high-speed circuit switched data, GPRS: general packet radio service, EDGE: enhanced data rates for GSM evolution. Also, HIPERLAN: high performance radio local area network

General Comments on Communications

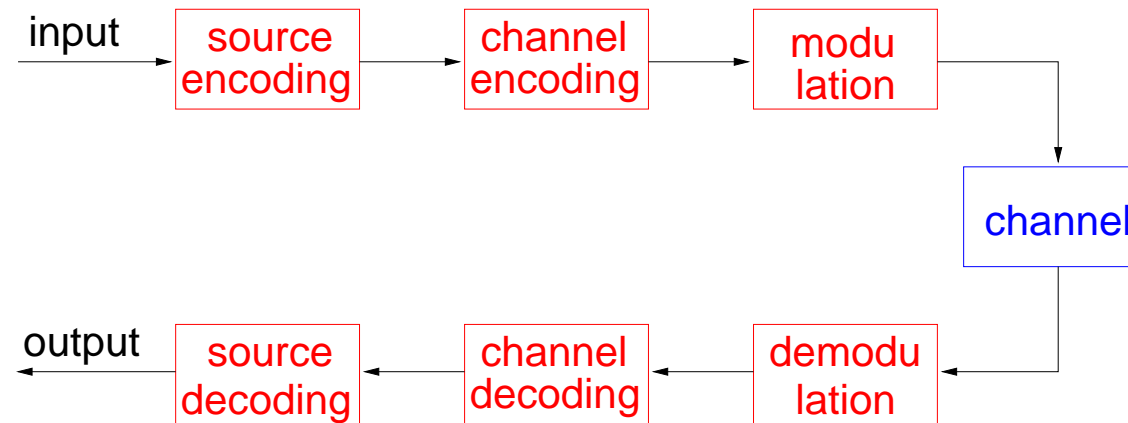
- Aim of telecommunications: to communicate information between geographically separated locations via a communications channel of adequate **quality** (at certain **rate** **reliably**)



- The transmission will be based on digital data, which is obtained from (generally) analogue quantities by
 1. sampling (Nyquist: sampling with at least twice the maximum frequency), and
 2. quantisation (introduction of quantisation noise through rounding off)
- Transmitting at certain rate requires certain spectral **bandwidth**
- Here channel means whole system, which has certain **capacity**, the maximum rate that can be used to transmit information through the system **reliably**

General Transmission Scheme

- A **digital transmission** scheme generally involves:



- Input/output are considered digital (analogue sampled/quantised)
- **CODEC**, **MODEM**, **channel** (transmission medium)
- Your 3G mobile phone, for example, contains a pair of **transmitter** and **receiver** (together called **transceiver**), consisting of a CODEC and MODEM

What is Information

- Generic question: what is **information**? How to measure it (**unit**)?
- Generic digital source is characterised by:
 - Source alphabet (message or symbol set): m_1, m_2, \dots, m_q
 - Probability of occurrence (symbol probabilities): p_1, p_2, \dots, p_q
e.g. binary equiprobable source $m_1 = \mathbf{0}$ and $m_2 = \mathbf{1}$ with $p_1 = 0.5$ and $p_2 = 0.5$
 - Symbol rate (symbols/s or Hz)
 - Probabilistic interdependence of symbols (correlation of symbols, e.g. does m_i tell us nothing about m_j or something?)
- At a specific symbol interval, symbol m_i is transmitted correctly to receiver
 - What is *amount of information* conveyed from transmitter to receiver?
 - The answer:

$$I(m_i) = \log_2 \frac{1}{p_i} = -\log_2 p_i \quad (\text{bits})$$

Concept of Information

- Forecast: tomorrow, rain in three different places:
 1. Raining season in a tropical forest
 2. Somewhere in England
 3. A desert where rarely rains
- **Information content** of an event is connected with **uncertainty** or inverse of probability. The more unexpected (smaller probability) the event is, the more information it contains
- **Information theory** (largely due to Shannon)
 - Measure of information
 - Information capacity of channel
 - coding as a means of utilising channel capacity

Shannon Limit

- We know different communication system designs achieve different performance levels and we also know system performance is always limited by the available *signal power*, the inevitable *noise* and the need to limit *bandwidth*
- What is the ultimate performance **limit** of communication systems, underlying only by the fundamental physical nature?
- Shannon's information theory addresses this question

Shannon's theorem: If the rate of information from a source does not exceed the capacity of a communication channel, then there exists a coding technique such that the information can be transmitted over the channel with arbitrarily small probability of error, despite the presence of noise

- In 1992, two French Electronics professors developed practical *turbo coding*, which approaches Shannon limit (transmit information at capacity rate)



Information Content

- Source with **independent** symbols: m_1, m_2, \dots, m_q , and probability of occurrence: p_1, p_2, \dots, p_q
- Definition of information: amount of information in i th symbol m_i is defined by

$$I(m_i) = \log_2 \frac{1}{p_i} = -\log_2 p_i \quad (\text{bits})$$

Note the unit of information: bits !

- Properties of information
 - Since probability $0 \leq p_i \leq 1$, $I(m_i) \geq 0$: information is nonnegative
 - If $p_i > p_j$, $I(m_i) < I(m_j)$: the lower the probability of a source symbol, the higher the information conveyed by it
 - $I(m_i) \rightarrow 0$ as $p_i \rightarrow 1$: symbol with probability one carries no information
 - $I(m_i) \rightarrow \infty$ as $p_i \rightarrow 0$: symbol with probability zero carries infinite amount of information (but it never occurs)

Physical Interpretation

- Information content of a symbol or message is equal to minimum number of binary digits required to encode it and, hence, has a unit of bits
 - Binary equiprobable symbols: $m_1, m_2 \leftrightarrow \mathbf{0}, \mathbf{1}$, minimum of one binary digit (one bit) is required to represent each symbol
Equal to information content of each symbol: $I(m_1) = I(m_2) = \log_2 2 = 1$ bit
 - Four equiprobable symbols: $m_1, m_2, m_3, m_4 \leftrightarrow \mathbf{00}, \mathbf{01}, \mathbf{10}, \mathbf{11}$ minimum of two bits is required to represent each symbol
Equal to information content of each symbol: $I(m_1) = I(m_2) = I(m_3) = I(m_4) = \log_2 4 = 2$ bits
 - In general, q equiprobable symbols $m_i, 1 \leq i \leq q$, minimum number of bits to represent each symbol is $\log_2 q$
Equal to information content of each symbol: $I(m_i) = \log_2 q$ bits
- Use $\log_2 q$ bits for each symbol is called **Binary Coded Decimal**
 - **Equiprobable** case: $m_i, 1 \leq i \leq q$, are equiprobable \Rightarrow BCD is good
 - **Non-equiprobable** case ?

Information of Memoryless Source

Source emitting a symbol sequence of length N . A memoryless Source implies that each message emitted is independent of the previous messages

Assume that N is large, so symbol m_i appears $p_i \cdot N$ times in the sequence

- Information contribution from i th symbol m_i

$$I_i = (p_i \cdot N) \cdot \log_2 \frac{1}{p_i}$$

- Total information of symbol sequence of length N

$$I_{total} = \sum_{i=1}^q I_i = \sum_{i=1}^q p_i \cdot N \cdot \log_2 \frac{1}{p_i}$$

- Average information per symbol (entropy) is

$$\frac{I_{total}}{N} = \sum_{i=1}^q p_i \cdot \log_2 \frac{1}{p_i} \quad (\text{bits/symbol})$$

Entropy

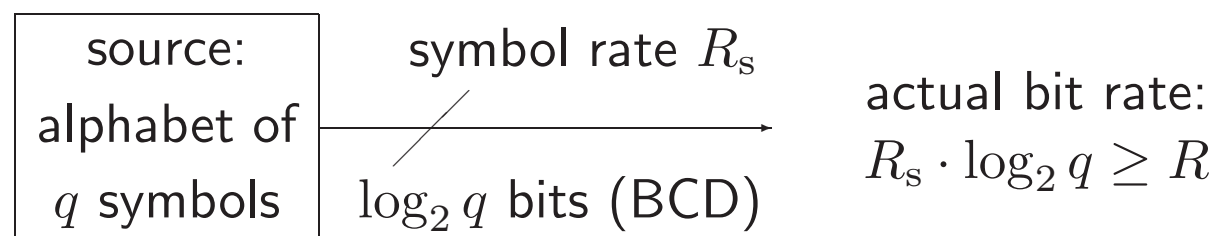
- Memoryless source **entropy** is defined as the **average information per symbol**:

$$H = \sum_{i=1}^q p_i \cdot \log_2 \frac{1}{p_i} = - \sum_{i=1}^q p_i \cdot \log_2 p_i \quad (\text{bits/symbol})$$

- Source emitting at rate of R_s symbols/sec has **information rate**:

$$R = R_s \cdot H \quad (\text{bits/sec})$$

- If each symbol is encoded by $\log_2 q$ bits, i.e. binary coded decimal, average output bit rate is $R_s \cdot \log_2 q$. Note information rate R is always smaller or equal to the average output bit rate of the source¹ !



¹Hint: $H \leq \log_2 q$

Summary

- Overview of a digital communication system: system building blocks
- Appreciation of information theory
- Information content of a symbol, properties of information
- Memoryless source with independent symbols: entropy and source information rate

