ELEC6214 AWCNSs: Advanced Topics Seminar

Accurate Acquisition of MIMO Channel State Information: How Big the Problem

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MIMO Wonderland

- Coherent MIMO: promises **wonderland** of **diversity** and/or **multiplexing** gains
 - Reaching MIMO promised land requires accurate MIMO CSI estimate
- **Challenge**: acquisition of accurate MIMO channel state information
 - Without sacrificing system throughput too much
 - Avoiding significant increase in computational complexity
- **Training** based or pure **blind** methods cannot meet these needs
- No-coherent or differential MIMO does not require CSI but suffers from 3 dB penalty in SNR and less design freedom
- Existing state-of-the-art: **semi-blind** iterative channel estimation and turbo detection-decoding
 - Using a very small training overhead to obtain initial MIMO CSI estimate
 - Using soft decisions from turbo detector-decoder to update MIMO CSI



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Challenge/Motivation

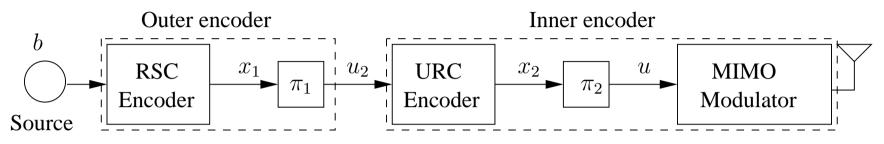
- The best **existing** state-of-the-arts still suffer from some serious drawbacks:
 - 1. Introduce extra iterative loop between CE and turbo detector-decoder \Rightarrow increase complexity considerably
 - 2. Use entire frame of L_F detected soft bits for CE \Rightarrow SDD least squares channel estimate imposes complexity $\mathcal{O}(L_F^3)$ unacceptably high
 - 3. Error propagation **severely degrade** achievable performance ⇒ fail to approach optimal ML turbo detection-decoding bound associated with perfect CSI
- It seems reaching **MIMO wonderland** necessary to implant substantial training overhead, which dramatically erodes system's throughput
- Or is it? Our objective is to demonstrate MIMO wonderland can be reached
 - with aid of very modest (minimum) training overhead
 - without significantly increasing complexity associated with the optimal ML turbo detector-decoder of perfect CSI

Reaching MIMO Wonderland

- Block-of-bits selection based soft-decision aided CE scheme:
 - select just-sufficient-number of high-quality blocks of bits or detected symbols for channel estimation
- Our BBSB-SCE and three-stage turbo detector-decoder:
 - 1. CE naturally embedded in original turbo detection-decoding process \Rightarrow **no extra iterative loop** between CE and turbo detector-decoder
 - 2. Only utilize more reliable detected symbols \Rightarrow **not entire frame** of detected soft bits for CE, dramatically reducing complexity
 - 3. Attain optimal ML turbo detector-decoder bound associated with perfect CSI, while imposing similar complexity
- P. Zhang, S. Chen and L. Hanzo, "Near-capacity joint channel estimation and three-stage turbo detection for MIMO systems," *WCNC 2013* (Shanghai, China), April 7-10, 2013 (best paper award)
- –, "Embedded iterative semi-blind channel estimation for three-stage-concatenated MIMO-aided QAM turbo-transceivers," *IEEE Trans. Vehicular Technology*, 63(1), 439–446, 2014

Three-Stage Turbo Encoder

• Three-stage turbo encoder employed at transmitter:



- Two-stage inner encoder is formed by L-QAM MIMO modulator with unityrate-code (URC) encoder
- **Outer** encoder employs half-rate recursive systematic code
- Low-complexity memory-1 URC has infinite impulse response
 - Spread **extrinsic** information beneficially across the iterative decoder components without increasing its delay
 - Extrinsic information transfer curve is capable of reaching (1.0, 1.0) point of perfect convergence in EXIT charts
 - A necessary condition for near-capacity operation and for achieving vanishingly small bit error rate



MIMO System Model

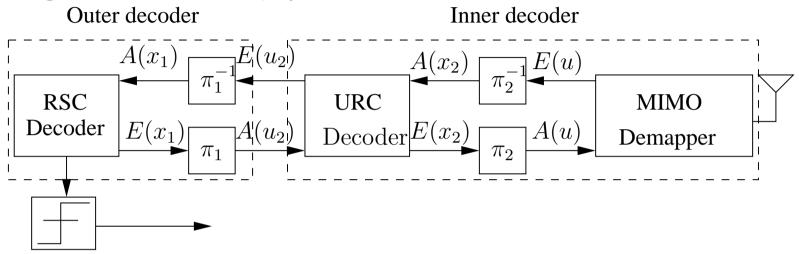
• MIMO system employs N_T transmit antennas and N_R receive antennas for communication over flat Rayleigh fading environment

 $\boldsymbol{y}(i) = \boldsymbol{H}\boldsymbol{s}(i) + \boldsymbol{v}(i)$

- $\mathbf{y}(i) \in \mathbb{C}^{N_R}$: received signal vector
- $H \in \mathbb{C}^{N_R imes N_T}$ MIMO channel matrix whose elements obey $\mathcal{CN}(0,1)$
- $\mathbf{s}(i) \in \mathbb{C}^{N_T}$: transmitted *L*-QAM symbol vector
- $\boldsymbol{v}(i) \in \mathbb{C}^{N_R}$: AWGN vector whose elements obey $\mathcal{CN}(0, N_{\mathrm{o}})$
- $\{u_k\}_{k=1}^{\text{BPB}}$: bits that are mapped to s(i)
- Frame of received MIMO data sequence $\boldsymbol{Y}_{\mathrm{d}M_F} = [\boldsymbol{y}(1) \ \boldsymbol{y}(2) \cdots \boldsymbol{y}(M_F)]$
- Number of bits per symbol: BPS = $\log_2(L)$; number of bits per block: BPB = $N_T \cdot \log_2(L)$
- A frame contains M_F symbol vectors, or $L_F = \mathsf{BPB} \cdot M_F$ bits
- System SNR = $E_{\rm s}/N_{\rm o}$, with $E_{\rm s}$ being average symbol energy

Three-Stage Turbo Decoder

• Three-stage turbo decoder employed at receiver:



• Upon obtaining a priori LLRs $\{L_a(u)\}_{k=1}^{BPB}$ from channel decoder, ML MIMO soft-demapper produces a posterior LLRs:

$$L_{p}(u_{k}) = L_{p}(k) = \ln \frac{\sum_{\substack{s^{n} \in \{s_{u_{k}}=1\}}} \exp(p_{n})}{\sum_{\substack{s^{n} \in \{s_{u_{k}}=0\}}} \exp(p_{n})}$$

$$p_n = -rac{\|oldsymbol{y}(i) - oldsymbol{H}oldsymbol{s}^n\|^2}{N_{ ext{o}}} + \sum_{k=1}^{ ext{BPB}} ilde{u}_k L_a(u_k)$$

 $\{\tilde{u}_k\}_{k=1}^{ ext{BPB}}$ are the corresponding bits that map to the specific symbol vector $m{s}^n$

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Three-Stage ML Turbo Detector-Decoder

• Given the CSI *H*, computational complexity of the three-stage **optimal maximum likelihood** turbo receiver

$$C_{\text{ideal}} = I_{\text{out}} \Big(C_{\text{RSC}} + I_{\text{in}} \big(C_{\text{ML}} + C_{\text{URC}} \big) \Big)$$

- C_{RSC} , C_{URC} and C_{ML} : complexity of **RSC decoder**, **URC decoder**, and **ML soft-demapper**, respectively
- Two-stage inner turbo loop: I_{in} iterations; outer turbo loop: $\mathit{I}_{\mathrm{out}}$ iterations
- For larges MIMOs, use reduced-complexity near-optimum detectors, e.g. K-best sphere detector, to avoid exponentially increasing complexity of ML
- For unknown CSI, training based LS estimator may be employed to obtain $m{H}$

$$\widehat{\boldsymbol{H}}_{LSCE} = \boldsymbol{Y}_{tM_T} \boldsymbol{S}_{tM_T}^{\mathrm{H}} \big(\boldsymbol{S}_{tM_T} \boldsymbol{S}_{tM_T}^{\mathrm{H}} \big)^{-1}$$

- given $M_T \ge N_T$ training data $\boldsymbol{Y}_{tM_T} = \begin{bmatrix} \boldsymbol{y}(1) \ \boldsymbol{y}(2) \cdots \boldsymbol{y}(M_T) \end{bmatrix}$ and $\boldsymbol{S}_{tM_T} = \begin{bmatrix} \boldsymbol{s}(1) \ \boldsymbol{s}(2) \cdots \boldsymbol{s}(M_T) \end{bmatrix} \Rightarrow$ Unless M_T is sufficiently large, accuracy is poor

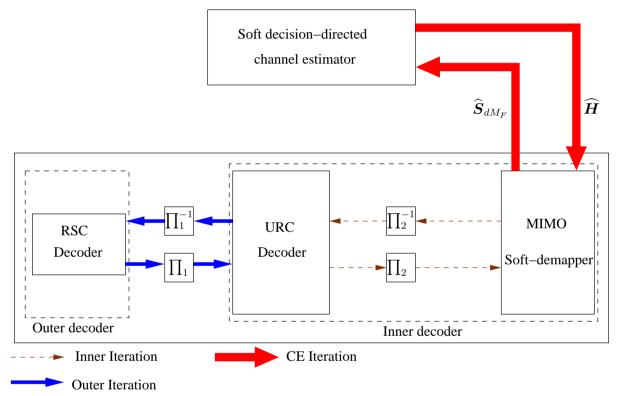


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Existing State-of-the-Arts

• To maintain system's throughput, use small $(M_T \text{ close to } N_T)$ training data to obtain initial \widehat{H}_{LSCE} , then use soft-decision based LS estimator



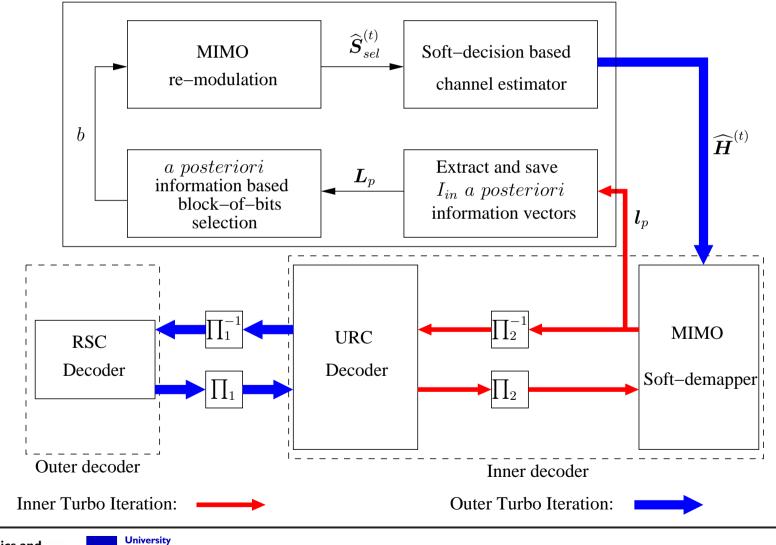
- To fully exploit error correction capability, soft-decision channel estimation takes place **after convergence** of three-stage turbo detection-decoding
 - This introduces the additional CE loop

Complexity/Performance of Existing State-of-the-Arts

- Able to rely on very small training overhead M_T
 - Three-stage turbo detector-decoder improve reliability of detected bits
 - Which assists soft-decision channel estimator to provide more accurate CE
 - Iterations result in increasingly more reliable turbo detector-decoder output
- Although very powerful with excellent performance, having following drawbacks
 - 1. Have to use entire frame of M_F soft-decision detected symbol vectors for DD LSCE, with complexity $\mathcal{O}(M_F^3)$
 - 2. Need extra CE iterative loop, which requires I_{ce} iterations to converge
 - 3. Cannot attain idealised optimal ML three-stage turbo detector-decoder bound associated with perfect CSI (still unable to reach MIMO promised land)
- Total complexity: $C_{\text{con}} = I_{\text{ce}} \cdot \mathcal{O}(M_F^3) + I_{\text{ce}} \cdot C_{\text{ideal}}$
 - Repeat three-stage turbo detection-decoding $\mathit{I}_{\rm ce}$ times
 - As M_F typically in thousands, $\mathcal{O}(M_F^3)$ is extremely high
 - Complexity is significantly higher than C_{ideal}

How to Reach MIMO Wonderland

 Proposed scheme: soft-decision based channel estimator naturally embedded in original iterative process of three-stage turbo detector-decoder ⇒ no extra CE loop

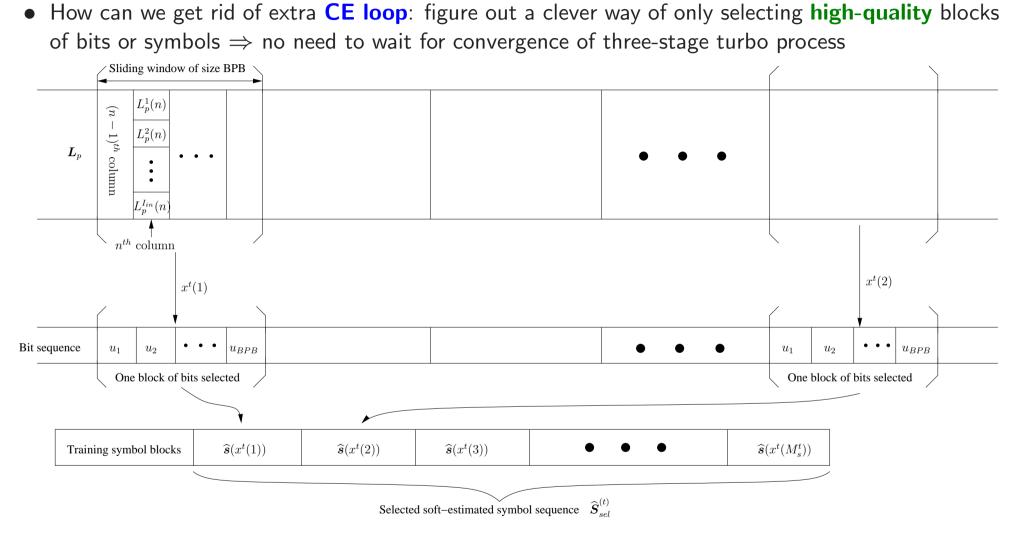


BBSB channel estimator





Select Reliable Blocks of Bits (1)



• Inner decoder iterations yield I_{in} a posterior soft decisions $\{L_p^1(n), L_p^2(n), \cdots, L_p^{I_{in}}(n)\}$ for nth bit \Rightarrow information regarding whether nth detected bit is reliable or not



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Select Reliable Blocks of Bits (2)

1. *n*th bit is **reliable**: if *n*th column of *a posterior* information matrix $L_p \in \mathbb{C}^{I_{in} \times L_F}$ satisfies

$$\frac{|L_p^1(n) - L_p^2(n)| + |L_p^2(n) - L_p^3(n)| + \dots + |L_p^{I_{\text{in}}-1}(n) - L_p^{I_{\text{in}}}(n)|}{|\mu|} \in (0, T_h)$$

where μ is the mean of the column, and T_h a pre-defined block-of-bits selection threshold

- Soft decisions for nth bit relatively similar ⇒ a stable state may be reached by turbo decoder and stable decisions of the inner decoder are likely to be the correct ones
- Experience suggests most of chosen bit blocks or symbols are selected according to *Criterion 1*
- 2. *n*th bit is **reliable**: if soft decisions have same sign and their absolute values in monotonically **ascending**

$$|L_p^1(n)| < |L_p^2(n)| < \dots < |L_p^{I_{\text{in}}}(n)|, \, \operatorname{sign}\{L_p^1(n)\} = \operatorname{sign}\{L_p^2(n)\} = \dots = \operatorname{sign}\{L_p^{I_{\text{in}}}(n)\}$$

- Correct decisions may experience iteration gain leading to **increasing** absolute values of softdecisions as number of inner iterations increases
- This type of reliable decisions could be missed by *Criterion 1* and hence we have *Criterion 2*
- Fully exploit information provided by entire inner turbo iterative process \Rightarrow capable of making **high-confidence** decision regarding whether *n*th detected bit is reliable or not



Select Reliable Blocks of Bits (3)

- Sliding-window with **window-size** of BPB bits: only when BPB **consecutive** detected bits of a block are all regarded as correct, corresponding symbol vector is selected for CE
- This process yields an integer-index vector $\boldsymbol{x}^t = \begin{bmatrix} x^t(1) \ x^t(2) \cdots x^t(M_s^t) \end{bmatrix}^T$ at the *t*-th outer turbo iteration, in which
 - $x^{t}(i)$ is **position** or index of *i*th selected symbol vector in transmitted symbol vector sequence
 - corresponding observation vectors $\boldsymbol{Y}_{sel}^{(t)} = \left[\boldsymbol{y}(x^t(1)) \; \boldsymbol{y}(x^t(2)) \cdots \boldsymbol{y}(x^t(M_s^t)) \right]$
- Number of the selected symbol vectors M_s^t varies within $\{1, 2, \cdots, M_{sel}\}$, where $M_{sel} \ll M_F$ is the maximum number of blocks imposed for CE
 - whenever the number of selected reliable symbol vectors M_s^t reaches the limit $M_{
 m sel}$, the sliding-window process ends
 - otherwise, the sliding-window process examines all the possible bit blocks and outputs the M^t_{s} selected symbol vectors
- Given \boldsymbol{x}^t , we have soft-estimated symbol vectors $\widehat{\boldsymbol{S}}_{sel}^{(t)} = \left[\widehat{\boldsymbol{s}}(x^t(1))\ \widehat{\boldsymbol{s}}(x^t(2))\cdots \widehat{\boldsymbol{s}}(x^t(M_s^t))\right]$ in which *m*th element of $\widehat{\boldsymbol{s}}(x^t(n))$:

$$\widehat{s}^{m}(x^{t}(n)) = \sum_{l=1}^{L} s^{l} \Pr\{s^{m}(x^{t}(n)) = s^{l}\} = \sum_{l=1}^{L} s^{l} \cdot \frac{\exp\left(\sum_{j=1}^{\mathsf{BPS}} \widetilde{u}_{j} L_{a}(u_{j})\right)}{\prod_{j=1}^{\mathsf{BPS}} \left(1 + \exp\left(L_{a}(u_{j})\right)\right)}$$

where $\{\widetilde{u}_j\}_{j=1}^{\mathsf{BPS}}$ represents the bit mapping for L-QAM symbol set $\{s^l\}_{l=1}^L$

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Complexity/Performance of Proposed Scheme

• Soft decision-directed LSCE with complexity $< O(M_{sel}^3)$

$$\widehat{\boldsymbol{H}}^{(t+1)} = \boldsymbol{Y}_{\text{sel}}^{(t)} \big(\widehat{\boldsymbol{S}}_{\text{sel}}^{(t)} \big)^{\mathsf{H}} \Big(\widehat{\boldsymbol{S}}_{\text{sel}}^{(t)} \big(\widehat{\boldsymbol{S}}_{\text{sel}}^{(t)} \big)^{\mathsf{H}} \Big)^{-1}$$

- $M_F = 1000$, $M_{sel} = 100$: complexity more than 10^3 times smaller than $\mathcal{O}(M_F^3)$

• Because our LSCE is naturally **embedded** in original turbo process, total complexity

$$C_{\rm pro} \le I_{\rm out} \cdot \mathcal{O}(M_{\rm sel}^3) + C_{\rm ideal}$$

- Since $I_{\text{out}} \cdot \mathcal{O}(M_{\text{sel}}^3) \ll C_{\text{ideal}}$, we have $C_{\text{pro}} \approx C_{\text{ideal}}$

- Because only use reliable decisions in CE, error propagation is dramatically alleviated, coupled with turbo effect
 - With minimum training overhead, capable of **attaining** idealised optimal threestage turbo detection-decoding bound associated with perfect CSI
 - Impose **similar** complexity to idealised three-stage turbo detector-decoder

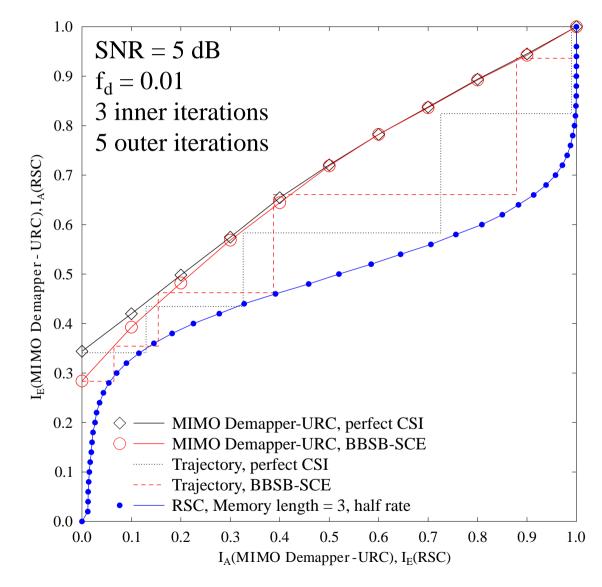


Simulation System (1)

- 1. Quasi-static Rayleigh fading MIMO: $N_T = N_R = 4$ and L = 16-QAM
 - Channel taps are static within frame and faded between frames at normalised Doppler frequency $f_d=0.01$
 - All the results were averaged over 100 channel realisations
- 2. Interleaver length of $L_F = 16,000$ bits, or $M_F = 1000$ symbol vectors
 - RSC generator polynomials: $G_{RSC} = [1, 0, 1]_2$, $G_{RSC}^r = [1, 1, 1]_2$
 - URC generator polynomials: $G_{URC} = [1, 0]_2$, $G_{URC}^r = [1, 1]_2$
- 3. Transmitted signal power normalised to unity, SNR defined as $\frac{1}{N_0}$
 - Number of initial training data blocks: $M_T = 6$ (close to minimum of 4), training overhead 0.6%
 - Blocks-of-bits selection limit set to $M_{\rm sel}=100$

EXIT Chart Analysis

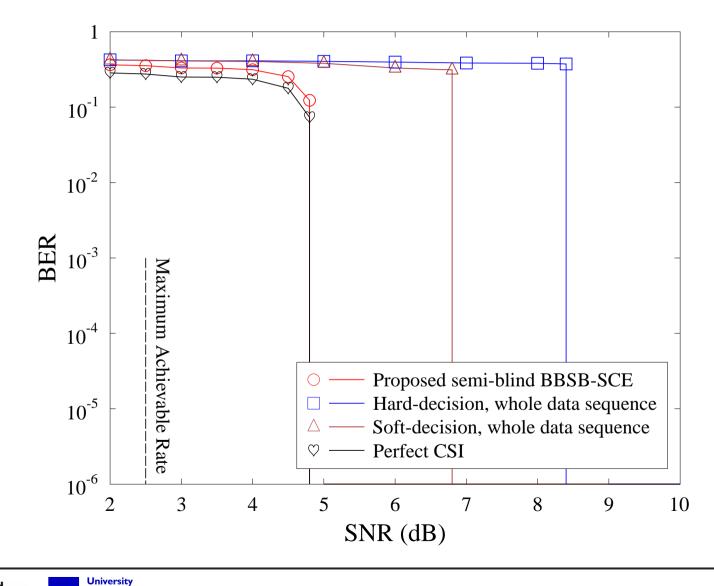
• EXIT chart analysis of our proposed semi-blind joint BBSB-SCE and three-stage turbo receiver with the block-of-bits selection threshold of $T_h = 1.0$, in comparison to the perfect-CSI scenario





BER Performance Comparison

BER comparison: the proposed joint BBSB-SCE and three-stage turbo receiver with a block-of-bits selection threshold of $T_h = 1.0$, the ۲ perfect CSI scenario as well as the conventional joint CE and three-stage turbo receivers employing the entire detected data sequence for the soft-decision and hard-decision aided channel estimators, respectively

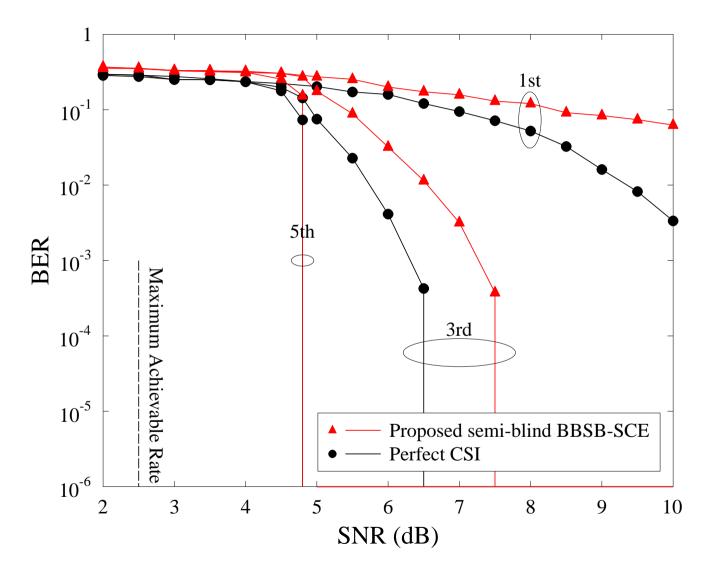




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BER Convergence Performance

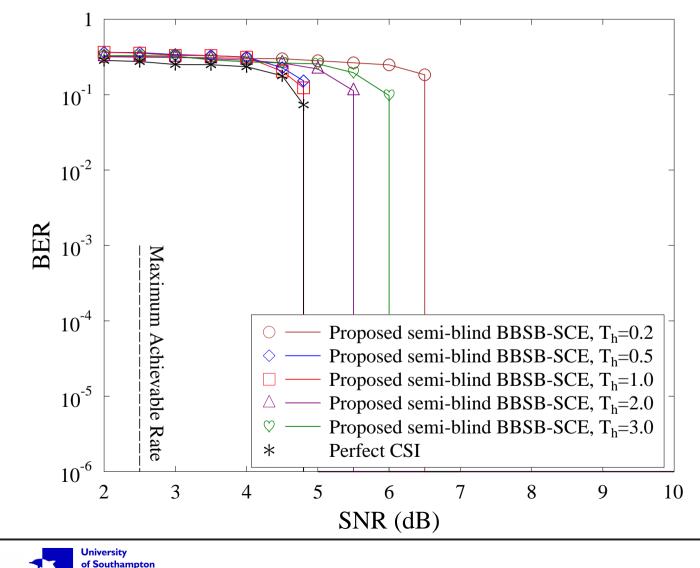
• BER convergence performance versu outer iterations of the proposed joint BBSB-SCE and three-stage turbo receiver with a block-of-bits selection threshold of $T_h = 1.0$, in comparison to the perfect-CSI case





Influence of Selection Threshold

- Effects of the block-of-bits selection threshold T_h on the BER performance of our proposed semi-blind joint BBSB-SCE and three-stage turbo receiver
- $T_h \in [0.5, 1.0]$ appropriate for this example, and as long as the threshold is not chosen to be too small or too large, the scheme is not sensitive to the value of T_h used



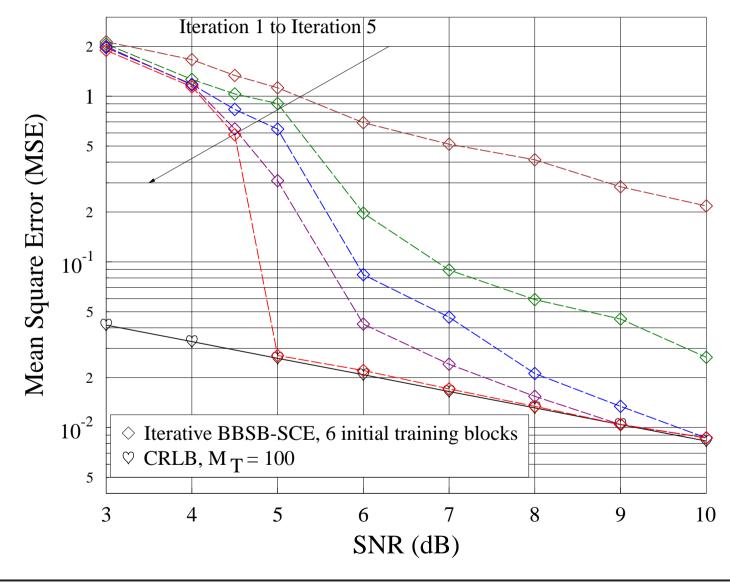


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MSE Convergence Performance

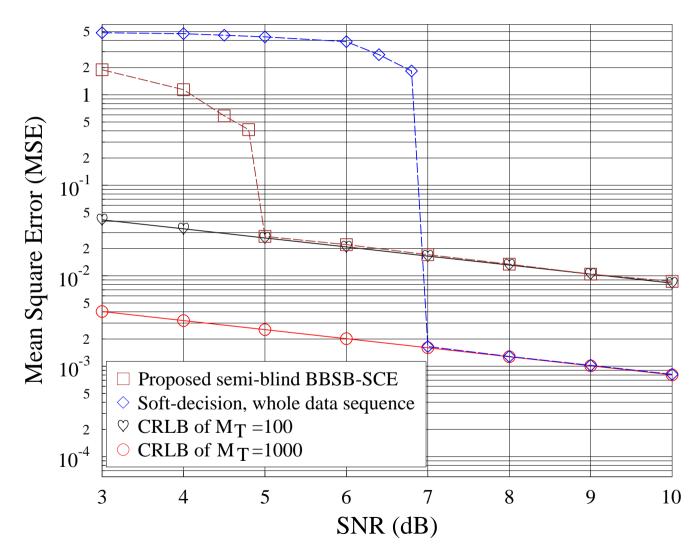
• Mean square error convergence performance versu outer iterations of the channel estimator in our proposed semi-blind joint BBSB-SCE and three-stage turbo receiver using a block-of-bits selection threshold of $T_h = 1.0$ and $M_s^t \le 100$





MSE Performance Comparison

• MSE performance comparison: proposed joint BBSB-SCE and three-stage turbo receiver, which selects $M_s^t \leq 100$ high-quality soft detected symbol vectors for channel estimator, and conventional joint CE and three-stage turbo receiver, which uses all $M_F = 1000$ soft detected symbol vectors for channel estimator





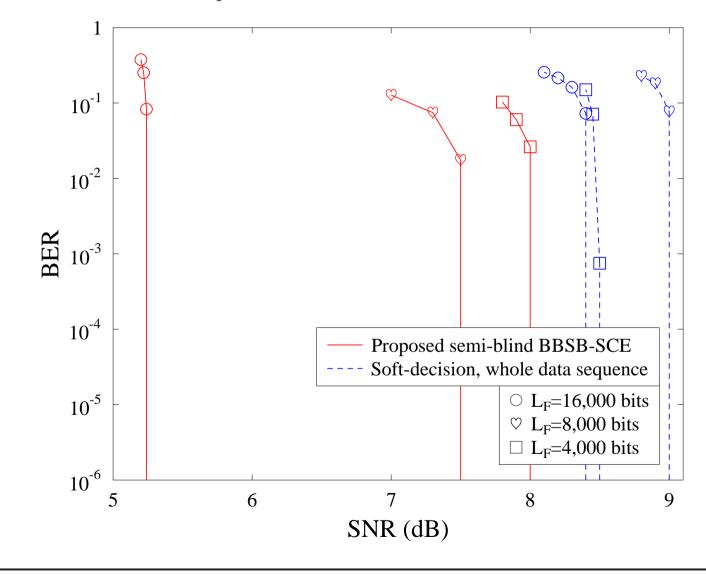
Simulation System (2)

- Time-varying Rayleigh fading MIMO: System settings identical to Simulation System (1), except
 - MIMO channels are faded at symbol rate with normalised Doppler frequency f_d
- For time-varying MIMO: trade off between time-varying channel's estimation (TVCE) performance and turbo channel decoder's performance
 - For turbo channel coding, a **long** interleaver length L_F is preferred for the sake of achieving near-capacity performance
 - A short frame length M_F , i.e. a **short** interleaver length L_F is preferred for the sake of achieving a good TVCE performance.
- We compare our proposed scheme with the existing stat-of-the-art that uses entire soft-decision frame for CE, in terms of **achievable bit error rate**
 - Computational complexity of our scheme is dramatically lower

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• BER performance comparison: a) proposed joint BBSB-SCE and three-stage turbo receiver with $T_h = 1.0$, and b) existing joint CE and three-stage turbo receiver employing the entire detected data sequence for the soft decision aided channel estimator, for the time-varying MIMO system with the interleaver lengths of $L_F = 16,000$ bits, 8,000 bits and 4,000 bits, respectively.

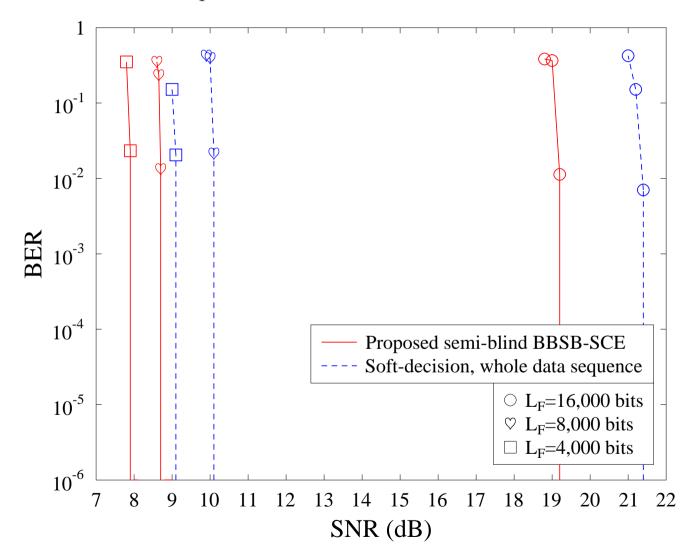




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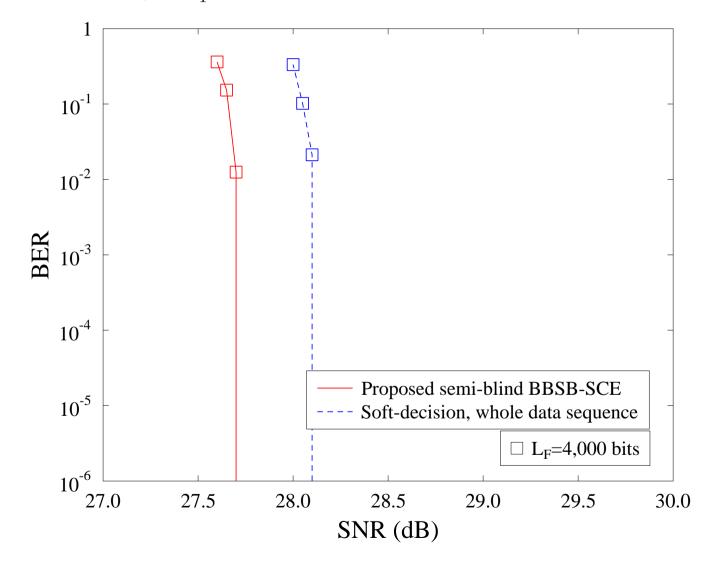
• BER performance comparison: a) proposed joint BBSB-SCE and three-stage turbo receiver with $T_h = 1.0$, and b) existing joint CE and three-stage turbo receiver employing the entire detected data sequence for the soft decision aided channel estimator, for the time-varying MIMO system with the interleaver lengths of $L_F = 16,000$ bits, 8,000 bits and 4,000 bits, respectively.





$$f_d = 5 \times 10^{-4}$$

BER performance comparison: a) proposed joint BBSB-SCE and three-stage turbo receiver with $T_h = 1.0$, and b) existing joint CE and ۲ three-stage turbo receiver employing the entire detected data sequence for the soft decision aided channel estimator, for the time-varying MIMO system with the interleaver length of $L_F = 4,000$ bits.



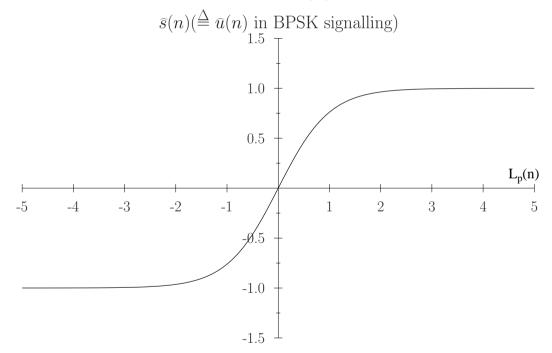


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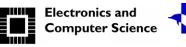
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Simulation System (3)

- Quasi-static Rayleigh fading MIMO: $N_T = N_R = 2$, BPSK, and $M_T = 6$
 - Other system settings identical to Simulation System (1)
- For **BPSK**, there exists a scheme of selecting high-quality bits according to LLRs $L_p^{I_{in}}(n)$
 - T. Abe and T. Matsumoto, "Space-time turbo equalization in frequency-selective MIMO channels," *IEEE Trans. Vehicular Technology*, 52(3), 469–475, 2003



- Soft symbol (bit) estimate $\hat{s}(n) = \tanh (L_p^{I_{\text{in}}}(n))$: magnitude $|\hat{s}(n)|$ as estimated probability of *n*th bit \Rightarrow decide whether this bit is reliable or not

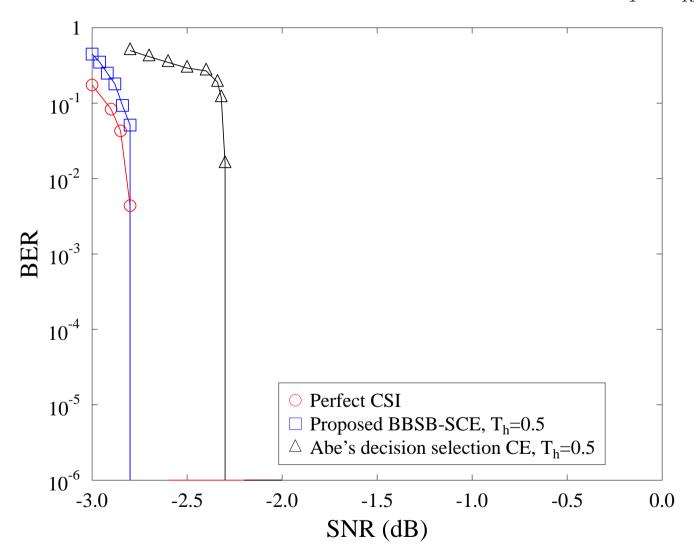


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BER Performance Comparison

• BER performance comparison: a) perfect CSI case, b) proposed joint BBSB-SCE and three-stage turbo receiver with $T_h = 0.5$, and c) Abe and Matsumoto's BPSK decision selection scheme based soft CE, for quasi-static **BPSK MIMO** system with $N_T = N_R = 2$.





Summary

- Our challenging objective is to reach MIMO wonderland
 - with aid of very modest (minimum) training overhead
 - without significantly increasing associated complexity
- Semi-blind iterative **block-of-bits selection** based soft-decision aided channel estimation and three-stage turbo detection-decoding
 - 1. Only utilize high-quality or reliable detected symbols \Rightarrow **not entire frame** of detected soft bits for CE, dramatically reducing CE complexity
 - 2. Channel estimation naturally embedded in original turbo detection-decoding process \Rightarrow **no extra iterative loop** between CE and turbo detector-decoder
 - 3. Capable of **attaining optimal** ML turbo detector-decoder bound associated with perfect CSI, while imposing similar complexity
- With this **BBSB-SCE** scheme, we can reach **MIMO** wonderland



References

- 1. Wang, Ng, Wolfgang, Yang, Chen, Hanzo, "Near-capacity three-stage MMSE turbo equalization using irregular convolutional codes," in: Proc. Turbo-Coding-2006 (Munich, Germany), April 3-7, 2006, 6 pages.
- 2. Hanzo, Alamri, El-Hajjar, Wu, Near-Capacity Multi-Functional MIMO Systems: Sphere-Packing, Iterative Detection and Cooperation. John Wiley & Sons, 2009.
- 3. Zhang, Chen, Hanzo, "Reduced-complexity near-capacity joint channel estimation and three-stage turbo detection for coherent space-time shift keying," IEEE Trans. Communications, vol.61, no.5, pp.1902–1913, May 2013
- 4. Zhang, Chen, Hanzo, "Embedded iterative semi-blind channel estimation for threestage-concatenated MIMO-aided QAM turbo-transceivers," IEEE Trans. Vehicular Technology, vol.63, no.1, pp.439–446, Jan. 2014



Next Big Challenge: Pilot Contamination

- What we have discussed is effectively **single-cell** MIMO
- Practical systems are **multi cells**, and every cell needs to do training for estimating its associated MIMO CSI, causing pilot contamination across cells
- Pilot contamination in multi-cell MIMO is a **big big** challenge, and it is currently a hot topic
- Our recent work on pilot contamination problem:

Zhang, Zhang, Chen, Mu, El-Hajjar, Hanzo, "Pilot contamination elimination for large-scale multiple-antenna aided OFDM systems," *IEEE J. Selected Topics in Signal Processing*, Special Issue on Signal Processing for Large-Scale MIMO Communications, vol.8, no.5, pp.759–772, 2014



Next Big Challenge: Massive MIMO

- Everyone is talking about massive MIMO, as it is supposed to bring an even more wonderful wonderland
 - In theory, we can have massive **diagonal** MIMO with huge number of parallel channels or digital pipes
- Massive MIMO also bring about massive problem
 - While it may become easy to realize 10 antennas, it is another matter to implement 10 radio frequency chains, not to say tens or hundreds
- While we may have many many antennas in system, in practice, we may only have a few RF chains
 - To best utilize this limited hardware resource, the solution is to select the best subset of antennas to form the associated subset MIMO



Our Recent Works

- P. Zhang, S. Chen, C. Dong, L. Li and L. Hanzo, "Norm-based joint transmit/receive antenna selection aided and two-tier channel estimation assisted STSK systems," in *Proc. ICC 2014* (Sydney, Australia), June 10-14, 2014, pp.1-6
- P. Zhang, S. Chen and L. Hanzo, "Two-tier channel estimation aided near-capcity MIMO transceivers relaying on norm-based joint transmit and receive antenna selection," *IEEE Trans. Wireless Communications*, to appear, 2015
- J. Jiang, P. Zhang, R. Zhang, S. Chen and L. Hanzo, "Aperture selection for ACO-OFDM in free-space optical turbulence channel," submitted to *IEEE Trans. Vehicular Technology*



