Revision of Lecture Six

- We have discussed phase shift keying, in particular, one bit per symbol BPSK and two bits per symbol QPSK
- Carrier recovery operation and clock recovery operation, in particular,
 - Time-2 carrier recovery: suitable for binary modulation scheme
 - Time-2, early-late, zero crossing clock recovery schemes: suitable for binary signalling, and synchroniser clock recovery: generally applicable

Carrier recovery and clock recovery are important, as each transceiver has a pair

• This lecture looks into bandwidth much more efficient modulation scheme called **quadrature amplitude modulation**, with emphasis on general **design considerations** of digital modulation scheme

When one gains bandwidth efficiency, what is penalty ? (hint: From channel capacity, one can trade-off bandwidth / SNR. What about power efficiency?)

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Linear and Nonlinear Modulation

• PSK belongs to the class of **linear modulation**, where the RF signal amplitude varies linearly with the modulating digital signal

This can be seen from the PSK RF signal:

 $s_i(t) = A\left(\cos(\phi_i(t))\cos(\omega_c t) - \sin(\phi_i(t))\sin(\omega_c t)\right)$

Another example is amplitude shift keying

- Linear modulation techniques are **bandwidth efficient** but **power inefficient**, requiring expensive linear amplifiers
- A class of **nonlinear modulation** are constant envelope modulation techniques An example is frequency shift keying
- Nonlinear modulation techniques are bandwidth less efficient but power efficient, no need for expensive linear amplifiers



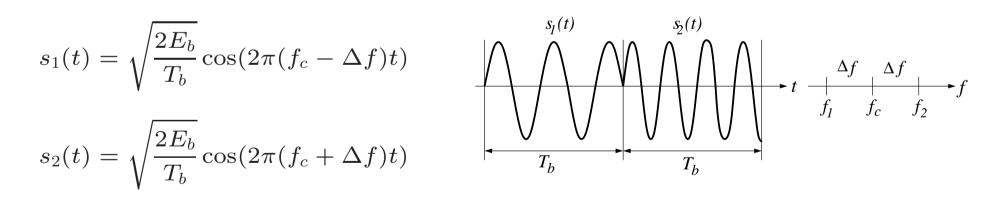
Frequency Shift Keying

• FSK: a **constant envelope** modulation, f_i carries symbol information

$$s_i(t) = A\cos(2\pi f_i t + \theta), \ 1 \le i \le M, \ 0 \le t \le T_s$$

BFSK, QFSK, etc. Coherent and non-coherent detection can be used

• BFSK: M=2, bit 0: $f_1=f_c-\Delta f$, bit 1: $f_2=f_c+\Delta f$



• BFSK RF bandwidth (raised cosine): $B_p = 2\Delta f + 2B = 2\Delta f + (1 + \gamma)R_b$, where *B* is the baseband digital signal bandwidth (Note: BPSK $B_p = (1 + \gamma)R_b$)

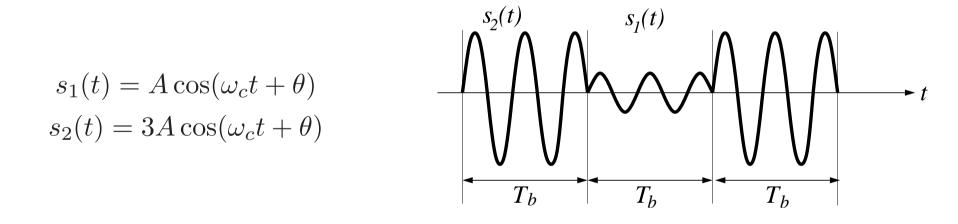


Amplitude Shift Keying

• ASK: A_i carries symbol information

$$s_i(t) = A_i \cos(\omega_c t + \theta), \ 1 \le i \le M, \ 0 \le t \le T_s$$

• BASK: M = 2, bit 0: $A_1 = A$, bit 1: $A_2 = 3A$



- For ASK, **linear amplifier is essential**. A nonlinear channel can seriously distort ASK signals, and ASK is rarely used on it own
- Typically, ASK and PS are combined \Rightarrow quadrature amplitude modulation



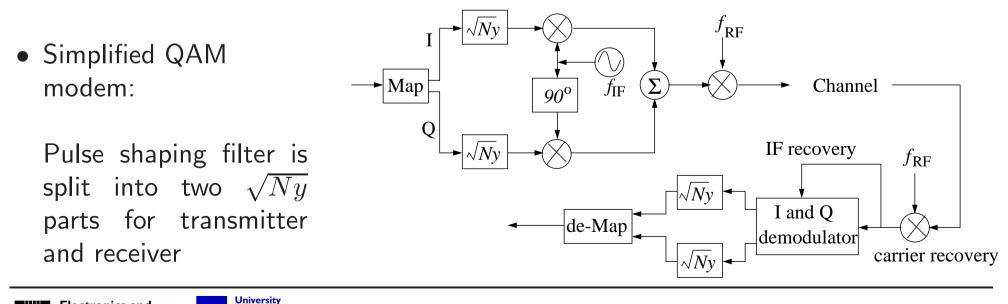
Quadrature Amplitude Modulation

• QAM: combined amplitude/phase keying

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 $s_i(t) = A_i \cos(\omega_c t + \phi_i(t)), \ 0 \le t \le T_s, \ 1 \le i \le M$

- T_{s} being symbol period, as both amplitude and phase are used to carry symbol information, it is very bandwidth efficient
- symbol set size $M: 2^1 \times 2^1 = 4$, $2^2 \times 2^2 = 16$, $2^3 \times 2^3 = 64$, etc \longrightarrow 4QAM, 16QAM, 64QAM with 2, 4, 6 BPS etc
- The larger M is, the better bandwidth efficiency but lower robustness against noise and fading





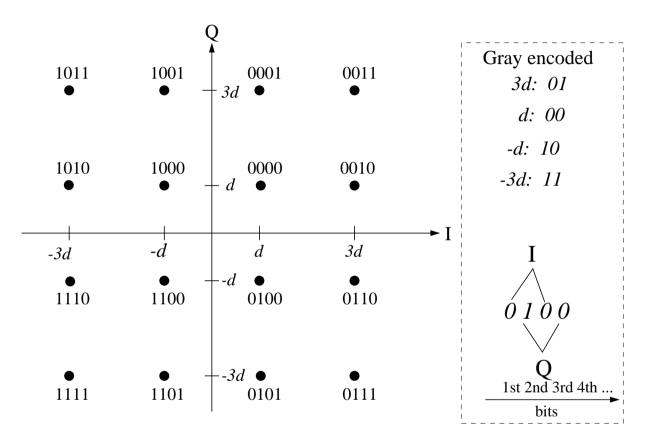
Mapping Bits to Symbols

• Example: squared 16-QAM

Shortest distance among the neighbour points is $2d \ % d = \frac{1}{2} d \ d = \frac$

Bit stream is split into

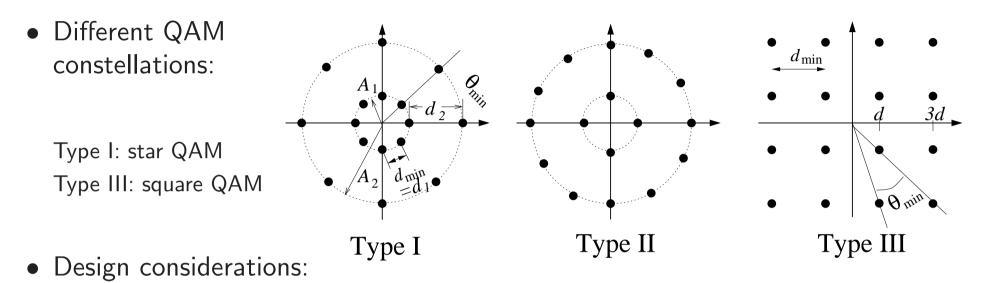
 I and Q streams.
 I and Q are Gray encoded
 (neighbour points only
 differ in 1 bit position) to
 produce symbol points in
 constellation



• For squared 16QAM, I and Q components are Gray encoded by assigning the bits 01, 00, 10 and 11 to the levels 3d, d, -d and -3d

For 4-QAM, I and Q are BPSK; for 16QAM, I and Q are 4-ary; For M-QAM, I and Q are \sqrt{M} -ary





(1) The **minimum distance** d_{\min} among phasors, which is the characteristic of the noise immunity of the scheme

(2) The minimum phase rotation θ_{\min} among constellation points, determining the phase jitter immunity and hence resilience against clock recovery errors and channel phase rotation

(3) The ratio of peak-to-average power r, which is a measure of robustness against nonlinear distortions introduced by the power amplifier



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QAM Design Considerations (continue)

 Comparison for 16QAM: 	Туре	$ heta_{\min}$	d_{\min}	r
$ullet$ Type III: $ heta_{ m min} < 45^{ m o}$ and $d_{ m min} = 2d$		45°	$0.53\sqrt{E_s}$	1.5
Peak energy is $(9d^2+9d^2)=18d^2$		$< 45^{\circ}$	$0.63\sqrt{E_s}$	1.8
Average energy is				
$E_s = \frac{4 \times (d^2 + d^2) + 8 \times (9d^2 + d^2) + 4 \times (9d^2 + 9d^2)}{16} = 10d^2$				
Thus $d_{ m min}=2d=2\sqrt{E_s/10}pprox 0.63\sqrt{E_s}$ and $r=rac{18d^2}{10d^2}=1.8$				
• For optimum type I: $d_1=d_2=d$ and $ heta_{\min}=45^{ m o}$				
$d_1=2A_1\cos(67.5^\circ)$ or $A_1pprox 1.31d$, and $A_2=A_1+dpprox 2.31d$. Since average energy				
$E_s = \frac{8 \times A_1^2 + 8 \times A_2^2}{16} = \frac{A_1^2 + A_2^2}{2} \approx 3.53d^2$				
$d_{ m min}pprox \sqrt{E_s/3.53}pprox 0.53\sqrt{E_s}$. Also peak energy is A_2^2 , so $rpprox rac{(2.31d)^2}{3.53d^2}pprox 1.5$				
• Type I has a higher jitter immunity and slightly lower peak-to-average energy ratio than type III, and it is more robust to fading and has better power efficiency				
However, type III has an almost 20% ((0.63-0.53)/0.53) higher minimum distance at the same average energy and it is optimum in terms of error probability for AWGN channels				

Intermediate Frequency Modulation

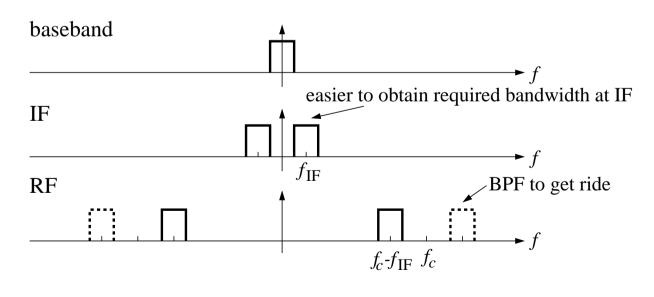
• In theory, the modulation is done by multiplying baseband signal with carrier

 $s(t) = m_I(t)\cos(2\pi f_c t) + m_Q(t)\sin(2\pi f_c t)$

- In practice, however, it is often seen that modulation is first via an intermediate frequency modulation and then RF modulation by f_c , as in slide 71 of QAM modem
- Modulation will introduce noise and spread power into adjacent bands

So BPF (not shown in slide 71) must be used to obtain required bandwidth

• This is easier at a low frequency (IF) than at RF





Example

The Shannon-Hartley law is given by:

$$\frac{C}{B_p} = \log_2(1 + \mathsf{SNR}) \ \frac{\mathsf{bps}}{\mathsf{Hz}}$$

where B_p is the RF channel bandwidth in Hz and C is the channel capacity in bps.

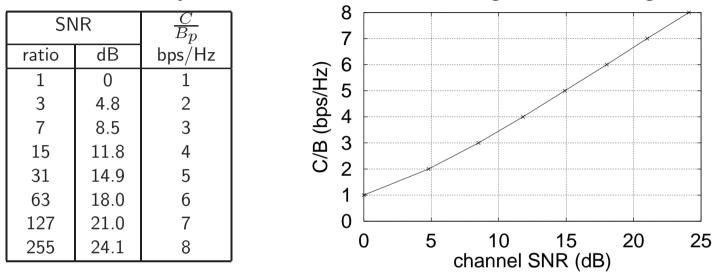
- 1. Assuming the roll-off factor $\gamma = 0$, state the minimum required channel SNR for supporting 1, 2 and 4 bit/symbol (BPS) BPSK, QPSK and 16QAM, respectively, signalling over Gaussian channels.
- 2. Assuming $\gamma=0.5$ and a channel bandwidth of 600 kHz, calculate the achievable bit rate of BPSK, QPSK and 16QAM.

Note: Shannon-Hartley channel capacity is for Gaussian signal. BPSK, QPSK and 16QAM are not Gaussian signal, although PDF of 16QAM signal is much closer to a Gaussian PDF than PDF of BPSK signal. Nevertheless, we use this ideal case channel capacity as though it were the channel capacity of BPSK, QPSK and 16QAM channels, i.e. we use the upper limit.



Solution

From the Shannon-Hartley law, we have the following table and figure:



- 1. Noting $\gamma = 0$, the symbol or transmission rate $f_s = B_p$, that is, C/B_p is the same as BPS. Thus, the minimum required channel SNRs for supporting 1, 2 and 4 BPS BPSK, QPSK and 16QAM are 0, 4.8 and 11.8 dB, respectively.
- 2. For $\gamma = 0.5$, $B_p = (1 + \gamma)f_s = 1.5f_s$, leading to $f_s = 400$ kHz. The data rate (bps) $R = BPS \times f_s$. Thus, $R_{BPSK} = 400$ kbps, $R_{QPSK} = 800$ kbps, and $R_{16QAM} = 1600$ kbps.



Summary

- PSK: is a linear modulation, bandwidth efficient but power inefficient
- FSK: waveform, frequencies carry symbol information, BFSK, QFSK etc

is a constant envelope (nonlinear) modulation, bandwidth inefficient but power efficient

- ASK: waveform, amplitudes carry symbol information, is a linear modulation and rarely used on it own
- QAM: combining ASK and PSK, bandwidth very efficient, is a linear modulation waveform, QAM modem diagram, mapping bits to symbols type of constellations, constellation design considerations why IF stage



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