

# Polarization Sensitive Array Based Physical-Layer Security

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**Abstract**—We propose a framework exploiting the polarization sensitive array (PSA) to improve the physical layer security of wireless communications. Specifically, the polarization difference among signals is utilized to improve the secrecy rate of wireless communications, especially when these signals are spatially indistinguishable. We firstly investigate the PSA based secure communications for point-to-point wireless systems from the perspectives of both total power minimization and secrecy rate maximization. We then apply the PSA based secure beamforming designs to relaying networks. The secrecy rate maximization for relaying networks is discussed in detail under both the perfect channel state information and the polarization sensitive array pointing error. In the later case, a robust scheme to achieve secure communications for relaying networks is proposed. Simulation results show that the proposed PSA based algorithms achieve lower total power consumption and better security performance compared to the conventional scalar array designs, especially under challenging environments where all received signals at destination are difficult to distinguish in the spatial domain.

**Index Terms**—Physical layer security, polarization sensitive arrays, point-to-point wireless systems, relaying networks.

## I. INTRODUCTION

THE issue of information security in wireless networks has attracted extensive attention in recent years considering the openness of wireless links [1], [2]. Traditionally, encryption techniques are utilized to ensure secure communications, which are generally applied in the upper layer of network and have a high design complexity [3]. Therefore, an intrinsic approach exploring the characteristics of wireless fading channels to improve information security emerges as a prominent technique, which is referred to as the physical layer security [4]. The fundamental theory for physical layer security was firstly established by Shannon [5]. Following Shannon's work, Wyner [6] introduced the famous wiretap channel model and further

defined the channel secrecy capacity. The work [7] proposed a Gaussian degraded wiretap channel which is widely used to model the wireless propagation environment.

Based on these pioneering theoretical concepts, a large amount of literature focusing on various design aspects of secure communications have sprung up. By applying multiple antennas at communication nodes to exploit spatial freedom, these researches aimed to significantly improve the physical layer security of wireless networks [8]–[11]. For example, an artificial noise scheme was proposed for wiretap channels in [8] to study the impact of antenna selection on security performance of multi-input multi-output (MIMO) two-way relaying networks. The work [9] introduced an effective method called cooperative jamming to confuse the eavesdropper deliberately. With the aid of the game theory, a collaborative physical-layer security transmission scheme was designed in [10] to effectively balance the security performance among different links. All these works however assume that the wireless channels are ideally Rayleigh distributed, which ignores the influence of array directivity and correlation. A technique known as the directional modulation was also investigated to realize secure communications. In the work [12], the directional modulation technique was applied to the phased array to offer security. Specifically, by shifting each array element's phase appropriately, the desired symbol phase and amplitude in a given direction is generated. The study [13] on the other hand adopted the directional modulation technique to enhance the security of multi-user MIMO systems. Different from the standard secrecy rate optimization, the secure communications of multi-user MIMO systems are achieved by increasing the symbol error rate at the eavesdropper. It can be seen that the directional modulation technique designs the weighting coefficients of the phased array. As will be shown, our polarization sensitive array (PSA) based technique designs the spatial pointing of each antenna to effectively extract the signals' polarization information for realizing secure communications.

Generally, the polarization status, similar to the amplitude and phase, is a feature of the signal. Many researches have indicated that the direction-finding performance and short-wave communication quality can be improved by means of the polarization difference among signals [14]. However, in many practical communication scenarios, such as radar and electronic reconnaissance, the conventional scalar array (CSA) is widely deployed. In essence, the CSA is the uniformly spaced linear array with the same spatial properties in all its array elements.

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Generally, CSA is blind to the polarization status of signal and sensitive to the array aperture and signal wavelength [15]. Worse still, in some specific array alignment, a CSA may present the morbid response to the polarization status of signal. Different from the CSA, the PSA consists of a certain number of antennas with different spatial pointings, which can be utilized to extract the signal information more meticulously and comprehensively in a vector way [16], [17]. The spatial pointings of the PSA offer extra design degrees of freedom for physical layer security of wireless networks. In most practical wireless networks, jammer is typically introduced to effectively interfere with the eavesdropper, but it simultaneously causes the interference to the destination. When the jammer signal has approximately the same spatial properties as the source, the CSA based destination beamforming optimization is unable to suppress the interference, as it can only rely on the signals' spatial characteristics. By contrast, since different polarization information can be extracted by the spatial pointings of PSA, the PSA based destination beamforming optimization is capable of suppressing the interference effectively, even when the signals are indistinguishable in the spatial domain. Therefore, utilizing the PSA to realize secure communications for wireless networks can achieve superior performance over the CSA design.

However, most existing PSA related works focus on the problem of estimating the signal's direction of arrival (DOA). In [18], a two-step maximum-likelihood signal estimation procedure was developed under the PSA. Based on the sparse polarization sensor measurements, the DOA estimation of the transmitted signal was conducted in [19]. There also exist some works specifically related to the optimization of dual-polarization array to enhance the system capacity. Compared to the single polarization array, the orthogonal dual polarization antenna can enhance MIMO spatial multiplexing gain remarkably by means of the eigenvalue ratio decomposition [20]. The study [21] designed a linear-polarized dual-polarization frequency reuse system to increase spectrum utilization and further improve the system capacity, while the work [22] compared three different transmission schemes for MIMO networks to achieve the maximum diversity under a dual-polarization channel model. All these works do not consider utilizing PSA to enhance secure communications.

Against the above background, this paper investigates the PSA based secure transmission strategy for wireless networks. Specifically, we first consider the PSA based secure communications for the point-to-point single-input multi-output (SIMO) network with the aid of jammer. In this case, the secure beamforming is firstly designed aiming at minimizing the total transmit power subject to the secrecy rate requirements. Then the secrecy rate maximization scheme is proposed to improve the secrecy capacity of SIMO network as much as possible. Further extending our research into the more complicated scenario where the relay is employed to enlarge the communication coverage of source nodes, we consider the secrecy rate maximization under both perfect channel state information (CSI) and imperfect PSA pointing, respectively. It is worth noting that convex optimization techniques [23] can be utilized to solve the optimization problems formulated in this paper effectively.

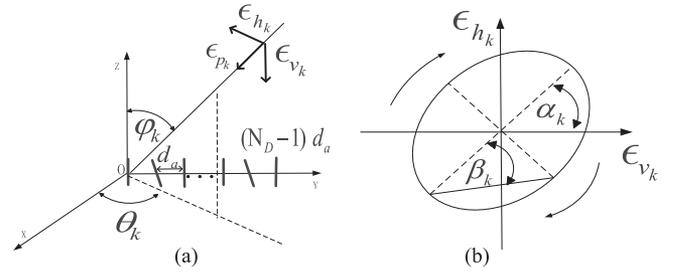


Fig. 1. Polarization sensitive array model: (a) the uniform linear crossed dipole array with  $N_D$  antennas, and (b) the polarized ellipse of EM signal.

Throughout our discussions, the following notational conventions are adopted. The normal-faced lower-case letters denote scalars, while bold-faced lower-case and upper-case letters stand for vectors and matrices, respectively.  $||$  denotes the absolute value and  $|||$  denotes the Euclidean norm, while  $(\cdot)^*$ ,  $(\cdot)^T$ ,  $(\cdot)^H$  and  $(\cdot)^{-1}$  represent the conjugate, transpose, conjugate transpose and inverse operators, respectively. An optimal solution is marked by  $*$ , while  $\text{tr}(\cdot)$  and  $\text{rank}(\cdot)$  denote the trace and rank of matrix, respectively. The  $n$ th row of matrix  $\mathbf{A}$  is given by  $\mathbf{A}[n, :]$ , and the  $n$ th-row and  $m$ th-column element of  $\mathbf{A}$  is  $\mathbf{A}[n, m]$ .  $\mathbf{A} \succeq 0$  means that  $\mathbf{A}$  is a positive semidefinite matrix. The vector stacking operator  $\text{vec}(\cdot)$  stacks the columns of a matrix on top of one another, and  $\text{diag}\{u_1, \dots, u_N\}$  is the diagonal matrix with the diagonal elements  $u_1, \dots, u_N$ .  $\mathbf{I}_N$  is the  $N \times N$  identity matrix, and  $\mathbf{0}_{n \times m}$  is the  $n \times m$  matrix with all zero elements.  $\mathbf{a} \sim \mathcal{CN}(\mathbf{0}, \sigma^2 \mathbf{I})$  means that  $\mathbf{a}$  is a complex Gaussian distributed random vector with the zero mean vector  $\mathbf{0}$  and the covariance matrix  $\sigma^2 \mathbf{I}$ , while  $\mathbf{E}\{\cdot\}$  is the expectation operator. The determinant operation is denoted by  $\det(\cdot)$ , and  $\otimes$  denotes the Kronecker product. Finally,  $j = \sqrt{-1}$ , and  $[a]^+ = \max\{0, a\}$ .

## II. POLARIZATION SENSITIVE ARRAY SYSTEM MODEL

Without loss of generality, we assume that a total of  $N_D$  antennas are located in the  $y$ -axis and the distance  $d_a$  between the adjacent antennas is half wavelength, as illustrated in Fig. 1(a). Here two plane electromagnetic (EM) signals are considered, i.e., the desired EM signal  $s_d$  and the jamming EM signal  $s_j$ . They arrive at the  $N_D$  antennas of the PSA from different incident angles. As is well known, the EM wave is traveling in a single direction, where the electric component and the magnetic component are perpendicular to each other as well as perpendicular to this propagation direction. Taking the electric component as an example, we define the transverse electric field vectors of the EM signal  $s_k$  as

$$\mathbf{e}_{s_k}(t) = e_{h_k}(t)\boldsymbol{\epsilon}_{h_k} + e_{v_k}(t)\boldsymbol{\epsilon}_{v_k}, \quad k = d, j, \quad (1)$$

where  $e_{h_k}(t)$  and  $e_{v_k}(t)$  are the electric field projections on the  $\boldsymbol{\epsilon}_{h_k}$  and  $\boldsymbol{\epsilon}_{v_k}$  directions, respectively. As a result, the magnetic field biases of the EM signal are  $\boldsymbol{\epsilon}_{v_k}$  and  $-\boldsymbol{\epsilon}_{h_k}$ , respectively, for keeping the orthogonality [24]. Furthermore, it is assumed that the EM signals are completely polarized signals which means that the time varying  $e_{h_k}(t)$  and  $e_{v_k}(t)$  can be formulated as an

ellipse. As described in Fig. 1(b),  $\alpha_k$  and  $\beta_k$  are the polarization orientation and ellipse angle, respectively, which represent the track of the EM signal's electric vector and are thereafter called the POA for short. According to the EM theory [19]–[22], [24]–[26], we can express the EM signal in a vector form with its DOA  $(\theta_k, \varphi_k)$  and POA  $(\alpha_k, \beta_k)$  as follows

$$\hat{\mathbf{s}}_k = \Xi(\theta_k, \varphi_k) \mathbf{R}(\alpha_k) \ell(\beta_k) = [\hat{\mathbf{s}}_k(1) \cdots \hat{\mathbf{s}}_k(6)]^T, \quad k = d, j, \quad (2)$$

where  $\theta_k$  and  $\varphi_k$  are the azimuth and elevation angles of the EM signal  $s_k$ , respectively, while

$$\Xi(\theta_k, \varphi_k) = \begin{bmatrix} \epsilon_{h_k} & \epsilon_{v_k} \\ \epsilon_{v_k} & -\epsilon_{h_k} \end{bmatrix} = \begin{bmatrix} -\sin \theta_k & \cos \varphi_k \cos \theta_k \\ \cos \theta_k & \cos \varphi_k \sin \theta_k \\ 0 & -\sin \varphi_k \\ \cos \varphi_k \cos \theta_k & \sin \theta_k \\ \cos \varphi_k \sin \theta_k & -\cos \theta_k \\ -\sin \varphi_k & 0 \end{bmatrix}, \quad (3)$$

$$\mathbf{R}(\alpha_k) = \begin{bmatrix} \cos \alpha_k & -\sin \alpha_k \\ \sin \alpha_k & \cos \alpha_k \end{bmatrix} \quad \text{and} \quad \ell(\beta_k) = \begin{bmatrix} \cos \beta_k \\ \sin \beta_k \end{bmatrix}. \quad (4)$$

$\Xi(\theta_k, \varphi_k)$  is the steering matrix of  $s_k$ , which is composed of the electric and magnetic field bases of the EM signal, while  $\mathbf{R}(\alpha_k)$  and  $\ell(\beta_k)$  are the corresponding rotation and ellipticity matrix of  $s_k$ , respectively, [26].

In addition to the polarization of EM signals, the antenna polarization should also be considered. It is noted that only short dipole antennas are adopted in our work, and thus the array magnetic response can be neglected. Besides, the polarization sensitive matrix  $\mathbf{P}$  which represents the polarization characteristics of the array is defined by the spatial pointing angles of the  $N_D$  antennas of the PSA, i.e.,  $(\theta^{(e,n)}, \varphi^{(e,n)})$  for  $0 \leq n \leq N_D - 1$ , where  $\theta^{(e,n)}$  and  $\varphi^{(e,n)}$  are the azimuth and elevation pointing angle of the  $n$ th antenna of the PSA, respectively. Mathematically, we have

$$\mathbf{P} = [\mathbf{P}_e \mathbf{0}] = \begin{bmatrix} p_{e,x}^{(0)} & p_{e,y}^{(0)} & p_{e,z}^{(0)} & 0 & 0 & 0 \\ p_{e,x}^{(1)} & p_{e,y}^{(1)} & p_{e,z}^{(1)} & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ p_{e,x}^{(N_D-1)} & p_{e,y}^{(N_D-1)} & p_{e,z}^{(N_D-1)} & 0 & 0 & 0 \end{bmatrix}, \quad (5)$$

with

$$\begin{bmatrix} p_{e,x}^{(n)} \\ p_{e,y}^{(n)} \\ p_{e,z}^{(n)} \end{bmatrix} = G_e \begin{bmatrix} \sin \varphi^{(e,n)} \cos \theta^{(e,n)} \\ \sin \varphi^{(e,n)} \sin \theta^{(e,n)} \\ \cos \varphi^{(e,n)} \end{bmatrix}, \quad 0 \leq n \leq N_D - 1, \quad (6)$$

where  $G_e$  is the antenna gain, which takes the value of 1 when the polarization status of the EM signal perfectly matches the antenna. Note that the matrix  $\mathbf{0}$  included in  $\mathbf{P}$  indicates that the array magnetic response is ignored. In addition, for the matrix  $\mathbf{P}_e$ , we have

$$\|\mathbf{P}_e[n+1, :]\|^2 = 1, \quad 0 \leq n \leq N_D - 1. \quad (7)$$

It is worth emphasizing that different from [19], where the PSA consists of the aligned short dipole antennas, each antenna of the PSA in our paper is deployed with a different spatial pointing angle, which becomes an optimization variable for secure communications.

Furthermore, the space phase matrix  $\mathbf{U}_k$  of the EM signal  $s_k$  impinging on the PSA is given by

$$\mathbf{U}_k = \text{diag}\{u_{k,0}, u_{k,1}, \dots, u_{k,N_D-1}\}, \quad (8)$$

$$u_{k,n} = e^{-j2\pi(\boldsymbol{\xi}(\theta_k, \varphi_k) \mathbf{r}_n) / \lambda_k} = e^{j\pi n \sin \varphi_k \sin \theta_k}, \quad k = d, j, \quad 0 \leq n \leq N_D - 1, \quad (9)$$

where  $\boldsymbol{\xi}(\theta_k, \varphi_k) = -[\sin \varphi_k \cos \theta_k \sin \varphi_k \sin \theta_k \cos \varphi_k]$  denotes the propagation vector of the EM signal  $s_k$ ,  $\mathbf{r}_n = [0, nd_a, 0]^T$  is the position vector of the  $n$ th polarization antenna, and  $\lambda_k$  is the wavelength of  $s_k$ . Based on (2), (5) and (8), the spatio-polarized manifold for the EM signal  $\hat{\mathbf{s}}_k$  is defined as

$$\mathbf{a}_{\theta_k, \varphi_k, \alpha_k, \beta_k} = \mathbf{U}_k \mathbf{P} \hat{\mathbf{s}}_k = \mathbf{U}_k \mathbf{P} \Xi(\theta_k, \varphi_k) \mathbf{R}(\alpha_k) \ell(\beta_k), \quad (10)$$

for  $k = d, j$ . For notational convenience, we will simplify  $\mathbf{a}_{\theta_k, \varphi_k, \alpha_k, \beta_k}$  as  $\mathbf{a}_k$  in the sequel.

For the sake of maximizing secrecy rate, the PSA's spatial pointings need to be optimized. In order to perform this optimization conveniently, the formulation (10) is rewritten as

$$\mathbf{a}_k = \mathbf{U}_k [\mathbf{P}_e \mathbf{0}] \hat{\mathbf{s}}_k = \mathbf{U}_k \mathbf{P}_e [\hat{\mathbf{s}}_k(1) \hat{\mathbf{s}}_k(2) \hat{\mathbf{s}}_k(3)]^T = \mathbf{Q}_k \mathbf{p}, \quad (11)$$

for  $k = d, j$ , where

$$\mathbf{p} = [p_{e,x}^{(0)} \cdots p_{e,x}^{(N_D-1)} p_{e,y}^{(0)} \cdots p_{e,y}^{(N_D-1)} p_{e,z}^{(0)} \cdots p_{e,z}^{(N_D-1)}]^T = \text{vec}(\mathbf{P}_e) \in \mathbb{R}^{3N_D}, \quad (12)$$

$$\mathbf{Q}_k = [\mathbf{U}_k \otimes \hat{\mathbf{s}}_k(1) \mathbf{U}_k \otimes \hat{\mathbf{s}}_k(2) \mathbf{U}_k \otimes \hat{\mathbf{s}}_k(3)] \in \mathbb{C}^{N_D \times 3N_D}. \quad (13)$$

Clearly, the new vector  $\mathbf{p}$  denotes the PSA's spatial pointings and thus becomes our optimization variables.

### III. POINT-TO-POINT SECRECY BEAMFORMING DESIGN

We consider the simplest but most representative wiretap channel as a source, a destination and an eavesdropper. In most cases, the capacity of the wiretap channel is higher than the main channel owing to the concealment and intention of the eavesdropper. In order to realize secure communications, we introduce a jammer to disturb the eavesdropper sufficiently. In this four-terminal network as depicted in Fig. 2, the source  $S$  and jammer  $J$  are equipped with single antenna, while the eavesdropper  $E$  is equipped with the CSA of  $N_E$  antennas and the destination  $D$  utilizes the PSA with  $N_D$  antennas.<sup>1</sup>

<sup>1</sup>Our work can easily be extended to the more general case, where the eavesdropper is also equipped with the PSA of  $N_E$  antennas. In fact, in this case, all our designs and algorithms remains applicable and effective. Due to the space limitation, the detailed discussions are omitted here. Reader interested to see the achievable performance in the scenario where the eavesdropper is also equipped with the PSA, please refer to <https://arxiv.org/abs/1601.05982>.

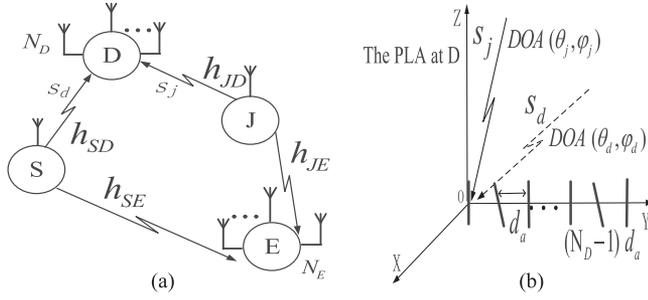


Fig. 2. A point-to-point SIMO network with the polarization sensitive array having  $N_D$  antennas at destination.

Let  $\mathbf{h}_{mn} \sim \mathcal{CN}(\mathbf{0}, \sigma_h^2 \mathbf{I})$  be the channel gain vector from node  $m$  to node  $n$ , where  $m = S, J$  and  $n = E$ . Furthermore, we assume far field communications related to destination  $D$ , and we denote  $h_{SD}$  and  $h_{JD}$  as the channel gains from source  $S$  and jammer  $J$  to the reference antenna (the first antenna) of the PSA at destination  $D$ , respectively. It is worth pointing out that the eavesdropper  $E$  in our work is a legitimate, active but non-intended receiver, which means that  $E$  can simultaneously transmit signals to other nodes and intercept the confidential signal from source. Based on this assumption, the CSI of eavesdropper  $E$  is available through a training-based channel estimation technique. For the sake of improving security performance of the SIMO network, a beamforming vector  $\boldsymbol{\omega}_d = [\omega_0 \omega_1 \cdots \omega_{N_D-1}]^T$  satisfying  $\|\boldsymbol{\omega}_d\|^2 = 1$  is applied to the  $N_D$  antennas of the PSA to maximize the received confidential signal to interference plus noise ratio (SINR). Based on this setting, source  $S$  and jammer  $J$  simultaneously transmit the confidential signal  $\hat{s}_d$  and the jammer signal  $\hat{s}_j$  to the destination  $D$  and eavesdropper  $E$ , respectively. Here,  $\mathbf{E}\{|\hat{s}_d|^2\} = \mathbf{E}\{|\hat{s}_j|^2\} = 1$  is assumed. Since  $\hat{s}_d$  and  $\hat{s}_j$  are far field signals relative to the PSA, the signals  $s_d$  and  $s_j$  impinging on the reference antenna of the PSA from source  $S$  and jammer  $J$  are represented as  $s_d = h_{SD} \sqrt{P_S} \hat{s}_d$  and  $s_j = h_{JD} \sqrt{P_J} \hat{s}_j$ , respectively, where  $P_S$  and  $P_J$  denote the transmit powers of source  $S$  and jammer  $J$ , respectively.

Because both source  $S$  and jammer  $J$  are far-field narrowband synchronized transmitters,<sup>2</sup> the change of the complex envelope of the corresponding EM signal when sweeping across the PSA

<sup>2</sup>Synchronizing the transmissions of source and jammer is important. To achieve the synchronization between two transmitters, one of the transmitters can serve as master and the other as slave, see for example [27]. In our case, the source serves as the master, who broadcasts the carrier and timing signals, while the jammer acts as the slave, who locks up to the carrier and timing signals from the master. In this way, the jammer acquires the carrier frequency and phase as well as achieves the timing synchronization with the source.

is negligible. Therefore, the output signals at the PSA and the eavesdropper  $E$  are given respectively as

$$y_D = \boldsymbol{\omega}_d^H \mathbf{Q}_d \mathbf{p} h_{SD} \sqrt{P_S} \hat{s}_d + \boldsymbol{\omega}_d^H \mathbf{Q}_j \mathbf{p} h_{JD} \sqrt{P_J} \hat{s}_j + \boldsymbol{\omega}_d^H \mathbf{n}_D, \quad (14)$$

$$y_E = \boldsymbol{\omega}_e^H \mathbf{h}_{SE} \sqrt{P_S} \hat{s}_d + \boldsymbol{\omega}_e^H \mathbf{h}_{JE} \sqrt{P_J} \hat{s}_j + \boldsymbol{\omega}_e^H \mathbf{n}_E, \quad (15)$$

where  $\boldsymbol{\omega}_e \in \mathbb{C}^{N_E}$  with  $\|\boldsymbol{\omega}_e\|^2 = 1$  is the receive beamforming vector of eavesdropper  $E$ , while  $\mathbf{n}_D \sim \mathcal{CN}(\mathbf{0}, \sigma^2 \mathbf{I}_{N_D})$  and  $\mathbf{n}_E \sim \mathcal{CN}(\mathbf{0}, \sigma_e^2 \mathbf{I}_{N_E})$  are the received Gaussian noise vectors at destination  $D$  and eavesdropper  $E$ , respectively. From the perspective of eavesdropper  $E$ , the optimal  $\boldsymbol{\omega}_e$  is designed to achieve the maximum amount of wiretapped information, i.e., to maximize its desired SINR, which is obtained by solving the following problem

$$\max_{\boldsymbol{\omega}_e} \frac{\boldsymbol{\omega}_e^H \mathbf{h}_{SE} \mathbf{h}_{SE}^H \boldsymbol{\omega}_e}{\boldsymbol{\omega}_e^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E}) \boldsymbol{\omega}_e}. \quad (16)$$

Clearly, the above problem is a standard generalized Rayleigh quotient problem, whose optimal solution is the generalized eigenvector corresponding to the largest generalized eigenvalue of the matrix pencil  $(\mathbf{h}_{SE} \mathbf{h}_{SE}^H, P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})$  [28]. Owing to the fact that the matrix  $P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E}$  is non-singular, the optimal eavesdropper's receive beamforming vector  $\boldsymbol{\omega}_e$  is equivalent to the normalized eigenvector associated with the maximum eigenvalue of the matrix  $(P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE} \mathbf{h}_{SE}^H$ , that is,

$$\boldsymbol{\omega}_e^* = c_e \boldsymbol{\vartheta}_{\max} \left( (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE} \mathbf{h}_{SE}^H \right), \quad (17)$$

where  $c_e$  is a normalized factor to satisfy  $\|\boldsymbol{\omega}_e\| = 1$  and  $\boldsymbol{\vartheta}_{\max}(\mathbf{A})$  denotes the eigenvector corresponding to the maximum eigenvalue of the matrix  $\mathbf{A}$ . Considering the rank-1 property of the matrix  $P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E}$ , the matrix  $(P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE} \mathbf{h}_{SE}^H$  is also rank-1 and only has one nonzero eigenvalue. Specifically, we have the formulation (18) given at the bottom of this page. Thus the unique nonzero eigenvalue and the corresponding eigenvector are  $\mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}$  and  $(P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}$ , respectively. Thus, the optimal eavesdropper's receive beamforming vector (17) can be written as

$$\boldsymbol{\omega}_e^* = \frac{P_J (\mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}}{\|(\mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}\|}. \quad (19)$$

$$\begin{aligned} & \left( (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE} \mathbf{h}_{SE}^H \right) \left( (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE} \right) \\ &= \underbrace{\left( \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE} \right)}_{\lambda_{\max}} \underbrace{\left( (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE} \right)}_{\boldsymbol{\vartheta}_{\max}}. \end{aligned} \quad (18)$$

$$\begin{aligned}
& \min_{P_S, P_J, \mathbf{p}} P_S + P_J, \\
& \text{s.t.} \quad \frac{1 + \sigma^{-2} \mathbf{p}^H (P_S |h_{SD}|^2 \mathbf{Q}_d^H \mathbf{Q}_d + P_J |h_{JD}|^2 \mathbf{Q}_j^H \mathbf{Q}_j) \mathbf{p} + \sigma^{-4} P_S P_J |h_{SD}|^2 |h_{JD}|^2 C_p}{1 + \sigma^{-2} P_J |h_{JD}|^2 \|\mathbf{a}_j\|^2} \\
& \quad \geq 2^{R_{\text{sec}}^0} (1 + P_S \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}), \\
& \quad \text{tr}(\mathbf{p}^T \mathbf{F}_n \mathbf{p}) = 1, 0 \leq n \leq N_D - 1, P_S \geq 0, P_J \geq 0.
\end{aligned} \tag{27}$$

Based on (14) as well as (15) and (19), we formulate the received SINRs at destination  $D$  and eavesdropper  $E$  as

$$\text{SINR}_D = \frac{P_S |h_{SD}|^2 |\omega_d^H \mathbf{Q}_d \mathbf{p}|^2}{\omega_d^H (\sigma^2 \mathbf{I}_{N_D} + P_J |h_{JD}|^2 \mathbf{Q}_j \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H) \omega_d}, \tag{20}$$

$$\begin{aligned}
\text{SINR}_E &= \frac{P_S (\omega_e^*)^H \mathbf{h}_{SE} \mathbf{h}_{SE}^H \omega_e^*}{(\omega_e^*)^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E}) \omega_e^*} \\
&= P_S \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE},
\end{aligned} \tag{21}$$

respectively, where  $\mathbf{p}^T = \mathbf{p}^H$  applies because  $\mathbf{p}$  is a real vector. To realize secure communication of the SIMO network, the security metric called the maximum achievable secrecy rate [6] is considered, which is defined as follows

$$R_{\text{sec}} \leq [I(y_D, \hat{s}_d) - I(y_E, \hat{s}_d)]^+, \tag{22}$$

where  $R_{\text{sec}}$  denotes the achievable secrecy rate,  $I(y_D, \hat{s}_d)$  is the mutual information between source and destination, and  $I(y_E, \hat{s}_d)$  is the mutual information between source and eavesdropper. With the assumption of Gaussian wireless channels,  $I(y_D, \hat{s}_d)$  and  $I(y_E, \hat{s}_d)$  can readily be calculated as  $I(y_D, \hat{s}_d) = \log_2(1 + \text{SINR}_D)$  and  $I(y_E, \hat{s}_d) = \log_2(1 + \text{SINR}_E)$ , respectively. Thus the maximum achievable secrecy rate of the SIMO network is formulated as

$$R_{\text{sec}}^{\max} = \left[ \log_2 \frac{1 + \frac{P_S |h_{SD}|^2 |\omega_d^H \mathbf{Q}_d \mathbf{p}|^2}{\omega_d^H (\sigma^2 \mathbf{I}_{N_D} + P_J |h_{JD}|^2 \mathbf{Q}_j \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H) \omega_d}}{1 + P_S \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}} \right]^+. \tag{23}$$

For the point-to-point SIMO network, we consider two optimization problems, which are the total power minimization under secrecy rate constraint and the secrecy rate maximization under transmit power constraints, respectively.

#### A. Total Power Minimization

The optimization problem is defined as the one that minimizes the total transmit power of the SIMO network subject to the

minimum secrecy rate constraint  $R_{\text{sec}}^0$ , that is,

$$\begin{aligned}
& \min_{P_S, P_J, \mathbf{p}, \omega_d} P_S + P_J, \\
& \text{s.t.} \quad \log_2 \frac{1 + \frac{P_S |h_{SD}|^2 |\omega_d^H \mathbf{Q}_d \mathbf{p}|^2}{\omega_d^H (\sigma^2 \mathbf{I}_{N_D} + P_J |h_{JD}|^2 \mathbf{Q}_j \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H) \omega_d}}{1 + P_S \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}} \geq R_{\text{sec}}^0, \\
& \quad P_S \geq 0, P_J \geq 0, \text{tr}(\mathbf{p}^T \mathbf{F}_n \mathbf{p}) = 1, 0 \leq n \leq N_D - 1,
\end{aligned} \tag{24}$$

where  $\mathbf{F}_n = (\mathbf{F}_n^1)^T \mathbf{F}_n^1$  and  $\mathbf{F}_n^1 = [\mathbf{0}_{3 \times n} \ \mathbf{F} \ \mathbf{0}_{3 \times (N_D - n - 1)}]$ , in which the sparse matrix  $\mathbf{F} \in \mathbb{R}^{3 \times (2N_D + 1)}$  is defined as

$$\mathbf{F}[i, j] = \begin{cases} 1, & (i, j) \in \{(1, 1), (2, N_D + 1), (3, 2N_D + 1)\}, \\ 0, & \text{otherwise.} \end{cases} \tag{25}$$

Note that the constraint  $\text{tr}(\mathbf{p}^T \mathbf{F}_n \mathbf{p}) = 1$  in (24) is equivalent to the property of PSA spatial pointings given in (7). When  $P_S$  and  $P_J$  are given, the optimal  $\omega_d$  for the problem (24) is obtained, similar to the derivation of  $\omega_e^*$ , as

$$\omega_d^{\text{opt}} = \frac{(\sigma^2 \mathbf{I}_{N_D} + P_J |h_{JD}|^2 \mathbf{Q}_j \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H)^{-1} \mathbf{Q}_d \mathbf{p}}{\|(\sigma^2 \mathbf{I}_{N_D} + P_J |h_{JD}|^2 \mathbf{Q}_j \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H)^{-1} \mathbf{Q}_d \mathbf{p}\|}. \tag{26}$$

Next we substitute (26) into (24) to reformulate the total power minimization problem as (27), which is given at the top of this page. Unfortunately, because of the nonlinear and coupled term  $C_p$ , which is given by

$$C_p = \mathbf{p}^T \mathbf{Q}_d^H \mathbf{Q}_d \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H \mathbf{Q}_j \mathbf{p} - \mathbf{p}^T \mathbf{Q}_d^H \mathbf{Q}_j \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H \mathbf{Q}_d \mathbf{p} \geq 0, \tag{28}$$

the optimization problem (27) is generally nonconvex and difficult to solve directly. Hence we propose a suboptimal algorithm for the optimization problem (27), i.e., (24). With this method, the optimization of  $\mathbf{p}$  is performed independently from  $P_S$  and  $P_J$ . Specifically, since the received desired signal strength at destination  $D$  in the SIMO network satisfies

$$\begin{aligned}
P_S |h_{SD}|^2 |\omega_d^H \mathbf{Q}_d \mathbf{p}|^2 &\leq P_S |h_{SD}|^2 \|\omega_d\|^2 \|\mathbf{Q}_d \mathbf{p}\|^2 \\
&= P_S |h_{SD}|^2 \text{tr}(\mathbf{Q}_d^H \mathbf{Q}_d \mathbf{p} \mathbf{p}^T),
\end{aligned} \tag{29}$$

we can consider the term  $P_S |h_{SD}|^2 \text{tr}(\mathbf{Q}_d^H \mathbf{Q}_d \mathbf{P}_c)$  as the optimization objective for the PSA spatial pointings  $\mathbf{p}$  by introducing  $\mathbf{P}_c = \mathbf{p} \mathbf{p}^T$ . Thus, the secrecy optimization problem with

respect to  $\mathbf{p}$  can be formulated as

$$\begin{aligned} \max_{\mathbf{P}_c} \quad & P_S |h_{SD}|^2 \text{tr}(\mathbf{Q}_d^H \mathbf{Q}_d \mathbf{P}_c), \\ \text{s.t.} \quad & \mathbf{P}_c \succeq 0, \text{rank}(\mathbf{P}_c) = 1, \text{tr}(\mathbf{Q}_j^H \mathbf{Q}_j \mathbf{P}_c) = 0, \\ & \text{tr}(\mathbf{F}_n \mathbf{P}_c) = 1, 0 \leq n \leq N_D - 1. \end{aligned} \quad (30)$$

where the constraint  $\text{tr}(\mathbf{Q}_j^H \mathbf{Q}_j \mathbf{P}_c) = 0$  indicates that the interference introduced by jammer  $J$  to destination  $D$  can be canceled completely. However, the problem (30) is nonconvex and NP-hard due to the rank-1 constraint.

In order to find an efficient way of solving the optimization (30), we firstly relax it to a standard semidefinite programming (SDP) problem by neglecting the rank-1 constraint temporarily. Then the penalty based method [29] is utilized to obtain the finally rank-1 satisfied solution for the problem (30). To be specific, let  $\mathbf{P}_c^{\text{opt}}$  be the optimal solution of (30) without considering the rank-1 constraint. Then  $\text{tr}(\mathbf{Q}_d^H \mathbf{Q}_d \mathbf{P}_c^{\text{opt}})$  is actually an upper bound of  $\text{tr}(\mathbf{Q}_d^H \mathbf{Q}_d \mathbf{P}_c)$  in the objective function of the problem (30). With the penalty based method, this  $\mathbf{P}_c^{\text{opt}}$  is adopted as the initial point  $\mathbf{P}_c^{(0)}$  for the iterative optimization given in (31):

$$\begin{aligned} \mathbf{P}_c^{(t+1)} = \arg \min_{\mathbf{P}_c} \quad & \text{tr}(\mathbf{P}_c) - \lambda_{\max}(\mathbf{P}_c^{(t)}) \\ & - \text{tr}(\boldsymbol{\vartheta}_{\max}^{(t)} (\boldsymbol{\vartheta}_{\max}^{(t)})^H (\mathbf{P}_c - \mathbf{P}_c^{(t)})), \\ \text{s.t.} \quad & \text{tr}(\mathbf{Q}_d^H \mathbf{Q}_d \mathbf{P}_c) \leq \gamma, \mathbf{P}_c \succeq 0, \text{tr}(\mathbf{Q}_j^H \mathbf{Q}_j \mathbf{P}_c) = 0, \\ & \text{tr}(\mathbf{F}_n \mathbf{P}_c) = 1, 0 \leq n \leq N_D - 1, \end{aligned} \quad (31)$$

where the auxiliary variable  $\gamma$  satisfying  $0 \leq \gamma \leq \text{tr}(\mathbf{Q}_d^H \mathbf{Q}_d \mathbf{P}_c^{\text{opt}})$ , and the superscript  $(t)$  denotes the iteration number, while  $\lambda_{\max}(\mathbf{P}_c^{(t)})$  is the maximum eigenvalue of  $\mathbf{P}_c^{(t)}$  and  $\boldsymbol{\vartheta}_{\max}^{(t)}$  denotes the corresponding eigenvector. For a fixed  $\gamma$ , we can obtain the optimal rank-1 satisfied solution  $\mathbf{P}_c^{\text{opt}}$  by solving the optimization problem (31) iteratively, and the corresponding optimal  $\mathbf{p}^{\text{opt}}$  is calculated through the eigenvalue decomposition of  $\mathbf{P}_c^{\text{opt}}$ . We utilize the bisection method [30] to perform one-dimensional search for obtaining the optimal auxiliary variable  $\gamma^*$ , so as to obtain the optimal solution  $\mathbf{p}^*$ . The convergence of utilizing this penalty based method to solve the problem (31) is proved in Appendix.

Once the optimal  $\mathbf{p}^*$  is given, the optimal  $\boldsymbol{\omega}_d^*$  and the SINR at destination are derived respectively from (26) and (20) as

$$\boldsymbol{\omega}_d^* = \mathbf{Q}_d \mathbf{p}^* / \|\mathbf{Q}_d \mathbf{p}^*\|, \quad (32)$$

$$\text{SINR}_D = \sigma^{-2} P_S |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2. \quad (33)$$

By substituting  $\mathbf{p}^*$  and  $\boldsymbol{\omega}_d^*$  into the original problem (24), the reformulated total power minimization problem is given by

$$\begin{aligned} \min_{P_S, P_J} \quad & P_S + P_J, \\ \text{s.t.} \quad & \log_2 \left( \frac{1 + \sigma^{-2} P_S |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2}{1 + P_S \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}} \right) \geq R_{\text{sec}}^0, \\ & P_S \geq 0, P_J \geq 0. \end{aligned} \quad (34)$$

After performing some mathematical transformations, we have

$$\begin{aligned} \min_{P_S, P_J} \quad & P_S + P_J, \\ \text{s.t.} \quad & \sigma_e^2 (2^{R_{\text{sec}}^0} - 1) + (2^{R_{\text{sec}}^0} - 1) \|\mathbf{h}_{JE}\|^2 P_J \\ & + (2^{R_{\text{sec}}^0} \|\mathbf{h}_{SE}\|^2 - \sigma_e^2 \sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2) P_S \\ & + (2^{R_{\text{sec}}^0} \sigma_e^{-2} a \\ & - \sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2 \|\mathbf{h}_{JE}\|^2) P_S P_J \leq 0, \\ & P_S \geq 0, P_J \geq 0, \end{aligned} \quad (35)$$

where  $a = \|\mathbf{h}_{SE}\|^2 \|\mathbf{h}_{JE}\|^2 - |\mathbf{h}_{SE}^H \mathbf{h}_{JE}|^2$ . For effectively solving the optimization problem (35), we consider different cases of the required secrecy rate threshold  $R_{\text{sec}}^0$ , which corresponds to different optimal solutions of  $P_S + P_J$ . Firstly, two bounds of  $R_{\text{sec}}^0$  are defined as

$$R_1 = \log_2 \left( \frac{\sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2}{\sigma_e^{-2} \|\mathbf{h}_{SE}\|^2} \right), \quad (36)$$

$$R_2 = \log_2 \left( \frac{\sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2 \|\mathbf{h}_{JE}\|^2}{\sigma_e^{-2} a} \right), \quad (37)$$

Based on (36) and (37), the following three cases of  $R_{\text{sec}}^0$  are discussed.

*Case 1.  $R_1 < R_{\text{sec}}^0 < R_2$ :* In this case, the optimization problem (35) is actually a standard geometric programming (GP) problem, which is

$$\begin{aligned} \min_{P_S, P_J} \quad & P_S + P_J, \\ \text{s.t.} \quad & g_2 P_S^{-1} + g_3 P_J^{-1} + g_1 P_S^{-1} P_J^{-1} \leq 1 \\ & P_S \geq 0, P_J \geq 0. \end{aligned} \quad (38)$$

where

$$g_1 = \frac{\sigma_e^2 (2^{R_{\text{sec}}^0} - 1)}{(\sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2 \|\mathbf{h}_{JE}\|^2 - 2^{R_{\text{sec}}^0} \sigma_e^{-2} a)}, \quad (39)$$

$$g_2 = \frac{(2^{R_{\text{sec}}^0} - 1) \|\mathbf{h}_{JE}\|^2}{(\sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2 \|\mathbf{h}_{JE}\|^2 - 2^{R_{\text{sec}}^0} \sigma_e^{-2} a)}, \quad (40)$$

$$g_3 = \frac{(2^{R_{\text{sec}}^0} \|\mathbf{h}_{SE}\|^2 - \sigma_e^2 \sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2)}{(\sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2 \|\mathbf{h}_{JE}\|^2 - 2^{R_{\text{sec}}^0} \sigma_e^{-2} a)}. \quad (41)$$

Obviously, this optimization can be efficiently solved using the convex optimization technique to yield corresponding optimal total transmit power  $P_S^* + P_J^*$ .

*Case 2.  $R_{\text{sec}}^0 \leq R_1$ :* In fact, the expression  $R_1$  denotes the maximum secrecy rate of the SIMO network without introducing jammer  $J$  under a high SINR condition. If  $R_{\text{sec}}^0 \leq R_1$  is required, it makes no sense to introduce jammer  $J$  and thus  $P_J = 0$  is designed. Therefore, the optimization problem (35) is transformed into

$$\begin{aligned} \min_{P_S} \quad & P_S, \\ \text{s.t.} \quad & (2^{R_{\text{sec}}^0} \|\mathbf{h}_{SE}\|^2 - \sigma_e^2 \sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2) P_S \end{aligned}$$

$$\begin{aligned} & + \sigma_e^2 (2^{R_{\text{sec}}^0} - 1) \leq 0, \\ & P_S \geq 0, \end{aligned} \quad (42)$$

which has the optimal source transmit power  $P_S^*$  as

$$P_S^* = \frac{\sigma_e^2 (2^{R_{\text{sec}}^0} - 1)}{2^{R_{\text{sec}}^0} \|\mathbf{h}_{SE}\|^2 - \sigma_e^2 \sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2}. \quad (43)$$

In this case, the optimal total power consumption is then given by  $P_S^* + P_J^* = P_S^*$ .

*Case 3.*  $R_{\text{sec}}^0 \geq R_2$ : When jammer  $J$  is introduced to promote secure communications of the SIMO network, the maximum achievable secrecy rate is expressed as  $R_2$ . That is, if the required secrecy rate threshold  $R_{\text{sec}}^0 \geq R_2$ , the optimization problem (35) is infeasible.

In summary, by combining the optimization problems (31), (32) and (35), the total power minimization problem (24) can be solved efficiently in a suboptimal way by optimizing the PSA spatial pointings  $\mathbf{p}$ , the receive beamforming vector  $\boldsymbol{\omega}_d$  and the total transmit power  $P_S + P_J$ , separately.

### B. Secrecy Rate Maximization

We now investigate the secrecy rate maximization of the SIMO network subject to the total transmit power constraint  $P_{\text{max}}$ . Similar to the total power minimization of (24), the secrecy rate optimization problem is formulated as

$$\begin{aligned} \max_{P_S, P_J, \boldsymbol{\omega}_d, \mathbf{p}} \quad & \log_2 \frac{1 + \frac{P_S |h_{SD}|^2 |\boldsymbol{\omega}_d^H \mathbf{Q}_d \mathbf{p}|^2}{\boldsymbol{\omega}_d^H (\sigma^2 \mathbf{I}_{N_D} + P_J |h_{JD}|^2 \mathbf{Q}_j \mathbf{p} \mathbf{p}^T \mathbf{Q}_j^H) \boldsymbol{\omega}_d}}{1 + P_S \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}}, \\ \text{s.t.} \quad & \text{tr}(\mathbf{p}^T \mathbf{F}_n \mathbf{p}) = 1, 0 \leq n \leq N_D - 1, \\ & P_S + P_J \leq P_{\text{max}}, P_J \geq 0, P_S \geq 0. \end{aligned} \quad (44)$$

Likewise, the problem (44) is difficult to solve directly. Note that the secrecy rate maximization problem with the total power constraint, i.e., the problem (44), is mathematically equivalent to the total power minimization problem with the secrecy rate threshold constraint, i.e., the problem (24). Therefore, we can apply the same suboptimal approach for solving the problem (24) to solve the problem (44) by optimizing  $\mathbf{p}$ ,  $\boldsymbol{\omega}_d$  and  $(P_S, P_J)$ , separately. Specifically, the PSA spatial pointing vector  $\mathbf{p}$  is first optimized to maximize the received signal strength at destination while eliminating the interference introduced by jammer, according to (30), and the corresponding optimal  $\mathbf{p}^*$  is derived from (31). Then the optimal receive beamforming vector  $\boldsymbol{\omega}_d^*$  that maximizes the destination SINR is calculated according to (32) for the given  $\mathbf{p}^*$ . This is because at  $\mathbf{p}^*$ , we have the zero-interference from jammer, i.e.,  $\text{tr}(\mathbf{Q}_j^H \mathbf{Q}_j \mathbf{P}_c^*) = 0$ , and the optimal receive beamforming vector of (26) is reduced to (32). With  $\boldsymbol{\omega}_d$  and  $\mathbf{p}$  fixed to  $\boldsymbol{\omega}_d^*$  and  $\mathbf{p}^*$ , the optimization (44) becomes the following optimization problem

$$\begin{aligned} \max_{P_S, P_J} \quad & \log_2 \frac{1 + \sigma^{-2} P_S |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2}{1 + P_S \mathbf{h}_{SE}^H (P_J \mathbf{h}_{JE} \mathbf{h}_{JE}^H + \sigma_e^2 \mathbf{I}_{N_E})^{-1} \mathbf{h}_{SE}}, \\ \text{s.t.} \quad & P_S + P_J \leq P_{\text{max}}, P_J \geq 0, P_S \geq 0. \end{aligned} \quad (45)$$

Since the objective function of the constrained optimization (45) is monotonically increasing with  $P_J$ , it is self-evident that the

optimal solution of the constrained optimization (45) is achieved when the total power  $P_S + P_J$  reaches its maximum value, namely, when the total power constraint is active or  $P_S + P_J = P_{\text{max}}$  holds. Therefore, we can further rewrite the problem (45) as

$$\max_{0 \leq P_S \leq P_{\text{max}}} f(P_S), \quad (46)$$

where

$$f(P_S) = \frac{l_5 P_S^2 - l_4 P_S - l_1}{l_3 P_S^2 - l_2 P_S - l_1}, \quad (47)$$

and

$$\begin{cases} l_1 = \sigma_e^2 + P_{\text{max}} \|\mathbf{h}_{JE}\|^2, \\ l_2 = \|\mathbf{h}_{SE}\|^2 - \|\mathbf{h}_{JE}\|^2 + P_{\text{max}} l_3, \\ l_3 = \sigma_e^{-2} a \\ l_4 = \sigma^{-2} |h_{SD}|^2 \|\mathbf{Q}_d \mathbf{p}^*\|^2 (P_{\text{max}} |h_{JE}|^2 + \sigma_e^2) - \|\mathbf{h}_{JE}\|^2, \\ l_5 = \sigma^{-2} \|\mathbf{Q}_d \mathbf{p}^*\|^2 |h_{SD}|^2 \|\mathbf{h}_{JE}\|^2. \end{cases} \quad (48)$$

It can be seen that the optimization problem (46) is an unconstrained quadratically fractional function maximization problem, whose optimal solution  $P_S^*$  can easily be derived by the quadratic discriminant method, which is

$$P_S^* = \min \{P_{\text{max}}, P'_S\}, \quad (49)$$

with

$$P'_S = \left[ \frac{-l_1(l_3 - l_5) + \sqrt{l_1^2(l_3 - l_5)^2 - l_1(l_3 l_4 - l_5 l_2)(l_4 - l_2)}}{l_3 l_4 - l_5 l_2} \right]^+. \quad (50)$$

Once the optimal  $P_S^*$  is obtained, the optimal  $P_J^* = P_{\text{max}} - P_S^*$ . Given the optimal source and jammer transmit powers  $P_S^*$  and  $P_J^*$ , we can accordingly determine the maximum achievable secrecy rate of the SIMO network via (23). It is worth re-iterating that the 'optimal' PSA spatial pointing vector  $\mathbf{p}^*$ , the receive beamforming vector  $\boldsymbol{\omega}_d^*$ , the transmit power pairs  $P_S^*$  and  $P_J^*$  so obtained do not offer an optimal solution of the optimization problem (44). Rather they only provide a suboptimal solution.

## IV. RELAY AIDED SECURE BEAMFORMING DESIGN

We now extend the secure beamforming design to the relaying network with PSA. Specifically, two cases are considered, where the first case assumes that the perfect CSI in the relay network is available and the other one considers the imperfect PSA spatial pointings. For the both cases, we aim at improving the secrecy rate of the relaying network as much as possible.

As shown in Fig. 3, source  $S$ , destination  $D$ , eavesdropper  $E$  and jammer  $J$  are all equipped with single-antenna, while relay  $R$  employs the  $N_R$ -antenna PSA. Owing to the limit coverage of  $S$ , there exists no direct communication link between  $S$  and  $D$ . Therefore,  $S$  transmits confidential signal  $\hat{s}_d$  to  $D$  via  $R$ . Specifically, in the first phase known as multiple access (MAC) phase,  $S$  transmits  $\hat{s}_d$  to  $R$ , and then in the second phase called broadcast (BC) phase,  $R$  forwards the received signal in the first phase to  $D$ . Again, owing to the existence of eavesdropper  $E$ , jammer  $J$  is introduced to transmit jamming signal  $\hat{s}_j$  to

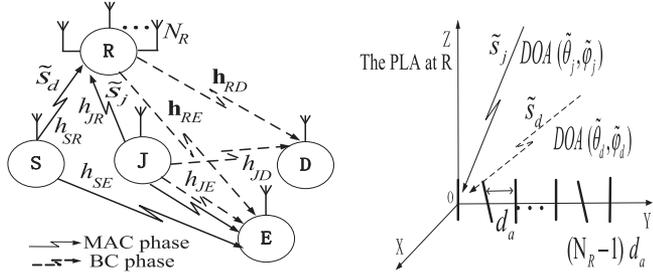


Fig. 3. A two-hop network with the polarization sensitive array having  $N_R$  antennas at relay.

decrease the information leakage which happens between  $S$  and  $R$  as well as between  $R$  and  $D$ . The transmissions of source  $S$  and jammer  $J$  in the MAC phase are synchronized, while the transmissions of relay  $R$  and jammer  $J$  in the BC phase are also synchronized. For this relay network, it is reasonable to assume that source transmits signal using maximum transmit power.

#### A. Secrecy Rate Maximization with Perfect CSI

Similar to Section III, the scalar  $h_{mn} \sim \mathcal{CN}(0, \sigma_h^2)$  denotes the flat-fading and quasi-static channel from node  $m$  to node  $n$  where  $m = S, J$  and  $n = E$ , while  $h_{SR}$  and  $h_{JR}$  denote the channel gains from source  $S$  and jammer  $J$  to the reference antenna of the relay's PSA, respectively. Furthermore, the CSI of eavesdropper  $E$  is assumed to be available. Based on these assumptions, the received signals at the  $N_R$  antennas of relay  $R$  in the MAC phase can be expressed as

$$\mathbf{y}_R = \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}} h_{SR} \sqrt{P_S} \tilde{s}_d + \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}} h_{JR} \sqrt{P_J^{(1)}} \tilde{s}_j + \mathbf{n}_R, \quad (51)$$

where  $\tilde{s}_d$  and  $\tilde{s}_j$  are the transmit signals of source  $S$  and jammer  $J$ , respectively, with  $\mathbf{E}\{\|\tilde{s}_d\|^2\} = \mathbf{E}\{\|\tilde{s}_j\|^2\} = 1$ ,  $P_S$  and  $P_J^{(1)}$  are the transmit powers of source  $S$  and jammer  $J$ , respectively, while  $\mathbf{n}_R \in \mathbb{C}^{N_R}$  is the Gaussian noise vector at relay  $R$  whose elements follow the distribution  $\mathcal{CN}(0, \sigma_r^2)$ . The spatio-polarized manifold matrices  $\tilde{\mathbf{Q}}_k \in \mathbb{C}^{N_R \times 3N_R}$  for  $k = d, j$  are defined similarly to (13), and the relay's PSA spatial pointing vector  $\tilde{\mathbf{p}} \in \mathbb{R}^{3N_R}$  is defined similarly to (12). The wiretapped signal at  $E$  in this phase is given by

$$\begin{aligned} \mathbf{y}_E^{(1)} &= h_{SE} \sqrt{P_S} \tilde{s}_d + h_{JE} \sqrt{P_J^{(1)}} \tilde{s}_j + n_E^{(1)} \\ &= h_{SE} \sqrt{P_S} \tilde{s}_d + \hat{n}_E^{(1)}, \end{aligned} \quad (52)$$

where the additive Gaussian noise  $n_E^{(1)}$  follows the distribution  $\mathcal{CN}(0, \sigma_e^2)$ , and  $\hat{n}_E^{(1)} = h_{JE} \sqrt{P_J^{(1)}} \tilde{s}_j + n_E^{(1)}$ .

In the BC phase, relay  $R$  utilizes the amplify-and-forward (AF) strategy to forward the received signal  $\mathbf{y}_R$ . To be specific, the retransmitted signal is  $\mathbf{y}'_R = \mathbf{W} \mathbf{y}_R$ , where  $\mathbf{W} \in \mathbb{C}^{N_R \times N_R}$  denotes the AF beamforming matrix. Thus, the transmit power of  $R$  is given by

$$\begin{aligned} P_R &= P_S |h_{SR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}\|^2 + P_J^{(1)} |h_{JR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}\|^2 \\ &\quad + \sigma^2 \text{tr}(\mathbf{W} \mathbf{W}^H). \end{aligned} \quad (53)$$

Simultaneously, jammer  $J$  sends the interference signal  $\tilde{s}_j^{(2)}$  with power  $P_J^{(2)}$  to  $D$ . Let  $\mathbf{h}_{RD} \in \mathbb{C}^{1 \times N_R}$  and  $\mathbf{h}_{RE} \in \mathbb{C}^{1 \times N_R}$  be the channel gain vectors from the  $N_R$  antennas of relay  $R$  to destination  $D$  and eavesdropper  $E$ , respectively, while  $h_{JD}$  denotes the channel gain from  $J$  to  $D$ . Then the received signals at  $D$  and  $E$  are formulated respectively as

$$\begin{aligned} y_D &= \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{y}'_R + \sqrt{P_J^{(2)}} h_{JD} \tilde{s}_j^{(2)} + n_D \\ &= \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}} h_{SR} \sqrt{P_S} \tilde{s}_d + \hat{n}_D, \end{aligned} \quad (54)$$

$$\begin{aligned} y_E^{(2)} &= \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{y}'_R + \sqrt{P_J^{(2)}} h_{JE} \tilde{s}_j^{(2)} + n_E^{(2)} \\ &= \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}} h_{SR} \sqrt{P_S} \tilde{s}_d + \hat{n}_E^{(2)}. \end{aligned} \quad (55)$$

Due to the fact that relay  $R$  adopts the PSA as the transmit array, its antenna correlation matrix  $\mathbf{R}_{\text{cor}} \in \mathbb{C}^{N_R \times N_R}$  must be considered, whose elements follow the exponential model of  $\mathbf{R}_{\text{cor}}[n, m] = p^{|n-m|}$  for  $1 \leq n, m \leq N_R$  with constant  $p$  [31]. The additive Gaussian noises at destination  $D$  and eavesdropper  $E$  are  $n_D \sim \mathcal{CN}(0, \sigma_d^2)$  and  $n_E^{(2)} \sim \mathcal{CN}(0, \sigma_e^2)$ , respectively, while the equivalent noise-plus-interference terms  $\hat{n}_D$  and  $\hat{n}_E^{(2)}$  are given by

$$\begin{aligned} \hat{n}_D &= \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}} h_{JR} \sqrt{P_J^{(1)}} \tilde{s}_j + \sqrt{P_J^{(2)}} h_{JD} \tilde{s}_j^{(2)} \\ &\quad + \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \mathbf{n}_R + n_D, \end{aligned} \quad (56)$$

$$\begin{aligned} \hat{n}_E^{(2)} &= \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}} h_{JR} \sqrt{P_J^{(1)}} \tilde{s}_j + \sqrt{P_J^{(2)}} h_{JE} \tilde{s}_j^{(2)} \\ &\quad + \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \mathbf{n}_R + n_E^{(2)}. \end{aligned} \quad (57)$$

Clearly, the total amount of information leakage to  $E$  comes from both  $S$  and  $R$ , as indicated in (52) and (55). Hence, the wiretapped information in the relay network is given by

$$\begin{aligned} \mathbf{y}_E &= \begin{bmatrix} h_{SE} \\ \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}} h_{SR} \end{bmatrix} \sqrt{P_S} \tilde{s}_d + \begin{bmatrix} \hat{n}_E^{(1)} \\ \hat{n}_E^{(2)} \end{bmatrix} \\ &= \mathbf{H}_E \sqrt{P_S} \tilde{s}_d + \hat{\mathbf{n}}_E. \end{aligned} \quad (58)$$

The covariance matrix  $\mathbf{O}_E$  of  $\hat{\mathbf{n}}_E$  and  $\mathbf{O}_D = \mathbf{E}\{\|\hat{n}_D\|^2\}$  are given by (59) and (60), respectively, at the top of the next page, in which  $K_e = P_J^{(2)} |h_{JE}|^2 + \sigma_r^2 \|\mathbf{h}_{RE}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}\|^2 + \sigma_d^2$ . Correspondingly, the achievable secrecy rate region of this relaying network is

$$\tilde{R}_{\text{sec}} \leq [\tilde{I}(y_D, \tilde{s}_d) - \tilde{I}(y_E, \tilde{s}_d)]^+, \quad (61)$$

in which the mutual information between source  $S$  and destination  $D$  and the mutual information between source  $S$  and eavesdropper  $E$  are given respectively by

$$\tilde{I}(y_D, \tilde{s}_d) = \log_2(1 + P_S |h_{SR}|^2 |\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}|^2 / \mathbf{O}_D), \quad (62)$$

$$\tilde{I}(y_E, \tilde{s}_d) = \log_2 \det(\mathbf{I}_2 + P_S \mathbf{H}_E \mathbf{H}_E^H \mathbf{O}_E^{-1}). \quad (63)$$

$$\mathbf{O}_E = \begin{bmatrix} \sigma_e^2 + P_J^{(1)} |h_{JE}|^2 & P_J^{(1)} h_{JE} h_{JR}^* (\mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}})^* \\ P_J^{(1)} (\mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}) h_{JR} h_{JE}^* & P_J^{(1)} |h_{JR}|^2 |\mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}|^2 + K_e \end{bmatrix}, \quad (59)$$

$$O_D = P_J^{(1)} |h_{JR}|^2 |\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}|^2 + P_J^{(2)} |h_{JD}|^2 + \sigma_r^2 \|\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}\|^2 + \sigma_d^2, \quad (60)$$

The optimization problem for the proposed secure beamforming design is formulated as

$$\begin{aligned} \max_{P_J^{(1)}, P_J^{(2)}, \mathbf{W}, \tilde{\mathbf{p}}} \quad & \log_2 \frac{1 + \frac{P_S |h_{SD}|^2 |\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}|^2}{O_D}}{\det(\mathbf{I}_2 + P_S \mathbf{H}_E \mathbf{H}_E^H \mathbf{O}_E^{-1})}, \\ \text{s.t.} \quad & \text{tr}(\tilde{\mathbf{p}}^T \tilde{\mathbf{F}}_n \tilde{\mathbf{p}}) = 1, \quad 0 \leq n \leq N_R - 1, \\ & P_S |h_{SR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}\|^2 + P_J^{(1)} |h_{JR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}\|^2 \\ & + \sigma_r^2 \text{tr}(\mathbf{W} \mathbf{W}^H) \leq P_R^{\text{max}}, \\ & 0 \leq P_J^{(1)} + P_J^{(2)} \leq P_J^{\text{max}}, \end{aligned} \quad (64)$$

where the definition of  $\tilde{\mathbf{F}}_n \in \mathbb{R}^{3N_R \times 3N_R}$  is similar to that of  $\mathbf{F}_n$  given in Section III-A, while  $P_R^{\text{max}}$  and  $P_J^{\text{max}}$  are the maximum relay and jammer transmit powers, respectively. It can be observed that the objective function of this problem is a product of two correlated generalized Rayleigh quotients and is obviously nonconvex. Thus this optimization is difficult to solve directly. Since eavesdropper  $E$  is a legitimate although not an intended receiver, we assume that the perfect CSI of  $E$  is available. Then the following operations are performed.

1) As the perfect CSI of  $E$  is available, the beamforming matrix  $\mathbf{W}$  is designed to satisfy  $\mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}} = 0$ . Thus the information leakage from  $R$  to  $E$  is canceled completely. With this beamforming matrix design, jammer  $J$  does not need to transmit signal  $\tilde{s}_j^{(2)}$  to decrease the information leakage caused by  $R$ , which means that  $P_J^{(2)} = 0$ .

2) As destination  $D$  is disturbed by the forwarded jammer signal  $\tilde{s}_j$  from the MAC phase, the beamforming matrix  $\mathbf{W}$  should be designed to satisfy  $\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}} = 0$  to eliminate the interference to  $D$  caused by jammer  $J$  completely.

3) Since only jammer signal  $\tilde{s}_j$  is utilized to decrease the information leakage to  $E$  in the MAC phase and  $P_J^{(2)} = 0$ , we can set  $P_J^{(1)} = P_J^{\text{max}}$  to interfere eavesdropper maximally. Thus the power allocation for jammer  $J$  is determined.

With the operations 1) to 3), the information leakage only occurs in the MAC phase, and the mutual information  $\tilde{I}(y_D, \tilde{s}_d)$  and  $\tilde{I}(y_E, \tilde{s}_d)$  are simplified as

$$\tilde{I}(y_D, \tilde{s}_d) = \log_2(1 + P_S |h_{SR}|^2 |\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}|^2 / O_D), \quad (65)$$

$$\tilde{I}(y_E, \tilde{s}_d) = \log_2 \left( 1 + \frac{P_S |h_{SE}|^2}{\sigma_e^2 + P_J^{\text{max}} |h_{JE}|^2} \right). \quad (66)$$

Thus the secrecy rate maximization problem (64) can be re-expressed as

$$\begin{aligned} \max_{\mathbf{W}, \tilde{\mathbf{p}}} \quad & \log_2 \frac{1 + \frac{P_S |h_{SR}|^2 |\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}|^2}{\sigma_d^2 + \sigma_r^2 \|\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}\|^2}}{1 + \frac{P_S |h_{SE}|^2}{\sigma_e^2 + P_J^{\text{max}} |h_{JE}|^2}}, \\ \text{s.t.} \quad & \text{tr}(\tilde{\mathbf{p}}^T \tilde{\mathbf{F}}_n \tilde{\mathbf{p}}) = 1, \quad 0 \leq n \leq N_R - 1, \\ & \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}} = 0, \quad \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}} = 0, \\ & P_S |h_{SR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}\|^2 + P_J^{\text{max}} |h_{JR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}\|^2 \\ & + \sigma_r^2 \text{tr}(\mathbf{W} \mathbf{W}^H) \leq P_R^{\text{max}}. \end{aligned} \quad (67)$$

Unfortunately, this problem is still neither convex nor concave with respect to  $\mathbf{W}$  and  $\tilde{\mathbf{p}}$ . Similar to solving (24), we propose an iterative suboptimal algorithm to solve (67) effectively.

1) *Optimization of  $\mathbf{W}$* : When the PSA spatial pointing vector is fixed to  $\tilde{\mathbf{p}} = \tilde{\mathbf{p}}^{(l-1)}$  where  $l$  is the outer iteration index and  $\text{tr}(\tilde{\mathbf{p}}^{(l-1)T} \tilde{\mathbf{F}}_n \tilde{\mathbf{p}}^{(l-1)}) = 1$  for  $0 \leq n \leq N_R - 1$ , the problem (67) is transformed into

$$\begin{aligned} \max_{\mathbf{W}} \quad & 1 + \frac{P_S |h_{SR}|^2 |\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}^{(l-1)}|^2}{\sigma_d^2 + \sigma_r^2 \|\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}\|^2}, \\ \text{s.t.} \quad & \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}^{(l-1)} = 0, \\ & \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}^{(l-1)} = 0, \\ & P_S |h_{SR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}^{(l-1)}\|^2 + P_J^{\text{max}} |h_{JR}|^2 \|\mathbf{W} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}^{(l-1)}\|^2 \\ & + \sigma_r^2 \text{tr}(\mathbf{W} \mathbf{W}^H) \leq P_R^{\text{max}}. \end{aligned} \quad (68)$$

After some manipulations, (68) can be rewritten as

$$\begin{aligned} \max_{\boldsymbol{\omega}_R} \quad & 1 + \frac{P_S |h_{SR}|^2 \boldsymbol{\omega}_R^H \mathbf{G}_d^{(l-1)} \boldsymbol{\omega}_R}{\sigma_d^2 + \sigma_r^2 \boldsymbol{\omega}_R^H \mathbf{G}_b \boldsymbol{\omega}_R}, \\ \text{s.t.} \quad & (\mathbf{g}_j^{(l-1)})^H \boldsymbol{\omega}_R = 0, \quad (\mathbf{g}_e^{(l-1)})^H \boldsymbol{\omega}_R = 0, \\ & \boldsymbol{\omega}_R^H (P_S |h_{SR}|^2 \mathbf{R}_d^{(l-1)} + P_J^{\text{max}} |h_{JR}|^2 \mathbf{R}_j^{(l-1)} \\ & + \sigma_r^2 \mathbf{I}_{N_R^2}) \boldsymbol{\omega}_R \leq P_R^{\text{max}}, \end{aligned} \quad (69)$$

where

$$\boldsymbol{\omega}_R = \text{vec}(\mathbf{W}) \in \mathbb{C}^{N_R^2}, \quad (70)$$

$$\mathbf{g}_k^{(l-1)} = (\tilde{\mathbf{Q}}_k \tilde{\mathbf{p}}^{(l-1)})^* \otimes (\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}})^H \in \mathbb{C}^{N_R^2}, \quad k = d, j, \quad (71)$$

$$\mathbf{g}_e^{(l-1)} = (\tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}^{(l-1)})^* \otimes (\mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}})^H \in \mathbb{C}^{N_R^2}, \quad (72)$$

$$\boldsymbol{\mu} = \left( (\mathbf{G}_{j_e}^{(l-1)\perp})^H (P_R^{\max} \mathbf{G}_b + P_S |h_{SR}|^2 \mathbf{R}_d^{(l-1)} + P_J^{\max} |h_{JR}|^2 \mathbf{R}_j^{(l-1)} + \sigma_r^2 \mathbf{I}_{N_R^2}) \mathbf{G}_{j_e}^{(l-1)\perp} \right)^{-1} (\mathbf{G}_{j_e}^{(l-1)\perp})^H \mathbf{g}_d^{(l-1)}, \quad (78)$$

$$c(\tilde{\mathbf{p}}^{(l-1)}) = \sqrt{P_R^{\max} / \left( \boldsymbol{\mu}^H (\mathbf{G}_{j_e}^{(l-1)\perp})^H (P_S |h_{SR}|^2 \mathbf{R}_d^{(l-1)} + P_J^{\max} |h_{JR}|^2 \mathbf{R}_j^{(l-1)} + \sigma_r^2 \mathbf{I}_{N_R^2}) \mathbf{G}_{j_e}^{(l-1)\perp} \boldsymbol{\mu} \right)}. \quad (79)$$

$$\mathbf{G}_d^{(l-1)} = \mathbf{g}_d^{(l-1)} (\mathbf{g}_d^{(l-1)})^H, \quad (73)$$

$$\mathbf{G}_b = (\mathbf{I}_{N_R} \otimes (\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}})^H) (\mathbf{I}_{N_R} \otimes (\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}})), \quad (74)$$

$$\mathbf{R}_k^{(l-1)} = ((\tilde{\mathbf{Q}}_k \tilde{\mathbf{p}}^{(l-1)})^* \otimes \mathbf{I}_{N_R}) ((\tilde{\mathbf{Q}}_k \tilde{\mathbf{p}}^{(l-1)})^T \otimes \mathbf{I}_{N_R}), \quad (75)$$

$$k = d, j.$$

Let  $\mathbf{G}_{j_e}^{(l-1)\perp}$  be the projection matrix onto the null space of  $\mathbf{G}_{j_e}^{(l-1)} = [\mathbf{g}_j^{(l-1)} \ \mathbf{g}_e^{(l-1)}]^H$ . Then the  $N_R^2$ -dimensional relay beamforming vector is denoted as  $\boldsymbol{\omega}_R = \mathbf{G}_{j_e}^{(l-1)\perp} \tilde{\boldsymbol{\omega}}_R$ , which transforms the original optimization variable  $\boldsymbol{\omega}_R$  into  $\tilde{\boldsymbol{\omega}}_R$ . Thus, the problem (69) can be rewritten as

$$\begin{aligned} \max_{\tilde{\boldsymbol{\omega}}_R} \quad & 1 + \frac{P_S |h_{SR}|^2 \tilde{\boldsymbol{\omega}}_R^H (\mathbf{G}_{j_e}^{(l-1)\perp})^H \mathbf{G}_d^{(l-1)} \mathbf{G}_{j_e}^{(l-1)\perp} \tilde{\boldsymbol{\omega}}_R}{\sigma_d^2 + \sigma_r^2 \tilde{\boldsymbol{\omega}}_R^H (\mathbf{G}_{j_e}^{(l-1)\perp})^H \mathbf{G}_b \mathbf{G}_{j_e}^{(l-1)\perp} \tilde{\boldsymbol{\omega}}_R}, \\ \text{s.t.} \quad & \tilde{\boldsymbol{\omega}}_R^H (\mathbf{G}_{j_e}^{(l-1)\perp})^H (P_S |h_{SR}|^2 \mathbf{R}_d^{(l-1)} \\ & + P_J^{\max} |h_{JR}|^2 \mathbf{R}_j^{(l-1)} + \sigma_r^2 \mathbf{I}_{N_R^2}) \mathbf{G}_{j_e}^{(l-1)\perp} \tilde{\boldsymbol{\omega}}_R \leq P_R^{\max}. \end{aligned} \quad (76)$$

The problem in (76) is also a generalized Rayleigh quotient problem, which has the closed-form solution

$$\tilde{\boldsymbol{\omega}}_R^{(l)} = c(\tilde{\mathbf{p}}^{(l-1)}) \boldsymbol{\mu}, \quad (77)$$

with  $\boldsymbol{\mu}$  and  $c(\tilde{\mathbf{p}}^{(l-1)})$  given by (78) and (79), respectively, at the top of this page. Once the optimal  $\tilde{\boldsymbol{\omega}}_R^{(l)}$  is obtained, the optimal  $\mathbf{W}^{(l)}$  can be derived based on  $\boldsymbol{\omega}_R^{(l)} = \mathbf{G}_{j_e}^{(l-1)\perp} \tilde{\boldsymbol{\omega}}_R^{(l)}$ .

$$\begin{aligned} \max_{\tilde{\mathbf{p}}} \quad & 1 + \frac{P_S |h_{SR}|^2 \tilde{\mathbf{p}}^H \tilde{\mathbf{Q}}_d^H (\mathbf{W}^{(l)})^H (\mathbf{R}_{\text{cor}}^{\frac{1}{2}})^H \mathbf{h}_{RD}^H \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}^{(l)} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}}{\sigma_d^2 + \sigma_r^2 \|\mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}^{(l)}\|^2}, \\ \text{s.t.} \quad & \text{tr}(\tilde{\mathbf{p}}^T \tilde{\mathbf{F}}_n \tilde{\mathbf{p}}) = 1, \ 0 \leq n \leq N_R - 1, \\ & \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}^{(l)} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}} = 0, \ \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}^{(l)} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}} = 0, \\ & P_S |h_{SR}|^2 \|\mathbf{W}^{(l)} \tilde{\mathbf{Q}}_d \tilde{\mathbf{p}}\|^2 + P_J^{\max} |h_{JR}|^2 \|\mathbf{W}^{(l)} \tilde{\mathbf{Q}}_j \tilde{\mathbf{p}}\|^2 \\ & + \sigma_r^2 \text{tr}(\mathbf{W}^{(l)} (\mathbf{W}^{(l)})^H) \leq P_R^{\max}. \end{aligned} \quad (80)$$

2) *Optimization of  $\tilde{\mathbf{p}}$* : Given  $\mathbf{W}^{(l)}$ , the optimization problem (67) is rewritten as

To simplify this complicated nonconvex problem, we define

$$\mathbf{P}_{j_e}^{(l)} = \begin{bmatrix} \mathbf{h}_{RD} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}^{(l)} \tilde{\mathbf{Q}}_j \\ \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}^{(l)} \tilde{\mathbf{Q}}_d \end{bmatrix} \in \mathbb{C}^{2 \times 3N_R}. \quad (81)$$

Then the feasible  $\tilde{\mathbf{p}}$  must be in the null-space of  $\mathbf{P}_{j_e}^{(l)}$ . Therefore,  $\tilde{\mathbf{p}} = \mathbf{P}_{j_e}^{(l)\perp} \hat{\tilde{\mathbf{p}}}$ , where  $\mathbf{P}_{j_e}^{(l)\perp}$  denotes the projection matrix onto the null space of  $\mathbf{P}_{j_e}^{(l)}$  and  $\hat{\tilde{\mathbf{p}}}$  is the equivalent variable vector to be optimized. By defining the Hermitian matrix  $\tilde{\mathbf{P}}_c = \hat{\tilde{\mathbf{p}}} \hat{\tilde{\mathbf{p}}}^H$ , the problem (80) is rewritten as

$$\begin{aligned} \max_{\tilde{\mathbf{P}}_c} \quad & P_S |h_{SD}|^2 \text{tr}(\tilde{\mathbf{R}}_d^{(l)} \tilde{\mathbf{P}}_c), \\ \text{s.t.} \quad & \text{tr}(\tilde{\mathbf{F}}_n^{(l)} \tilde{\mathbf{P}}_c) = 1, \ 0 \leq n \leq N_R - 1, \\ & \tilde{\mathbf{P}}_c \succeq \mathbf{0}, \ \text{rank}(\tilde{\mathbf{P}}_c) = 1, \\ & \text{tr} \left( (P_S |h_{SR}|^2 \tilde{\mathbf{G}}_d^{(l)} + P_J^{\max} |h_{JR}|^2 \tilde{\mathbf{G}}_j^{(l)}) \tilde{\mathbf{P}}_c \right) \\ & \leq P_R^{\max} - \sigma_r^2 \text{tr}(\mathbf{W}^{(l)} \mathbf{W}^{(l)H}), \end{aligned} \quad (82)$$

where

$$\begin{aligned} \tilde{\mathbf{R}}_d^{(l)} &= (\mathbf{P}_{j_e}^{(l)\perp})^H \tilde{\mathbf{Q}}_d^H (\mathbf{W}^{(l)})^H (\mathbf{R}_{\text{cor}}^{\frac{1}{2}})^H \mathbf{h}_{RD}^H \mathbf{h}_{RD} \\ &\times \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}^{(l)} \tilde{\mathbf{Q}}_d \mathbf{P}_{j_e}^{(l)\perp}, \end{aligned} \quad (83)$$

$$\tilde{\mathbf{F}}_n = (\mathbf{P}_{j_e}^{(l)\perp})^H \tilde{\mathbf{F}}_n \mathbf{P}_{j_e}^{(l)\perp}, \quad (84)$$

$$\tilde{\mathbf{G}}_k^{(l)} = (\mathbf{P}_{j_e}^{(l)\perp})^H \tilde{\mathbf{Q}}_k^H (\mathbf{W}^{(l)})^H \mathbf{W}^{(l)} \tilde{\mathbf{Q}}_k \mathbf{P}_{j_e}^{(l)\perp}, \ k = d, j. \quad (85)$$

It is observed that the problem (82) becomes a standard SDP problem if the rank-1 constraint is not considered. Similar to solving (30), we utilize the penalty based method to solve (82). The corresponding iterative optimization problem (86) is given at the top of the next page, where the superscript  $^{[t]}$  denotes the inner iteration index, and  $\tilde{\mathbf{v}}_{\max}^{[t]}$  is the eigenvector corresponding to the maximum eigenvalue  $\lambda_{\max}(\tilde{\mathbf{P}}_c^{[t]})$ . Note that the initial  $\tilde{\mathbf{P}}_c^{[0]}$  and the upper bound  $\tilde{\gamma}_{\text{up}} = \text{tr}(\tilde{\mathbf{R}}_d^{(l)} \tilde{\mathbf{P}}_c^{[0]})$  are derived from the problem (82) without considering the rank-1 constraint. Furthermore, the penalty based method and the bisection method are jointly applied to iteratively solve (86) to obtain the optimal rank-1 satisfied  $\tilde{\mathbf{P}}_c$ . This procedure is terminated when  $\text{tr}(\tilde{\mathbf{P}}_c^{[t+1]}) - \lambda_{\max}(\tilde{\mathbf{P}}_c^{[t+1]}) \approx 0$ . With the optimal solution  $\tilde{\mathbf{P}}_c^{(l)} = \tilde{\mathbf{P}}_c^{[t+1]}$ , the optimal  $\tilde{\mathbf{p}}^{(l)}$  can be obtained by the eigenvalue decomposition on  $\tilde{\mathbf{P}}_c^{(l)}$ . Since the iterative optimization (86) has exactly the same form as the iterative optimization (31), the convergence of the iterative algorithm for solving (86) is guaranteed.

Thus, instead of jointly optimizing  $\tilde{\mathbf{p}}$  and  $\mathbf{W}$ , we optimize  $\mathbf{W}$  and  $\tilde{\mathbf{p}}$  separately in an iterative procedure involving steps 1) and 2). Specifically, with the initial iteration index  $l = 1$  and

$$\begin{aligned}
\tilde{\mathbf{P}}_c^{[t+1]} &= \arg \min_{\tilde{\mathbf{P}}_c} \text{tr}(\tilde{\mathbf{P}}_c) - \lambda_{\max}(\tilde{\mathbf{P}}_c^{[t]}) - \text{tr}\left(\tilde{\mathbf{v}}_{\max}^{[t]} (\tilde{\mathbf{v}}_{\max}^{[t]})^H (\tilde{\mathbf{P}}_c - \tilde{\mathbf{P}}_c^{[t]})\right) - \text{tr}(\tilde{\mathbf{R}}_d^{(l)} \tilde{\mathbf{P}}_c), \\
\text{s.t. } \text{tr}(\tilde{\mathbf{R}}_d^{(l)} \tilde{\mathbf{P}}_c) &\leq \tilde{\gamma}, \text{tr}\left((P_S |h_{SR}|^2 \tilde{\mathbf{G}}_d^{(l)} + P_J^{\max} |h_{JR}|^2 \tilde{\mathbf{G}}_j^{(l)}) \tilde{\mathbf{P}}_c\right) \leq P_R^{\max} - \sigma_r^2 \text{tr}(\mathbf{W}^{(l)} (\mathbf{W}^{(l)})^H), \\
\tilde{\mathbf{P}}_c &\succeq \mathbf{0}, \text{tr}(\tilde{\mathbf{F}}_n^{(l)} \tilde{\mathbf{P}}_c) = 1, 0 \leq n \leq N_D - 1,
\end{aligned} \tag{86}$$

$$\begin{aligned}
\max_{\mathbf{W}_{\text{rb}}} \min_{\Delta \tilde{\mathbf{p}}} \log_2 &\left(1 + \frac{P_S |h_{SR}|^2 |\mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})|^2}{P_J^{(1)} |h_{JR}|^2 |\mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_j (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})|^2 + P_J^{(2)} |h_{JD}|^2 + \sigma_r^2 \|\mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}}\|^2 + \sigma_d^2}\right) \\
&- \log_2 \det(\mathbf{I}_2 + P_S \mathbf{H}_E \mathbf{H}_E^H \mathbf{O}_E^{-1}), \\
\text{s.t. } P_S |h_{SR}|^2 \|\mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})\|^2 &+ P_J^{(1)} |h_{JR}|^2 \|\mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_j (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})\|^2 + \sigma_r^2 \text{tr}(\mathbf{W}_{\text{rb}} \mathbf{W}_{\text{rb}}^H) \leq P_R^{\max}, 0 \leq P_J^{(1)} + P_J^{(2)} \leq P_J^{\max}.
\end{aligned} \tag{90}$$

a feasible initial  $\tilde{\mathbf{p}}^{(l-1)}$ , we obtain the optimal beamforming matrix  $\mathbf{W}^{(l)}$  using the closed-form solution (77). Then with  $\mathbf{W}^{(l)}$ , the optimal PSA pointing vector  $\tilde{\mathbf{p}}^{(l)}$  is determined by solving (86) iteratively. Because the pair  $(\mathbf{W}^{(l)}, \tilde{\mathbf{p}}^{(l)})$  is feasible in next iteration to obtain  $(\mathbf{W}^{(l+1)}, \tilde{\mathbf{p}}^{(l+1)})$ , the objective function in the original problem (67) is monotonously increasing and it converges to the maximum value as the iteration index increases. Hence, when a preset termination criterion is met, the procedure yields the optimal beamforming matrix  $\mathbf{W}^*$  and the optimal PSA pointing  $\tilde{\mathbf{p}}^*$ .

The complexity of this proposed algorithm mainly comes from the iterative SDP optimization (86) for deriving the PSA spatial pointing vector. According to [32], the computational complexity of a standard SDP problem is on the order of

$$C_{\text{SDP}} = \mathcal{O}\left(\left(M_{sdp} N_{sdp}^{3.5} + M_{sdp}^2 N_{sdp}^{2.5} + M_{sdp}^3 N_{sdp}^{0.5}\right) \log\left(\frac{1}{\epsilon}\right)\right), \tag{87}$$

where  $M_{sdp}$  is the number of semidefinite cone constraints and  $N_{sdp}$  is the dimension of the semidefinite cone, while  $\epsilon$  is the accuracy imposed to solve the SDP problem. Thus the per-iteration complexity of our proposed algorithm is

$$C_{\text{per-ite}}^{\text{perf}} = \mathcal{O}\left(\left((3N_R)^{3.5} + (3N_R)^{2.5} + (3N_R)^{0.5}\right) \log\left(\frac{1}{\epsilon}\right)\right). \tag{88}$$

### B. Robust Design for Maximizing Secrecy Rate

In the previous subsection, we obtain the optimal PSA pointing  $\tilde{\mathbf{p}}^*$ . In most practical deployments, however, the actual array spatial pointing implemented will deviate from this ideal one, due to the antenna distortion, operational environment factors or installation errors. Therefore, it is necessary to design a robust beamforming under an imperfect PSA pointing realization  $\tilde{\mathbf{p}}_{\text{act}}$ . There exist two types of array pointing errors. One is modeled as a deterministic matrix with bounded norm, and the other is unbounded and denoted by a statistical model of unknown parameters. For simplicity, we only consider the design of robust

relay beamforming  $\mathbf{W}_{\text{rb}}$  for the bounded PSA pointing error type. Specifically, an ellipsoid model is utilized to model the PSA spatial pointing error as

$$\tilde{\mathbf{p}}_{\text{act}} = \tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}}, \Delta \tilde{\mathbf{p}} \in \mathcal{P} = \{\Delta \tilde{\mathbf{p}} : \Delta \tilde{\mathbf{p}}^H \mathbf{C} \Delta \tilde{\mathbf{p}} \leq 1\}, \tag{89}$$

where  $\tilde{\mathbf{p}}^*$  is the optimal PSA pointing for the relaying network obtained in Subsection IV-A,  $\Delta \tilde{\mathbf{p}}$  is the elliptical array pointing error, and the matrix  $\mathbf{C} \succ 0$  determines the accuracy degree of the PSA pointing, which has the Cholesky decomposition of  $\mathbf{C} = \mathbf{C}^{\frac{1}{2}} (\mathbf{C}^{\frac{1}{2}})^H$ . If the elements of  $\mathbf{C}$  tend to infinity, the PSA pointing error approaches zero, i.e., the actual array structure is perfect. On the other hand, if the elements of  $\mathbf{C}$  approach 0, the PSA pointing is extremely inaccurate.

By considering the array pointing error, the resulting robust secrecy rate maximization problem (90) is formulated at the top of this page. This optimization is highly complicated, and we make some operational assumptions in order to simplify it. First, the robust beamforming matrix  $\mathbf{W}_{\text{rb}}$  is designed to satisfy  $\mathbf{h}_{RE}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d = \mathbf{0}$  to cancel the information leakage from  $R$  to  $E$  completely. Second,  $P_J^{(1)} = P_J^{\max}$  and  $P_J^{(2)} = 0$  are also applied to the robust beamforming optimization with the same reasons as given in Subsection IV-A. Under these conditions, (90) can be reformulated as the optimization problem (91) given at the top of the next page, where

$$\hat{\mathbf{R}}_k = (\mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_k)^H \mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_k, k = d, j, \tag{92}$$

and the lower bound of  $\tilde{\gamma}$  is zero, while the upper bound of  $\tilde{\gamma}$  is calculated based on the optimal  $\tilde{\mathbf{p}}^*$  and  $\mathbf{W}^*$  from the perfect CSI case. The first two constraints in the optimization problem (91) can be expressed as (93) and (94), respectively, given at the top of the next page, where

$$a = 2^{\tilde{\gamma}} (1 + P_S |h_{SE}|^2 / (\sigma_e^2 + P_J^{\max} |h_{JE}|^2)) - 1. \tag{95}$$

To promote the standard SDP formulation for the robust secrecy beamforming design, we employ the S-procedure lemma [33] to transform (93) and (94) into the linear matrix inequalities and, consequently, the optimization problem (91) is reformu-

$$\begin{aligned} & \max_{\mathbf{W}_{\text{rb}}} \bar{\gamma}, \\ \text{s.t.} & \frac{P_S |h_{SR}|^2 (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})^H \hat{\mathbf{R}}_d (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})}{P_J^{\max} |h_{JR}|^2 (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})^H \hat{\mathbf{R}}_j (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}}) + \sigma_r^2 \|\mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}}\|^2 + \sigma_d^2} \geq 2^{\bar{\gamma}} \left( 1 + \frac{P_S |h_{SE}|^2}{\sigma_e^2 + P_J^{\max} |h_{JE}|^2} \right) - 1, \forall \Delta \tilde{\mathbf{p}}, \\ & P_S |h_{SR}|^2 \|\mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})\|^2 + \sigma_r^2 \text{tr}(\mathbf{W}_{\text{rb}} \mathbf{W}_{\text{rb}}^H) \leq P_R^{\max} - P_J^{\max} |h_{JR}|^2 \|\mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_j (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})\|^2, \forall \Delta \tilde{\mathbf{p}}, \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d = \mathbf{0}, \end{aligned} \quad (91)$$

$$\min_{\Delta \tilde{\mathbf{p}} \in \mathcal{P}} (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})^H (P_S |h_{SR}|^2 \hat{\mathbf{R}}_d - a P_J^{\max} |h_{JR}|^2 \hat{\mathbf{R}}_j) (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}}) \geq a (\sigma_r^2 \|\mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}}\|^2 + \sigma_d^2), \quad (93)$$

$$\max_{\Delta \tilde{\mathbf{p}} \in \mathcal{P}} (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}})^H (P_S |h_{SR}|^2 \tilde{\mathbf{Q}}_d^H \mathbf{W}_{\text{rb}}^H \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d + P_J^{\max} |h_{JR}|^2 \tilde{\mathbf{Q}}_j^H \mathbf{W}_{\text{rb}}^H \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_j) (\tilde{\mathbf{p}}^* + \Delta \tilde{\mathbf{p}}) \leq P_R^{\max} - \sigma_r^2 \text{tr}(\mathbf{W}_{\text{rb}} \mathbf{W}_{\text{rb}}^H). \quad (94)$$

lated as

$$\begin{aligned} & \max_{\mathbf{W}_{\text{rb}}, u_1, u_2} \bar{\gamma}, \\ \text{s.t.} & \begin{bmatrix} u_1 \mathbf{C} + \Phi_{PJ} & \Phi_{PJ}^H \tilde{\mathbf{p}}^* \\ (\tilde{\mathbf{p}}^*)^H \Phi_{PJ} & t_1 \end{bmatrix} \succeq 0, \\ & \begin{bmatrix} u_2 \mathbf{C} - \Phi_{JD} & -\Phi_{JD}^H \tilde{\mathbf{p}}^* \\ -(\tilde{\mathbf{p}}^*)^H \Phi_{JD} & t_2 \end{bmatrix} \succeq 0, \\ & \mathbf{h}_{RE} \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d = \mathbf{0}, u_1 > 0, u_2 > 0, \end{aligned} \quad (96)$$

where

$$t_1 = (\tilde{\mathbf{p}}^*)^H \Phi_{PJ} \tilde{\mathbf{p}}^* - u_1 - \sigma_r^2 a (1 + \|\mathbf{h}_{RD}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}} \mathbf{W}_{\text{rb}}\|^2), \quad (97)$$

$$t_2 = P_R^{\max} - u_2 - (\tilde{\mathbf{p}}^*)^H \Phi_{JD} \tilde{\mathbf{p}}^* - \sigma_r^2 \text{tr}(\mathbf{W}_{\text{rb}} \mathbf{W}_{\text{rb}}^H), \quad (98)$$

$$\Phi_{PJ} = P_S |h_{SD}|^2 \hat{\mathbf{R}}_d - a P_J^{\max} |h_{JR}|^2 \hat{\mathbf{R}}_j, \quad (99)$$

$$\begin{aligned} \Phi_{JD} &= P_S |h_{SR}|^2 \tilde{\mathbf{Q}}_d^H \mathbf{W}_{\text{rb}}^H \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_d \\ &+ P_J^{\max} |h_{JR}|^2 \tilde{\mathbf{Q}}_j^H \mathbf{W}_{\text{rb}}^H \mathbf{W}_{\text{rb}} \tilde{\mathbf{Q}}_j. \end{aligned} \quad (100)$$

The optimization (96) is still nonconvex with respect to  $\mathbf{W}_{\text{rb}}$ . Similar to solving (80), some mathematical transformations are applied to reformulate (96) into a standard SDP problem with a rank-1 constraint. Specifically, by defining

$$\mathbf{W}'_{\text{rb}} = \text{vec}(\mathbf{W}_{\text{rb}}) \text{vec}(\mathbf{W}_{\text{rb}})^H \in \mathbb{C}^{N_R^2 \times N_R^2}, \quad (101)$$

the problem (96) is transformed into

$$\begin{aligned} & \max_{\mathbf{W}'_{\text{rb}}, u_1, u_2} \bar{\gamma}, \\ \text{s.t.} & \begin{bmatrix} u_1 \mathbf{C} + \Phi'_{PJ} & \Phi'_{PJ}{}^H \tilde{\mathbf{p}}^* \\ (\tilde{\mathbf{p}}^*)^H \Phi'_{PJ} & t'_1 \end{bmatrix} \succeq 0, \\ & \begin{bmatrix} u_2 \mathbf{C} - \Phi'_{JD} & -\Phi'_{JD}{}^H \tilde{\mathbf{p}}^* \\ -(\tilde{\mathbf{p}}^*)^H \Phi'_{JD} & t'_2 \end{bmatrix} \succeq 0, \\ & \text{tr}(\hat{\mathbf{Q}}_e \mathbf{W}'_{\text{rb}}) = 0, \mathbf{W}'_{\text{rb}} \succeq 0, \text{rank}(\mathbf{W}'_{\text{rb}}) = 1, \\ & u_1 > 0, u_2 > 0, \end{aligned} \quad (102)$$

where

$$t'_1 = (\tilde{\mathbf{p}}^*)^H \Phi'_{PJ} \tilde{\mathbf{p}}^* - u_1 - \sigma_r^2 a (1 + \text{tr}(\mathbf{G}_b \mathbf{W}'_{\text{rb}})), \quad (103)$$

$$t'_2 = P_R^{\max} - u_2 - (\tilde{\mathbf{p}}^*)^H \Phi'_{JD} \tilde{\mathbf{p}}^* - \sigma_r^2 \text{tr}(\mathbf{W}'_{\text{rb}}), \quad (104)$$

$$\begin{aligned} \Phi'_{PJ} &= P_S |h_{SD}|^2 \hat{\mathbf{Q}}_d^H (\mathbf{W}'_{\text{rb}})^* \hat{\mathbf{Q}}_d \\ &- a P_J^{\max} |h_{JR}|^2 \hat{\mathbf{Q}}_j^H (\mathbf{W}'_{\text{rb}})^* \hat{\mathbf{Q}}_j, \end{aligned} \quad (105)$$

$$\hat{\mathbf{Q}}_k = (\tilde{\mathbf{Q}}_k \otimes (\mathbf{R}_{\text{cor}}^{\frac{1}{2}})^T \mathbf{h}_{RD}), k = d, j, \quad (106)$$

$$\Phi'_{JD} = P_S |h_{SR}|^2 \tilde{\mathbf{D}}_d + P_J^{\max} |h_{JR}|^2 \tilde{\mathbf{D}}_j, \quad (107)$$

$$\hat{\mathbf{Q}}_e = (\tilde{\mathbf{Q}}_d^* \otimes (\mathbf{h}_{RE}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}})^H) (\tilde{\mathbf{Q}}_d^T \otimes \mathbf{h}_{RE}^T \mathbf{R}_{\text{cor}}^{\frac{1}{2}}), \quad (108)$$

$$\begin{aligned} \tilde{\mathbf{D}}_k [\hat{m}, \hat{n}] &= \text{tr}((\tilde{\mathbf{Q}}_k^* \otimes \mathbf{I}_{N_R}) \tilde{\mathbf{I}}_{\hat{m}}^H \tilde{\mathbf{I}}_{\hat{n}} (\tilde{\mathbf{Q}}_k^T \otimes \mathbf{I}_{N_R}) \mathbf{W}'_{\text{rb}}), \\ & k = d, j, \end{aligned} \quad (109)$$

with  $\tilde{\mathbf{I}}_l = [\mathbf{0}_{N_R \times (l-1)N_R} \mathbf{I}_{N_R} \mathbf{0}_{N_R \times (3N_R-l)N_R}] \in \mathbb{C}^{N_R \times 3N_R^2}$ , for  $l = \hat{m}, \hat{n}$  and  $1 \leq \hat{m}, \hat{n} \leq 3N_R$ . The penalty based method can also be used to solve the problem (102) effectively, and the obtained  $\mathbf{W}'_{\text{rb}}$  guarantees to satisfy the rank-1 property. The detailed optimization procedure is the same as that presented in Subsection IV-A. This proposed robust beamforming algorithm is based on the iterative SDP optimization, which is similar to the one we used to solve the secrecy rate maximization with perfect CSI presented in Subsection IV-A. Therefore, it has the same order of magnitude of the per-iteration complexity as the algorithm of Subsection IV-A, which can be shown to be

$$C_{\text{per-ite}}^{\text{robu}} = \mathcal{O} \left( (2(N_R^2)^{3.5} + 4(N_R^2)^{2.5} + 8(N_R^2)^{0.5}) \log \left( \frac{1}{\epsilon} \right) \right). \quad (110)$$

## V. SIMULATION RESULTS

In the simulation study, the DOA of desired signal  $s_d$  is specified by  $(\theta_d = 40^\circ, \varphi_d = 90^\circ)$ , and its POA is given by  $(\alpha_d = -30^\circ, \beta_d = 0^\circ)$ . For jammer signal  $s_j$ , its DOA is  $(\theta_j, 90^\circ)$  with  $\theta_j \in [0, \pi]$ , and its POA is  $(\alpha_j, \beta_j)$  with  $\alpha_j \in [-\frac{\pi}{2}, \frac{\pi}{2}]$  and  $\beta_j \in [-\frac{\pi}{4}, \frac{\pi}{4}]$ . Thus, the spatial and polarization distances between  $s_d$  and  $s_j$  are given respectively by  $\Delta_a = |\theta_j -$

TABLE I  
THE LIST OF MAJOR SIMULATION VARIABLES AND OPTIMIZED RESULTS

Scenario	DOA of $s_j$	Optimized 8-element array spatial angles $(\theta^{(e)}, \varphi^{(e)})$ (degrees) for given $\Delta_p$
SIMO Network	$(35^\circ, 90^\circ)$	$\begin{cases} \begin{bmatrix} 17.24 & 136.24 & 158.07 & 40.95 & 28.56 & 142.68 & 148.61 & 37.59 \\ 73.61 & -51.26 & 73.60 & -52.79 & 83.83 & -52.79 & 87.36 & -52.06 \end{bmatrix} & \Delta_p = 20^\circ \\ \begin{bmatrix} 109.87 & 107.99 & 66.16 & 19.03 & 142.15 & 143.02 & 42.10 & 52.63 \\ -60.87 & -44.87 & -67.54 & -17.06 & 56.72 & 64.35 & -19.63 & 58.86 \end{bmatrix} & \Delta_p = 10^\circ \\ \begin{bmatrix} 87.41 & 88.17 & 90.56 & 90.35 & 88.85 & 90.81 & 90.76 & 90.69 \\ 45.17 & 45.17 & 45.17 & 45.17 & 45.17 & 45.17 & 45.17 & 45.17 \end{bmatrix} & \Delta_p = 0^\circ \end{cases}$
	$(55^\circ, 90^\circ)$	$\begin{cases} \begin{bmatrix} 65.67 & 54.43 & 125.57 & 118.73 & 58.17 & 66.55 & 114.63 & 123.94 \\ -66.74 & -59.71 & -66.31 & -54.00 & -54.45 & -63.38 & -57.70 & -69.35 \end{bmatrix} & \Delta_p = 20^\circ \\ \begin{bmatrix} 65.71 & 55.94 & 124.14 & 119.30 & 58.59 & 65.80 & 116.15 & 122.38 \\ -71.70 & -58.84 & -68.75 & -52.39 & -52.65 & -66.24 & -57.48 & -74.12 \end{bmatrix} & \Delta_p = 10^\circ \\ \begin{bmatrix} 71.47 & 44.56 & 90.00 & 90.00 & 90.00 & 90.00 & 135.44 & 108.53 \\ 63.16 & -55.80 & 85.27 & -89.71 & 20.11 & 25.30 & -55.80 & 63.17 \end{bmatrix} & \Delta_p = 0^\circ \end{cases}$
Relaying Network	$(35^\circ, 90^\circ)$	$\begin{cases} \begin{bmatrix} 92.18 & 91.54 & 91.88 & 96.72 & 90.66 & 81.99 & 93.32 & 91.50 \\ 36.02 & 36.42 & 36.13 & 36.00 & 36.03 & 36.07 & 36.56 & 36.74 \end{bmatrix} & \Delta_p = 20^\circ \\ \begin{bmatrix} 94.05 & 85.94 & 94.05 & 85.94 & 85.94 & 85.94 & 94.05 & 85.94 \\ 34.02 & 34.03 & 34.07 & 34.02 & 34.03 & 34.02 & 34.02 & 34.02 \end{bmatrix} & \Delta_p = 10^\circ \\ \begin{bmatrix} 84.10 & 84.97 & 84.73 & 86.87 & 94.99 & 91.28 & 95.47 & 88.87 \\ 30.13 & 30.12 & 30.12 & 30.12 & 30.12 & 30.11 & 30.12 & 30.11 \end{bmatrix} & \Delta_p = 0^\circ \end{cases}$
	$(55^\circ, 90^\circ)$	$\begin{cases} \begin{bmatrix} 114.25 & 129.26 & 62.07 & 63.40 & 118.09 & 113.27 & 64.72 & 70.00 \\ -42.17 & -43.39 & -44.34 & -50.01 & -50.70 & -44.34 & -46.38 & -41.88 \end{bmatrix} & \Delta_p = 20^\circ \\ \begin{bmatrix} 64.05 & 65.03 & 116.16 & 116.37 & 64.84 & 64.40 & 114.38 & 114.95 \\ 39.79 & -34.00 & -46.81 & 43.68 & 47.26 & -48.34 & 35.78 & -42.98 \end{bmatrix} & \Delta_p = 10^\circ \\ \begin{bmatrix} 76.81 & 127.90 & 98.78 & 95.53 & 95.14 & 78.60 & 58.68 & 109.30 \\ 61.70 & -17.16 & -64.91 & 30.57 & -75.27 & -35.15 & 60.26 & -36.25 \end{bmatrix} & \Delta_p = 0^\circ \end{cases}$

$40^\circ$  and  $\Delta_p = \arccos(\cos 2\beta_d \cos 2\beta_j \cos(2(\alpha_d - \alpha_j)) + \sin 2\beta_d \sin 2\beta_j)$  [34]. The 8-antenna PSA is considered in our simulations and the antenna spacing is half of the transmit signal wavelength.<sup>3</sup> In the SIMO network, the eavesdropper is equipped with  $N_E = 6$  antennas. All channel coefficients are generated independently according to  $\mathcal{CN}(0, 1)$  and the power of the receive additive noise is  $\sigma_e^2 = \sigma^2 = 1$ . In order to solve the standard convex optimization problems such as the GP (38) and the SDP (86) efficiently, the software toolbox CVX [32] is used. Under this simulation setting, we perform numerical evaluations for the point-to-point SIMO network and the relaying network, respectively. In order to demonstrate the advantages of PSA, the standard CSA based technique is utilized as a comparison. Specifically, instead of employing the 8-element PSA, the destination  $D$  also employs the CSA with 8 antennas in the SIMO network case, while the relay  $R$  is also equipped with the 8-element CSA in the relay network case. All the results are averaged over 500 Monte Carlo simulations.

For different DOAs of the jammer signal  $s_j$ , Table I presents the optimized spatial pointings of the 8-antenna PSA for both the SIMO network and the relaying network is presented. The corresponding optimal destination beamforming and relay beamforming can be derived from (32) and (77), respectively.

#### A. The SIMO Network

We first consider the security performance of the SIMO network with the proposed algorithm for optimizing the receive beamforming, power allocation and PSA spatial pointings.

1) *Total power minimization:* With the 8-antenna PSA, Fig. 4 depicts the minimum power consumption of the SIMO

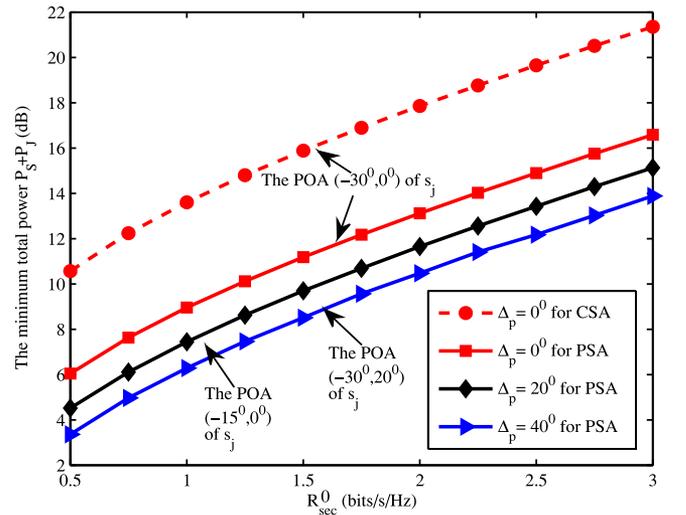


Fig. 4. The minimum total power consumption as the function of the secrecy rate threshold  $R_{\text{sec}}^0$  under different polarization distances  $\Delta_p$ . The DOA of  $s_j$  is  $(35^\circ, 90^\circ)$ .

network as the function of the secrecy rate threshold  $R_{\text{sec}}^0$ , under three different polarization distances  $\Delta_p$  with the DOA of jammer signal  $s_j$  given by  $(35^\circ, 90^\circ)$ , which is slightly difficult from the DOA  $(40^\circ, 90^\circ)$  of desired signal  $s_d$ . Thus, the spatial distance between  $s_d$  and  $s_j$  is only  $\Delta_a = 5^\circ$ , which is considered to be very small. Three POA values considered for  $s_j$  are  $(\alpha_j, \beta_j) \in \{(-30^\circ, 0^\circ), (-20^\circ, 0^\circ), (-30^\circ, 20^\circ)\}$ , corresponding to three polarization distances  $\Delta_p = 0^\circ, 20^\circ$  and  $40^\circ$ , respectively. It is obvious that the minimum total power consumption is a monotonously increasing function of the required secrecy rate  $R_{\text{sec}}^0$ , as clearly indicated in Fig. 4. Also observe from Fig. 4 that for the PSA, increasing  $\Delta_p$  leads to reduction in the total power consumption, which confirms that the polarization difference between the two signals is beneficial to improve the power efficiency of the PSA based SIMO network. As a

<sup>3</sup>Note that our work can also be extended easily to the planar array case with the different spatial phase matrix. Moreover, since the spatial phase matrix is not related to any optimization variable, the simulation conclusions obtained by applying the planar array are similar to that in Section V.

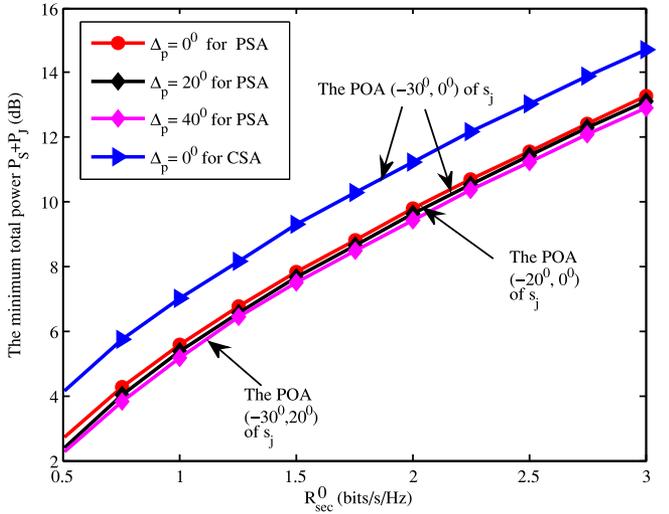


Fig. 5. The minimum total power consumption as the function of the secrecy rate threshold  $R_{\text{sec}}^0$  under different polarization distances  $\Delta_p$ . The DOA of  $s_j$  is  $(10^\circ, 90^\circ)$ .

comparison, the minimum total power consumption required by the CSA based SIMO network with the POA of  $s_j$  given by  $(-30^\circ, 0^\circ)$  is also plotted in Fig. 4, where it can be seen that the CSA needs consume more than 4 dB of power to achieve the required  $R_{\text{sec}}^0$ , compared with the PSA. This is because the CSA cannot utilize the signals' polarization information to improve performance.

We then change the DOA of  $s_j$  to  $(10^\circ, 90^\circ)$ , and repeat the same experiment. The results obtained are shown in Fig. 5. Compared with Fig. 4, we observe that the power consumptions of the both CSA-based and PSA-based SIMO networks are greatly reduced, because we have a large spatial difference  $\Delta_a = 30^\circ$  between  $s_d$  and  $s_j$ . From Fig. 5, it can be seen that the three minimum power consumption curves of the PSA for the three different polarization distances  $\Delta_p$  become very close. This phenomenon demonstrates that the polarization difference  $\Delta_p$  has little effect on the network performance when the two signals have a sufficiently large spatial distance. The results of Fig. 5 again confirm the advantage of the PSA over the CSA, as the former achieves 2 dB saving in power consumption in comparison with the latter.

Additionally, Fig. 6 depicts the minimum total power consumption of the PSA SIMO network as the function of DOA  $(\theta_j, 90^\circ)$  of  $s_j$  under three different polarization distances  $\Delta_p$  and given the secrecy rate threshold  $R_{\text{sec}}^0 = 2.5$  bits/s/Hz. It can be seen that as the DOA difference between  $s_d$  and  $s_j$ ,  $\Delta_a \rightarrow 0$ , the power consumption reaches the highest value. Again, increasing the polarization distance  $\Delta_p$  leads to the reduction in power consumption, as clearly shown in Fig. 6. Furthermore, when the spatial separation  $\Delta_a$  is sufficiently large, the influence of the polarization difference  $\Delta_p$  to power consumption becomes very small.

2) *Secrecy rate maximization*: In this investigation, we set the POA of  $s_j$  to  $(\alpha_j, 0^\circ)$ . The polarization distance between  $s_d$  and  $s_j$  is given by  $\Delta_p = 2|\alpha_j + 30^\circ|$ . Fig. 7 depicts the

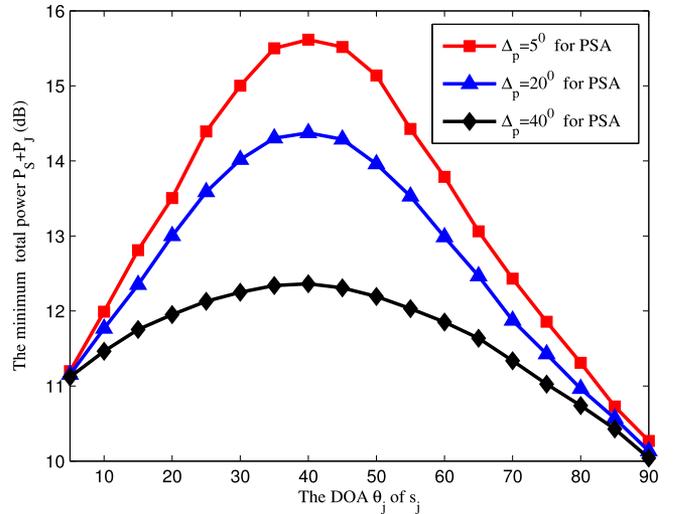


Fig. 6. The minimum total power consumption as the function of the PSA SIMO network as the function of the DOA  $(\theta_j, 90^\circ)$  of  $s_j$  under different polarization distances  $\Delta_p$  and given  $R_{\text{sec}}^0 = 2.5$  bits/s/Hz.

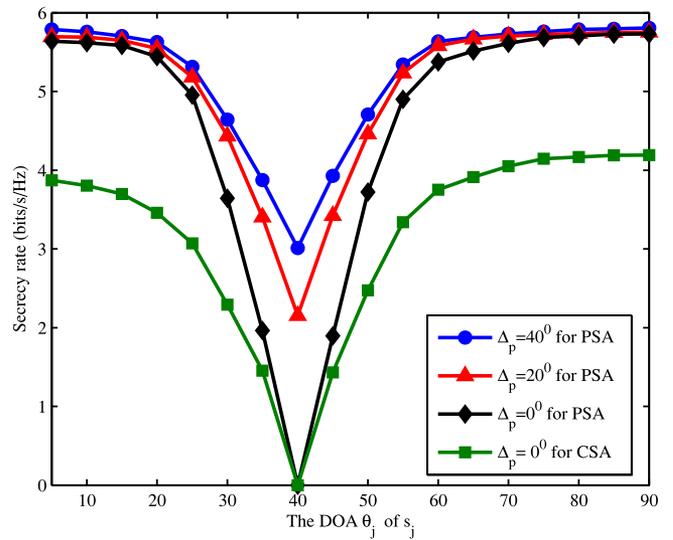


Fig. 7. The achievable secrecy rate as the function of the DOA  $(\theta_j, 90^\circ)$  of  $s_j$  under different polarization distances  $\Delta_p$  and given the total transmit power  $P_{\text{max}} = 12$  dB.

achievable secrecy rates of the PSA based SIMO network as the functions of the DOA  $(\theta_j, 90^\circ)$  of  $s_j$ , given  $P_{\text{max}} = P_S^{\text{max}} + P_J^{\text{max}} = 12$  dB. It can be seen that for a given  $\Delta_p$ , the achievable secrecy rate is reduced rapidly as the spatial separation between  $s_d$  and  $s_j$ ,  $\Delta_a = |\theta_j - 40^\circ|$ , decreases, and when  $\Delta_a \rightarrow 0$ , the achievable secrecy rate reaches the minimum value. It is also clear that the achievable secrecy rate increases with the increase of the polarization separation  $\Delta_p$ . Moreover, the influence of  $\Delta_p$  to the achievable secrecy rate is particularly strong when the two signals are near spatially inseparable, while the influence of  $\Delta_p$  becomes very small when the signals are sufficiently separable in the spatial domain. Note that at  $\Delta_p = 0$  and  $\Delta_a = 0$ , the secrecy rate is zero. As a comparison, the secrecy rate of the CSA-based

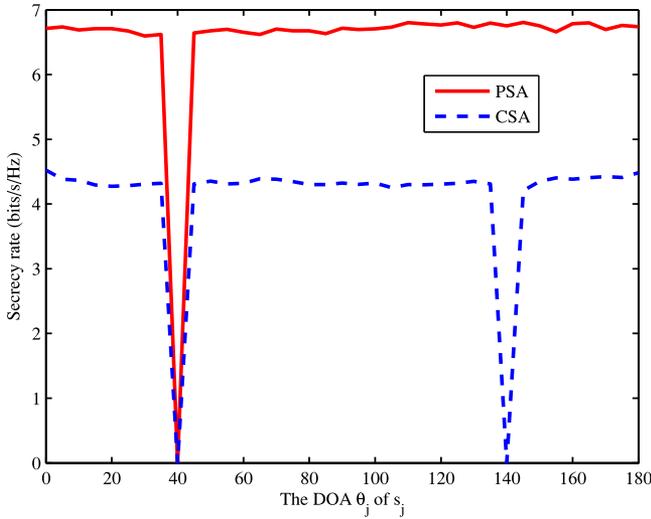


Fig. 8. The achievable secrecy rate as the function of the DOA  $(\theta_j, 90^\circ)$  of  $s_j$  given the polarization distance  $\Delta_p = 0$  and the total transmit power  $P_{\max} = 14$  dB. Note that the range of  $\theta_j$  is expanded from  $90^\circ$  to  $180^\circ$ .

SIMO network under  $\Delta_p = 0^\circ$  is also given in Fig. 7, where it is apparent that the PSA significantly outperforms the CSA.

Next we increase  $P_{\max}$  to 14 dB and expand the range of  $\theta_j$  from  $[0^\circ, 90^\circ]$  to  $[0^\circ, 180^\circ]$ . Given  $\Delta_p = 0$ , Fig. 8 compares the achievable secrecy rate of the PSA SIMO network with that of the CSA SIMO network. As expected, both the PSA and CSA attain a zero secrecy rate at  $\theta_j = 40^\circ$ , as at this point, both  $\Delta_a = 0$  and  $\Delta_p = 0$ . However, it is further noticed that for the CSA, the secrecy rate also deteriorates to zero when the DOA of  $s_j$  is  $(140^\circ, 90^\circ)$ . This is owing to the symmetric fuzzification and is referred to as grating lobe. By contrast, the secure communication of the SIMO network employing PSA is realized without introducing grating lobes, which is another significant advantage of the PSA over the CSA.

**B. The Relaying Network**

We now investigate the secure communication of the relay aided network. The DOAs and POAs of the incident signals  $\tilde{s}_d$  and  $\tilde{s}_j$  are the same as those given in Section V-A for the SIMO network. We concentrate on the maximum secrecy rate of the relaying network obtained by the iterative algorithm proposed in Section IV-A, assuming a perfect realization of the PSA pointing vector, but the robust design with imperfect realization of the PSA pointing vector is also studied.

1) *The secrecy rate maximization for the relaying network:* First, we demonstrate the convergence of our proposed iterative optimization algorithm given in Section IV-A. Specifically, we choose the POA  $(0^\circ, 0^\circ)$  for  $\tilde{s}_j$ , i.e., we consider the case of  $\Delta_p = 2|\alpha_j + 30^\circ| = 60^\circ$ , and we set  $P_s = 14$  dB,  $P_R^{\max} = 25$  dB and  $P_J^{\max} = 10$  dB. Fig. 9 depicts the convergence performance of the proposed iterative optimization algorithm under both the spatially separable and spatially inseparable cases. It can be seen from Fig. 9 that for the case of  $\Delta_a > 0$ , the algorithm takes  $l = 3$  outer iterations to con-

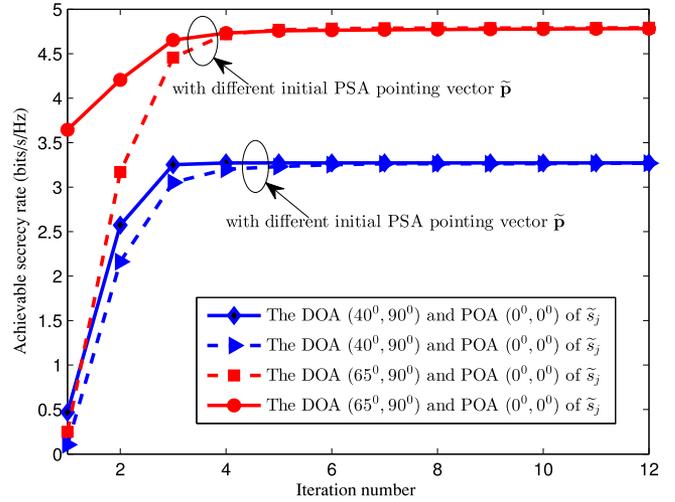


Fig. 9. Convergence performance of the proposed iterative algorithm for relaying network, given  $P_s = 14$  dB,  $P_R^{\max} = 25$  dB and  $P_J^{\max} = 10$  dB.

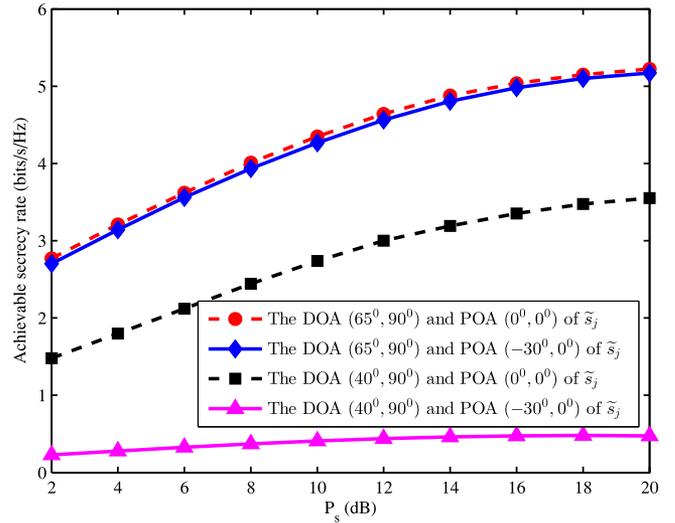


Fig. 10. The achievable secrecy rate of the PSA based relaying network as the function of source transmit power  $P_s$  under different DOA and POA settings of  $\tilde{s}_j$  with  $P_J^{\max} = 10$  dB and  $P_R^{\max} = 25$  dB.

verge, while for the case of  $\Delta_a = 0$ , the algorithm converges within  $l = 6$  outer iterations. Moreover, the choice of the initial  $\tilde{\mathbf{p}}^{(0)}$  does not seem to affect the algorithm’s convergence performance.

In Fig. 10, the achievable secrecy rate of the PSA relaying network is depicted as the function of the source transmit power  $P_s$ , under different DOA  $(\theta_j, 90^\circ)$  and POA  $(\alpha_j, 0^\circ)$  of jammer signal  $\tilde{s}_j$  with the maximum relay power  $P_R^{\max} = 25$  dB and the maximum jammer power  $P_J^{\max} = 10$  dB. Obviously, the achievable secrecy rate is a monotonically increasing function of  $P_s$  but it exhibits a saturation trend for large  $P_s$ . This is because increasing  $P_s$  also increases the information leakage from source  $S$  to eavesdropper  $E$ , while the relay transmit power  $P_R^{\max}$  is limited. Therefore, the achievable secrecy rate cannot go arbitrarily high. With the DOA of  $\tilde{s}_j$  given by  $(65^\circ, 90^\circ)$ ,

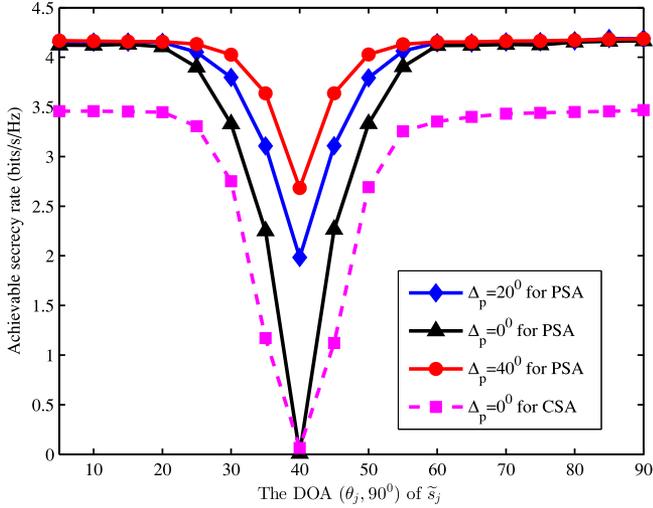


Fig. 11. The achievable secrecy rate of the relay network as the function of the DOA  $(\theta_j, 90^\circ)$  of  $\tilde{s}_j$  under different polarization differences  $\Delta_p$  and given  $P_J^{\max} = P_S = 10$  dB and  $P_R^{\max} = 25$  dB.

which is distinguishable from the DOA  $(40^\circ, 90^\circ)$  of  $\tilde{s}_d$ , the influence of the polarization distance  $\Delta_p$  between  $\tilde{s}_d$  and  $\tilde{s}_j$  on the achievable secrecy rate is very small. However, when  $\tilde{s}_j$  and  $\tilde{s}_d$  are spatially inseparable with  $\Delta_a = 0^\circ$ , the influence of  $\Delta_p$  becomes significant, and a larger  $\Delta_p$  leads to a larger achievable secrecy rate. Also observe from Fig. 10 that under the condition of  $\Delta_a = 0^\circ$  and  $\Delta_p = 0^\circ$ , the achievable secrecy rate of the PSA relaying network is very small.

Fig. 11 compares the achievable secrecy rates of the PSA and CSA relaying networks given the DOA  $(\theta_j, 90^\circ)$  for  $\tilde{s}_j$  with  $\theta_j \in [0^\circ, 90^\circ]$ ,  $P_J^{\max} = 10$  dB and  $P_S = 15$  dB. In this case, the POA of  $\tilde{s}_j$  is given by  $(\alpha_j, 0^\circ)$ , and the polarization distance between  $\tilde{s}_d$  and  $\tilde{s}_j$  is  $\Delta_p = 2|\alpha_j + 30^\circ|$ . The results of Fig. 11 demonstrate that the PSA based relaying network significantly outperforms the CSA based relaying network, in terms of achievable secrecy rate. Similar to the SIMO network case, at  $\Delta_a = 0^\circ$ , the achievable secrecy rates of both the PSA and CSA relaying networks deteriorate to their minimum values. In particular, under the condition of  $\Delta_a = 0^\circ$  and  $\Delta_p = 0^\circ$ , the secrecy rate of the CSA relaying network is zero but the secrecy rate of the PSA relaying network is a small nonzero value. Furthermore, by increasing the polarization separation  $\Delta_p$  to nonzero, the secrecy rate of the PSA relaying network can be increased considerably, because the PSA can effectively utilize the polarization information.

2) *Robust design with imperfect realization of the PSA pointing:* We next illustrate our robust beamforming optimization design for the PSA relaying network with imperfect PSA pointing realization. We set the PSA pointing error bound to  $\mathbf{C} = 100\mathbf{I}_{3N_R}$ . In order to reduce the computation complexity, we consider the 4-antenna PSA. In Fig. 12, the achievable secrecy rates of three designs as the functions of the maximum source transmit power  $P_S$  are depicted, given different DOA and POA conditions for  $\tilde{s}_j$  with the 4-antenna PSA as well as  $P_J^{\max} = 10$  dB and  $P_R^{\max} = 25$  dB. Based on the secrecy rate

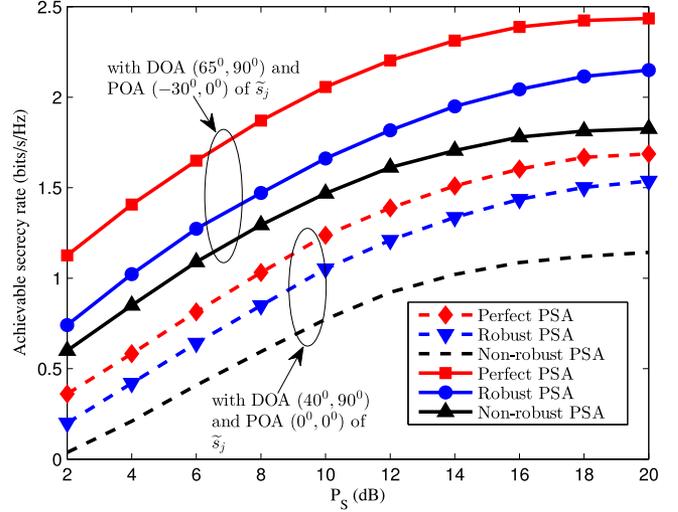


Fig. 12. The achievable secrecy rates of three designs as the functions of  $P_s$ , under different DOA and POA settings of  $\tilde{s}_j$  with the 4-antenna PSA as well as  $P_J^{\max} = 10$  dB and  $P_R^{\max} = 25$  dB.

maximization of Section IV-A, we can obtain the optimal design of  $\mathbf{W}^*$  and  $\tilde{\mathbf{p}}^*$ . If the PSA pointing implementation is perfect, we can realize the exact optimal PSA pointing solution  $\tilde{\mathbf{p}}^*$ , which is the curve under the title ‘Perfect PSA’ in Fig. 12. However, in practice, there usually exists PSA pointing implementation error, and the optimal design of  $\tilde{\mathbf{p}}^*$  is actually implemented as  $\tilde{\mathbf{p}}^* + \Delta\tilde{\mathbf{p}}$ , which is the curve under the title ‘Non-robust PSA’ in Fig. 12. Obviously, this implementation is far from optimal, and the actual secrecy rate achieved is significantly lower than that obtained with the perfect implementation of  $\tilde{\mathbf{p}}^*$ . Under the imperfect implementation of  $\tilde{\mathbf{p}}^* + \Delta\tilde{\mathbf{p}}$ , our robust beamforming optimization design presented in Section IV-B is capable of re-gaining considerable secrecy rate performance, which is shown in Fig. 12 under the title ‘Robust PSA’.

## VI. CONCLUSION

In this paper, a joint beamforming, power allocation and PSA pointing optimization has been proposed for wireless communications. Our main contribution has been to apply the polarization sensitive array to improve the security performance of wireless communications. Specifically, by utilizing the polarization difference among signals, the interference caused by jammer to destination is greatly reduced while the information leakage to eavesdropper is minimized, even when these signals are spatially indistinguishable. Two communication scenarios, the PSA based SIMO network and the PSA aided relaying network, have been considered. For the former scenario, both total transmit power minimization and secrecy rate maximization have been performed. For the relaying network assuming perfect CSI, both secrecy rate maximization designs under perfect and imperfect PSA spatial pointing implementations have been obtained. Since all the optimization problems involved are nonconvex with complicated constraints and/or objectives, alternative suboptimal algorithms have been proposed which enable us to apply convex optimization techniques to solve the transformed optimization

problems efficiently. Extensive simulation results have demonstrated the effectiveness of our proposed PSA based techniques for enhancing physical-layer security. In particular, it has been shown that the improvement of maximum achievable secrecy rate of wireless networks by the proposed PSA techniques over the standard CSA techniques is remarkable.

#### APPENDIX

The convergence of the proposed iterative algorithm to solve the optimization problem (31) was demonstrated in [29]. Here we prove the convergence of this algorithm.

Firstly, we define the following objective function

$$\begin{aligned} f(\mathbf{P}_c) &= \text{tr}(\mathbf{P}_c) - \lambda_{\max}(\mathbf{P}_c) - \text{tr}(\boldsymbol{\vartheta}_{\max} \boldsymbol{\vartheta}_{\max}^H (\mathbf{P}_c - \mathbf{P}_c)) \\ &= \text{tr}(\mathbf{P}_c) - \lambda_{\max}(\mathbf{P}_c). \end{aligned} \quad (111)$$

Then the lower bound of  $f(\mathbf{P}_c)$  is zero according to the following lemma.

*Lemma 1.* For an arbitrary square matrix  $\mathbf{A}$ , it holds that  $\text{tr}(\mathbf{A}) - \lambda_{\max}(\mathbf{A}) \geq 0$ , in which the equality is guaranteed if and only if  $\text{rank}(\mathbf{A}) = 1$  is satisfied.

Next, we modify  $f(\mathbf{P}_c)$  into the following penalty function

$$\begin{aligned} \tilde{f}(\mathbf{P}_c^{(t+1)}) &= \min_{\mathbf{P}_c} \text{tr}(\mathbf{P}_c) - \lambda_{\max}(\mathbf{P}_c^{(t)}) \\ &\quad - \text{tr}(\boldsymbol{\vartheta}_{\max}^{(t)} (\boldsymbol{\vartheta}_{\max}^{(t)})^H (\mathbf{P}_c - \mathbf{P}_c^{(t)})), \end{aligned} \quad (112)$$

where  $\text{tr}(\mathbf{P}_c) - \lambda_{\max}(\mathbf{P}_c^{(t)}) - \text{tr}(\boldsymbol{\vartheta}_{\max}^{(t)} (\boldsymbol{\vartheta}_{\max}^{(t)})^H (\mathbf{P}_c - \mathbf{P}_c^{(t)}))$  is the objective function in the  $(t+1)$ th iteration of (31).

Let  $\mathbf{P}_c^{(t)}$  be the optimal matrix obtained at the  $t$ th iteration of (31). Using  $\mathbf{P}_c^{(t)}$  in the iterative optimization procedure yields the optimal matrix  $\mathbf{P}_c^{(t+1)}$  at the  $(t+1)$ th iteration, which is feasible. Clearly, the optimized  $\tilde{f}(\mathbf{P}_c^{(t+1)})$  satisfies

$$\begin{aligned} \tilde{f}(\mathbf{P}_c^{(t+1)}) &= \text{tr}(\mathbf{P}_c^{(t+1)}) - \lambda_{\max}(\mathbf{P}_c^{(t)}) \\ &\quad - \text{tr}(\boldsymbol{\vartheta}_{\max}^{(t)} (\boldsymbol{\vartheta}_{\max}^{(t)})^H (\mathbf{P}_c^{(t+1)} - \mathbf{P}_c^{(t)})) \\ &\leq \text{tr}(\mathbf{P}_c^{(t)}) - \lambda_{\max}(\mathbf{P}_c^{(t)}) \\ &\quad - \text{tr}(\boldsymbol{\vartheta}_{\max}^{(t)} (\boldsymbol{\vartheta}_{\max}^{(t)})^H (\mathbf{P}_c^{(t)} - \mathbf{P}_c^{(t)})) \\ &= f(\mathbf{P}_c^{(t)}). \end{aligned} \quad (113)$$

For an arbitrary Hermitian matrix  $\mathbf{Z}$ , the following relationship holds

$$\begin{aligned} \text{tr}(\boldsymbol{\vartheta}_{\max} \boldsymbol{\vartheta}_{\max}^H (\mathbf{Z} - \mathbf{P}_c^{(t)})) &= \boldsymbol{\vartheta}_{\max}^H \mathbf{Z} \boldsymbol{\vartheta}_{\max} - \boldsymbol{\vartheta}_{\max}^H \mathbf{P}_c^{(t)} \boldsymbol{\vartheta}_{\max} \\ &= \boldsymbol{\vartheta}_{\max}^H \mathbf{Z} \boldsymbol{\vartheta}_{\max} - \lambda_{\max}(\mathbf{P}_c^{(t)}) \leq \lambda_{\max}(\mathbf{Z}) - \lambda_{\max}(\mathbf{P}_c^{(t)}). \end{aligned} \quad (114)$$

Therefore, we further obtain

$$\begin{aligned} \lambda_{\max}(\mathbf{P}_c^{(t+1)}) - \lambda_{\max}(\mathbf{P}_c^{(t)}) &\geq \\ \text{tr}(\boldsymbol{\vartheta}_{\max}^{(t)} (\boldsymbol{\vartheta}_{\max}^{(t)})^H (\mathbf{P}_c^{(t+1)} - \mathbf{P}_c^{(t)})). \end{aligned} \quad (115)$$

Based on (115), the function  $f(\mathbf{P}_c^{(t+1)})$  satisfies

$$\begin{aligned} f(\mathbf{P}_c^{(t+1)}) &= \text{tr}(\mathbf{P}_c^{(t+1)}) - \lambda_{\max}(\mathbf{P}_c^{(t+1)}) \\ &= \text{tr}(\mathbf{P}_c^{(t+1)}) - \lambda_{\max}(\mathbf{P}_c^{(t)}) + \lambda_{\max}(\mathbf{P}_c^{(t)}) - \lambda_{\max}(\mathbf{P}_c^{(t+1)}) \\ &\leq \text{tr}(\mathbf{P}_c^{(t+1)}) - \lambda_{\max}(\mathbf{P}_c^{(t)}) - \text{tr}(\boldsymbol{\vartheta}_{\max}^{(t)} (\boldsymbol{\vartheta}_{\max}^{(t)})^H (\mathbf{P}_c^{(t+1)} - \mathbf{P}_c^{(t)})) \\ &\leq f(\mathbf{P}_c^{(t)}), \end{aligned} \quad (116)$$

where the first inequality and the second inequality hold due to (115) and (113), respectively.

Thus, given an initial feasible  $\mathbf{P}_c^{(0)}$ , the optimization problem (31) can be iteratively solved to obtain a sequence  $\mathbf{P}_c^{(t)}$ ,  $t = 1, 2, \dots$ , whose rank approaches 1. Since this iteration procedure is monotonically decreasing, in terms of the objective function  $f(\mathbf{P}_c^{(t)})$ , as shown in (116), which has a lower bound of zero based on Lemma 1, it is naturally converged. Consequently, we conclude that the iterative optimization problem (31) based on the penalty function method converges to a rank-1 solution.

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