# **Reconfigurable Rateless Codes**

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Abstract—We propose novel reconfigurable rateless codes, that are capable of not only varying the block length but also adaptively modify their encoding strategy by incrementally adjusting their degree distribution according to the prevalent channel conditions without the availability of the channel state information at the transmitter. In particular, we characterize a reconfigurable rateless code designed for the transmission of 9,500 information bits that achieves a performance, which is approximately 1 dB away from the discrete-input continuousoutput memoryless channel's (DCMC) capacity over a diverse range of channel signal-to-noise (SNR) ratios.

*Index Terms*—Reconfigurable rateless codes, adaptive channel coding.

## I. INTRODUCTION

**M**ORE than a decade after the discovery of turbo codes [1] and the rediscovery of low-density paritycheck (LDPC) codes [2], [3], the problem of operating arbitrarily close to capacity using practical encoding and decoding algorithms is feasible, when assuming perfect channel knowledge. These research advances were achieved with the advent of high-performance iterative decoders, and design techniques such as density evolution [4] or extrinsic information transfer (EXIT) [5] charts.

Lately, the community's interest has been shifted towards the quest for codes that are capable of maintaining this excellent performance over channels characterized with widely varying qualities within a diverse range of signal-to-noise ratios (SNR) and where the channel state information is unknown to the transmitter. By employing a conventional *fixed-rate* channel code over such channels, we will naturally be facing the dilemma of opting for high rates to increase the throughput or to reduce the rate in order to achieve a higher error resilience. A channel exhibiting time-variant conditions will therefore necessitate an adaptive channel coding scheme, which is exemplified by *rateless* (or *fountain*) codes, allowing us to freely vary the block length (and thus the code-rate) in order to match a wide range of fluctuating channel conditions.

In the context of rateless codes, one must appropriately distinguish between what we refer to as being the *instantaneous* and the *effective* parameters. The instantaneous parameters, all

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of which will be differentiated by the  $(\cdot)$  notation, constitute those which occur during the actual packet's transmission. On the other hand, the effective parameters can only be determined upon the final successful decoding event. Without delving into the intricate code-design-related details, we define what we refer to as a *generic rateless encoder* as an arbitrary encoder that has the capability of generating "on-the-fly" a potentially infinite bit stream from any K information bits, which is denoted by the binary bit-vector  $\mathbf{a} = (a_1, a_2, \dots, a_K)$ . Let  $\overline{C}_i$  be a  $(\overline{N}_i, K)$  rateless code defined over GF(2), which is capable of generating a codeword  $\overline{\mathbf{c}_i} = (c_1, c_2, \dots, c_{\overline{N}}),$  $\overline{\mathbf{c}}_i \in \overline{C}_i$ , where  $\overline{N}_i$  represents the instantaneous block length at a particular transmission instant i and thus the instantaneous code-rate is defined by  $\overline{R}_i := K/\overline{N}_i$ . Moreover, the code  $\overline{C}_i$ will actually be a prefix to all succeeding codes  $\overline{C}_{i+j}$  having code-rates  $\overline{R}_{i+j} < \overline{R}_i$ , for all j > 0. A generic rateless decoder is then defined as an arbitrary decoder, which is capable of reconstructing the original information bit sequence a, with a low bit error probability from any received codeword  $\mathbf{c}_i$  after *i* transmission instants. The successful decision is then communicated back to the transmitter in the form of a singlebit acknowledgment (ACK) using an idealized error-free, zerodelay feedback channel. Subsequently, the transmitter will cease transmission of the current information sequence a and proceeds to the next sequence.

### A. Related Work

Rateless codes were originally designed to fill erasures inflicted by the binary erasure channel, with the Luby transform [6] code being their first practical realization. Metaphorically speaking, rateless codes can be compared to an abundant water supply (fountain) capable of providing an unlimited number of drops, i.e redundant packets. Palanki and Yedidia in [7] were the first to document the achieved performance of LT codes for transmission over the binary symmetric and the binary-input additive white Gaussian noise (BIAWGN) channels. More particularly, it was demonstrated that the bit error ratio (BER) and block error ratio (BLER) performance of LT codes over these channels exhibit high error floors [7]. For this reason, LT codes used for transmission over noisy channels have always been concatenated with other forward error correction (FEC) schemes, such as iteratively detected bit-interleaved coded modulation [8], generalized LDPC [9], and turbo codes [10]. Recently, we have also witnessed the emergence of Raptor codes [11], which do not share the error floor problem of their predecessors. In fact, the results published in [7], [12] attest near-capacity performance and "universal-like" attributes on a variety of noisy channels. These benefits were then exploited in a number of practical scenarios, such as for wireless relay channels [13] as well as for multimedia transmission [14].

From another point of view, we can consider the family of rateless codes for the provision of incremental redundancy (IR) [15]; for example in the context of adaptiverate schemes or as an instance of the so-called type-II hybrid automatic repeat-request (HARQ) [16] schemes. In such schemes, the transmitter continues to send additional incremental redundancies of a codeword until a positive ACK is received or all redundancy available for the current codeword was sent. The FEC codes that are employed in conjunction with IR are typically referred to as rate-compatible (RC) codes [17]. The techniques applied in order to design RC codes either use *puncturing* [17] of the parity bits from a low rate mother code in order to obtain higher rate codes or employ code *extension* [18] for concatenating additional parity bits to a high-rate code in order to create a low-rate code. Both methods have their own limitations and typically a combination of both techniques is generally preferred [18]. The striking similarities of rateless coding with HARQ were first exploited by Soljanin et al. in [19], who compared the performance of Raptor codes as well as punctured LDPC codes for transmission over the BIAWGN channel. Their results demonstrated that the family of Raptor codes represents a more suitable alternative than punctured LDPCs for covering an extensive range of channel SNR (and thus rates).

It is also worth noting that some rateless code families are closely related to their fixed-rate counterparts. For instance, an LT code [6] is analogous to a non-systematic lowdensity generator matrix (LDGM) [20] based code, having a generator matrix that is calculated online (and thus allowing adaptive-rate configuration for diverse channel conditions) and where the LT encoded codeword corresponds to a sequence of repeated parity-check equation values, each checking the parity of  $d_c$  information bits. Similarly, we can regard Raptor codes [11] as a serial concatenation of a (typically) high-rate LDPC code as the outer code combined with a rateless LDGM code as the inner code. Both the LT as well as Raptor codes are decoded using the classic belief propagation (BP) algorithm, in a similar fashion to the decoding of LDPC codes.

### B. Scope and Outline

To the best of our knowledge, the state-of-the-art rateless codes employ a fixed degree distribution [6]; i.e. the degree distribution used for coining the degree  $d_c$  for each transmitted bit is time invariant and thus channel-independent. Consequently, such rateless codes, can only alter the number of bits transmitted (i.e. the code-rate) in order to cater for the variations of the channel conditions encountered. However, it was shown in [21] that a degree distribution designed for rateless coded transmissions over time-varying noisy channels will depend on the underlying channel characteristics, and therefore a fixed degree distribution can never be optimal<sup>1</sup> at all code rates.

Motivated by this, we propose novel rateless codes, hereby referred to as reconfigurable rateless codes that are capable of not only varying the block length (and thus the rate) but also adaptively modify their encoding strategy according to the channel conditions. We will demonstrate that the proposed rateless codes are capable of shaping their own degree distribution according to near-instantaneous requirements imposed by the channel, but without the actual channel knowledge at the transmitter.

The remainder of the paper is structured as follows. Section II introduces the channel and the rateless coding scheme that were taken into consideration. The analysis of the proposed reconfigurable rateless codes and their adaptive incremental degree distribution is further detailed in Section III. Our simulation results are then presented in Section IV, while our concluding remarks are offered in Section V.

## **II. SYSTEM OVERVIEW**

### A. Channel Model

The canonical discrete-time complex baseband-equivalent channel model used is given by  $y_i = hx_i + n_i$ , where  $x_i$ ,  $y_i \in \mathbb{C}$  and  $n_i \sim C\mathcal{N}(0, 2\sigma_n^2)$  denotes the transmitted signal (i.e. the modulated codeword bit  $c_i$ ), the received signal and the complex additive white Gaussian noise (AWGN), respectively, at any transmission instant *i*. We consider a *quasistatic* fading (QSF) channel having a time-invariant channel gain *h* generated according to a complex circularly symmetric Gaussian distribution having a per-dimension noise variance of  $\sigma_n^2$ . This represents a non-frequency selective channel having a coherence time  $\tau$  that is higher than the system's maximum affordable codeword length determining the maximum system delay.

The instantaneous received SNR  $\overline{\psi}$  associated with a particular channel realization h is then given by  $\overline{\psi} := E_s |h|^2 / 2\sigma_n^2$  where  $E_s$  and  $|h|^2$  represent the constant energy-per-symbol and the fading power coefficient, respectively. The average received SNR is then given by:

$$\psi_{\text{avg}} := \frac{E_s \mathcal{E}(|h|^2)}{2\sigma_n^2} = \frac{E_s \mathcal{E}(|h|^2)}{N_0},\tag{1}$$

where  $\mathcal{E}(\cdot)$  denotes the expectation operator and  $N_0$  represents the two-dimensional noise variance. We note furthermore that all the attributes considered throughout this paper are computed with respect to  $N_0$  and not to  $\sigma_n^2$ . The achievable rate supported by the arbitrary channel gain h is defined as  $C(h) := \log_2(1 + \overline{\psi})$  bits per channel use.

The most commonly used performance metric for transmission over QSF channels is the outage probability defined as the likelihood of using an insufficiently low code-rate  $R_i$ , which is above the channel's capacity. This is formulated as  $\operatorname{Pr}_{\operatorname{out}}(\overline{R}_i) = \operatorname{Pr}(\overline{R}_i > C(h))$ , where  $\overline{R}_i$  has the same definition given in Section I. Therefore, given a fixed-rate code of rate  $R_x$ , there exist a fading coefficient h such that  $Pr_{out}(R_x)$  is non-zero. This also explains the reason why the design of fixed-rate error correction codes contrived for the QSF channels is significantly different than that constructed for the AWGN channel. Fixed-rate channel coding is capable of averaging out the effects of additive noise, but cannot counteract that of deep fades corresponding to low values of C(h). On the other hand, the outage probability  $Pr_{out}(R)$ of a rateless scheme may tend to zero independent of the channel conditions, since the (effective) code-rate R is actually

<sup>&</sup>lt;sup>1</sup>In this context, we use the adjective 'optimal' in terms of attaining a near-capacity performance.

determined by the decoder (and not the encoder), when the decoding is terminated after correctly decoding a. Therefore, rateless coded transmissions over the QSF channel can be modeled as AWGN channels having an effective SNR equal to  $\psi_{\rm avg}$ .

### B. Proposed Rateless Coding Scheme

The proposed rateless coding scheme is illustrated in Figure 1. The rateless encoder performs the four steps succinctly described below:

- 1) (Degree Selection) Randomly choose a degree  $d_c$  from a degree distribution  $\delta_i(x)$  supplied by the degree distribution selector;
- 2) (*Input bit/s Selection*) Randomly choose  $d_c$  input bits from the information bit sequence  $\mathbf{a} = (a_1, a_2, \dots, a_K)$  having the least number of connections at the current transmission instant;<sup>2</sup>
- 3) (Intermediate bit calculation) Calculate the value of the intermediate (check) bit  $b_q$ , q = 1, ..., N, by combining the  $d_c$  input bits selected at the previous step using modulo-2 addition;
- 4) (*Codeword bit calculation*) Determine the value of the codeword bit c<sub>q</sub> by:

$$c_q = b_q \qquad q = 1,$$
  
=  $b_q \oplus c_{q-1} \quad q = 2, \dots, N,$  (2)

where  $\oplus$  represents the modulo-2 addition operation. The degree distribution selector located at the transmitter will be simply denoted by  $DDS_T$ . We also note that the complexity of this rateless encoding process described in the above steps is linear in the block length.

Continuing the analogy we have drawn between rateless and fixed-rate codes in Section I-A, the degree distribution  $\delta_i(x)$  would then correspond to what is commonly referred to as the check node distribution. We will assume that all the (check) degree values of the degree distribution can represented by  $\mathbf{d}^i$ , where  $d_c \in \mathbf{d}^i$ . Accordingly, the probability generating function  $\delta_i(x)$  can be represented by means of a polynomial distribution given by:

$$\delta_i(x) := \sum_{\forall d_c \in \mathbf{d}^i} \delta_{d_c} x^{d_c - 1},$$
$$= \delta_1 + \delta_2 x + \ldots + \delta_{d_c} x^{d_c - 1} + \ldots + \delta_{D_c} x^{D_c - 1}, \qquad (3)$$

where the positive coefficients  $\delta_{d_c}$ ,  $d_c \in \mathbf{d}^i$  denote the particular fraction of intermediate bits (or check nodes) of degree  $d_c$  and  $D_c = \max(\mathbf{d}^i)$ . The variable or information node distribution can then be represented by:

$$v_i(x) := x^{d_v^i - 1}, (4)$$

which is regular due to the second step in the encoding procedure described above.

<sup>2</sup>This step can be readily carried out by means of storing the number of events that each specific information bit index has been selected up to the current transmission instant. By randomly selecting  $d_c$  input bits from those information bits that have the lowest number of connections at the current transmission instant, we aim for ensuring that each information bit will more-or-less have the same pre-defined degree.



Fig. 1. The proposed rateless coding scheme. The parameter  $\psi_i$  denotes to what we refer to as the channel quality estimate at transmission instant *i*. Perfect channel knowledge is assumed at the receiver and so,  $\psi_i$  represents the true estimate of the channel quality. On the other hand, the transmitter does not posses any channel state information and therefore  $\hat{\psi}_i$  can only be an optimistic guess of  $\psi_i$ . However, the transmitter can still incrementally improve its estimate by observing the feedback channel output (please refer to Section III-B). It is also implicitly assumed that there is another subsidiary DDS located at the receiver, namely DDS<sub>R</sub>, that can replicate the EXIT chart calculation and thus communicate the distributions  $\delta_i(x)$  and  $v_i(x)$  to the rateless decoder (please refer to Section III-A).

Similarly to [6], we assume that the transmitter and the receiver have synchronized clocks used for the seed of their pseudorandom number generators, and therefore the degree  $d_c \in \mathbf{d}^i$  as well as the specific modulo-2 connections selected by both the transmitter and the receiver are identical. In order to provide further insights, below we highlight the differences between the rateless encoding technique presented above and the LT encoding method proposed by Luby (*cf.* Section 1.1 in [6]):

- The aim of the degree distribution selector is to select (or compute online) an 'appropriate' degree distribution for reconfigurable rateless codes. The degree distribution selector is not required in the previously proposed rateless codes, such as the LT and Raptor codes, since the degree distribution is predetermined and fixed.
- 2) In LT codes, the d<sub>c</sub> information bits are selected uniformly at random, hence the actual degree d<sub>v</sub> attributed to each information bit can be modeled as a random variable V, V ~ π(λ), where π(λ) denotes the Poisson distribution with parameter λ. Therefore, the variable node distribution of the LT codes can be well approximated by:

$$v_{\rm LT}(x) \approx \pi(\lambda) = \sum_{d_v=1}^{N} \frac{e^{-\lambda} \lambda^{d_v}}{d_v!} x^{d_v - 1},$$
(5)

with parameter  $\lambda$  defined by  $\lambda := d_{c,avg} \frac{N}{K}$ , where K and N are assumed to be asymptotically large. The average check node degree  $d_{c,avg}$  is then given by:

$$d_{\mathrm{c,avg}} := \sum_{\forall d_c \in \mathbf{d}} \delta_{d_c} \cdot d_c. \tag{6}$$

This implies that some rows of the LT code generator matrix have a low weight with a non-negligible probability, thus resulting in codes that exhibit high error floors due to their poor distance properties. Furthermore, the variable node distribution  $v_{LT}(x)$  represented in (5) is effectively a function of the block length,<sup>3</sup> of the number of information bits as well as of the degree distribution of the LT code,  $\delta_{LT}(x)$ . In our system, having such

<sup>&</sup>lt;sup>3</sup>As it was mentioned in Section I, the block length of a rateless code is increasing at every transmission instant, until the receiver acknowledges the fact that  $\hat{\mathbf{a}} = \mathbf{a}$ . Therefore, the dependency of  $v_{\rm LT}(x)$  on the block length suggests that there exist a different  $v_{\rm LT}(x)$  at every transmission instant.

dependencies would have presented a problem, hence this issue will be further elaborated on in Section III-B. On the other hand, the variable node distribution  $v_i(x)$ of the proposed rateless codes represented by (4) does not exhibit these dependencies. This results from the second step in our encoding method described above.

3) The potential error floor of LDGM codes may be mitigated by their serial concatenation with another code, which is typically another LDGM code [20]. Motivated by this, we have added a fourth step of the rateless encoding procedure outlined at the beginning of this section, which essentially represents a unity-rate precoder (or accumulator).

In this light, the proposed codes can be considered as precoded LT codes,<sup>4</sup> or instances of "rateless repeataccumulate (RA)" codes. Establishing this relationship between fixed-rate and rateless codes will significantly simplify our forthcoming analysis, since we can conveniently model the proposed reconfigurable rateless codes as non-systematic RA codes.

#### **III. SYSTEM DESCRIPTION**

The next subsections detail the technique that enables the proposed reconfigurable rateless codes to adapt their encoding strategy (and thus modify their configuration) in order to better match the prevalent channel conditions. This enhanced adaptivity of reconfigurable rateless codes is attributed to what we refer to as the degree distribution selector ( $DDS_{T}$ ). Up to this point in time, the  $DDS_T$  of Figure 1 was treated as a black box capable of calculating the degree distribution  $\delta_i(x)$  online by observing the feedback channel's output. In Section III-A, we will simplify our analysis by temporarily assuming that the  $DDS_T$  of Figure 1 is equipped with perfect channel knowledge and thus is capable of determining the optimal degree distribution that facilitates a near-capacity performance. This assumption is then discarded in Section III-A, where we only assume having perfect channel state information at the receiver. From Section III-B onwards, the  $DDS_T$  of Figure 1 will only be able to monitor the ACKs received from the feedback channel.

#### A. Analysis Under Simplified Assumptions

In this sub-section, we will stipulate the following simplifying assumptions: (a) perfect channel knowledge is available at both the receiver as well as at the transmitter; (b) the rateless decoder is not bounded in terms of its complexity and (c) the decoder is capable of detecting<sup>5</sup> whether the decoded  $\hat{\mathbf{a}} = \mathbf{a}$ .

Using the fixed-rate versus rateless code analogy introduced in the previous sections, the rateless decoder of Figure 1 is constituted of two decoders separated by a uniform random interleaver, where the inner decoder is the amalgam of a memory-one trellis decoder used for the accumulator and of a check node decoder (CND), whilst the outer decoder is



Fig. 2. The fraction of check nodes of degree  $d_c \in \mathbf{d}^i$ ,  $\delta_{d_c}$ , with  $i \ge 0$ , calculated by the  $DDS_T$  of Figure 1 under the assumptions detailed in Section III-A. The degree distribution  $\delta_0(x)$  is covering the SNR values ranging from 15 to approximately 5 dB. Note that we have purposely reversed the abscissa axis in order to underline the *optimistic* philosophy adopted by the  $DDS_T$  (please refer to Section III-B.)

a variable node decoder (VND). We will assume that the interleavers have sufficiently high girth to ensure that the non-negligible correlations between the extrinsic log-likelihood ratios do not have a severe impact on the decoder.

The convergence behavior of this iterative rateless decoding process can then be analyzed in terms of the evolution of the input and output mutual information exchange between the inner and outer decoders in consecutive iterations, which is diagrammatically represented using the semi-analytical tool of EXIT charts [5]. There are three requirements to be satisfied in order to design a near-capacity system; (a) both the inner as well as the outer decoder's EXIT curves should reach the (1,1) point on the EXIT chart; (b) the inner decoder's curve  $I_{ACC\&CND}$  should always be above the outer decoder's curve  $I_{VND}$  and (c) the  $I_{ACC\&CND}$  curve has to match the shape of the  $I_{VND}$  curve as accurately as possible, thus resulting in an infinitesimally low EXIT-chart-tunnel area. There exists a direct relationship between the two EXIT curves corresponding to the check and variable node distribution, as represented by (3) and (4) respectively.

Given the distributions  $v_i(x)$  and  $\delta_i(x)$  of (3) and (4), the two EXIT curves correspond to two EXIT functions formulated by [5]:

$$I_{E,VND}(I_{A,VND}, d_v^i) = J\left(\sqrt{(d_v^i - 1)} \cdot J^{-1}(I_{A,VND})\right),$$
(7)

where the function  $J(\cdot)$  denotes the mutual information,  $I_{E,VND}(I_{A,VND}, d_v^i)$  represents the extrinsic information output of the VND as a function of the its *a-priori* information input  $I_{A,VND}$  and its variable node degree  $d_v^i$ . Similarly, the combined accumulator and CND EXIT function  $I_{E,ACC\&CND}(\cdot)$  is then approximated by (8) as explained in [5], where  $I_{A,CND}$  represents the a-priori information input of the CND and the extrinsic information accumulator output is denoted by  $I_{E,ACC}(I_{A,ACC})$ , where  $I_{A,ACC}$  denotes the

<sup>&</sup>lt;sup>4</sup>In our case, the intermediate bit  $b_i$  will be identical to the LT encoded bit, given that  $\delta_i(x) = \delta_{\text{LT}}(x)$  and  $v_i(x) = v_{\text{LT}}(x)$ .

<sup>&</sup>lt;sup>5</sup>This can be easily achieved by either appending a short cyclic redundancy check (CRC) to the original bit sequence **a**, which imposes a negligible ratepenalty as  $K \to \infty$ .

a-priori accumulator information input. The parameter  $\Delta_{d_c}^i$  corresponds to the specific fraction of edges emanating from the intermediate bits (or check nodes) of degree  $d_c \in \mathbf{d}^i$  given by  $\Delta_{d_c}^i = \delta_{d_c} \cdot \frac{d_c}{d_{c,avg}}$  and the average check node degree  $d_{c,avg}$  is defined in (6). Furthermore, we note that designing the two EXIT curves determines the two distributions and vice versa.

Consider the scenario of having binary phase-shift keying (BPSK) modulation transmissions over the BIAWGN channel characterized by SNRs ranging from -10 to 15 dB. If the  $DDS_T$  of Figure 1 possesses perfect channel knowledge, then it is capable of computing online the decoder's EXIT curves that satisfy the above three requirements, and from which we can determine the distributions  $\delta_i(x)$  and  $v_i(x)$ . The result of this experiment is portrayed in Figure 2, which shows particular fraction of check nodes of degree  $d_c$ ,  $\delta_{d_c}$ , that characterize the degree distribution  $\delta_i(x)$  across the range of SNR values considered. It can be observed from Figure 2 that the characteristics of the degree distribution  $\delta_i(x)$  across this range of SNRs are so distinctively dissimilar, which also highlights the inadequacy of a rateless codes having a fixed degree distribution in the face of time-variant SNRs. For example, the check degrees  $d_c > 2$  are the dominant degrees at high channel SNR values, whilst they are almost extinct when the channel quality is poor. Furthermore, we note that at low channel SNR values, the system reduces to a simple repetition code,<sup>6</sup> with the exception of a very small percentage of nodes having  $d_c = 100$ .

We emphasize that a non-systematic rateless coding scheme was preferred over its systematic counterpart in order to completely eliminate the dependency of the variable node distribution on the channel condition. This can also be verified from (7). By doing so, the channel dependency has been confined to only one of the two distributions; i.e. to  $\delta_i(x)$ corresponding to the  $I_{ACC\&CND}$  EXIT curve. However, the outer decoder's EXIT curve  $I_{VND}$  will now emerge from the (0,0) point of the EXIT chart and hence a certain percentage of degree-one check nodes  $\delta_{d_1}$  is always required in order to force the  $I_{ACC\&CND}$  curve to emerge from a higher initial value than the  $I_{VND}$  curve and thus guarantee that the iterative decoder begins to converge.<sup>7</sup> This percentage of doped check nodes  $\delta_{d_1}$  is also dependent on the channel quality, but the optimal IACC&CND curve is channel-quality dependent anyway.

# B. The Adaptive Incremental Degree Distribution Without Idealized Assumptions

In this subsection, we will no longer assume perfect channel state information at the transmitter, but only a single-bit ACK transmitted by the receiver on the feedback channel in a similar fashion to that used in incremental redundancy aided [15] schemes. We were particularly interested in finding the answer as to whether it is possible to design a variable incremental degree distribution, that attempts to imitate the attributes of the optimal channel-state dependent one. From another point of view, this question can be restated as to whether it is possible for the  $DDS_T$  to estimate the inner decoder's EXIT curve  $I_{ACC\&CND}$ , so that near-capacity performance is guaranteed, regardless of the channel conditions encountered. Once the  $I_{ACC\&CND}$  EXIT curve is computed, the degree distribution  $\delta_i(x)$  can be readily calculated and passed on to the rateless encoder. Hence there is a need for encoders having the capability of "thinking like decoders" before encoding.

Against this backdrop, we introduce what we refer to as the adaptive incremental distribution. The DDS<sub>T</sub> of Figure 1 is initialized by making a conjecture of the channel quality. For example, the initial estimate  $\hat{\psi}_0$  provided for the DDS<sub>T</sub> of Figure 1 can be set to the highest SNR considered, i.e. 15 dB, in an attempt to maximize the achievable throughput. However, it can be observed from Figure 2 that the rateless decoder should still be able to successfully decode  $\hat{a} = a$  using the same distribution  $\delta_0(x)$ , even if the receiver experiences an SNR of as low as 5 dB. Therefore, the estimate  $\hat{\psi}_0$  can be set to the latter value. Then, the rateless encoder employs the degree distribution  $\delta_0(x)$  designed for a code having a rate of 0.9681, which is given by  $\delta_0(x) = 0.0007 + 0.6781x + 0.1156x^2 + 0.1358x^4 + 0.0386x^5 + 0.0235x^{20} + 0.0077x^{99}$ and  $v_0(x) = x^3$ .

As it was already alluded to in Section III, the  $DDS_T$  is continuously observing the feedback channel output and must try its utmost to glean as much information as possible from it. While it is plausible that the simple ACK feedback is less beneficial than having complete channel knowledge, the ACK as well as the absence of the ACK can still prove to be useful for the  $DDS_T$  to improve the estimate of  $\hat{\psi}_0$ . Recall from Section III-A, that if  $DDS_T$  posses a precise estimate of the channel quality, then the problem is basically solved since the  $DDS_T$  is capable for calculating the specific degree distribution that achieves a performance arbitrarily close to capacity.

To elaborate further, it can be argued that the absence of a received ACK may indicate two options for the  $DDS_T$ ; either that the estimate of  $\psi_0$  is correct but the rateless decoder is unsuccessful in correctly decoding a due to using an insufficient number of iterations or  $\psi_0$  is representing an overly optimistic estimate of the channel conditions. We note that the first possibility must not to be completely neglected, especially when considering that the EXIT curves corresponding to the two distributions are closely matched in an attempt to maximize the achievable throughput and therefore a considerable number of iterations is necessary. If this occurs, then transmitting some additional redundant bits may make up for the limited number of affordable iterations. Thus we pay a rate-penalty in exchange for a lower computational complexity. On the other hand, if the  $DDS_{T}$  of Figure 1 has an incorrect estimate of the channel condition and thus no ACK has been received, two further possibilities might have occurred. Namely, the rateless decoder may have either started the decoding but was unsuccessful or else it did not even attempt to decode the received codeword, because  $\overline{R} < C(h)$ . The pictorial representation of all these possible scenarios is illustrated in Figure 3.

Since the SNR range considered is quite wide, we assume that the most likely cause of failure is feeding the  $DDS_T$ 

<sup>&</sup>lt;sup>6</sup>At very low SNRs, a high percentage of doped check nodes  $\delta_{d_1}$  is required in order to lift the  $I_{ACC\&CND}$  EXIT curve at a higher position than that of the  $I_{VND}$  EXIT curve.

<sup>&</sup>lt;sup>7</sup>This technique is sometimes referred to as code doping and was first proposed by Brink in [5].

$$I_{E,ACC\&CND}(I_{A,CND}, \mathbf{d}^{i}, \psi_{\text{avg}}) \approx \sum_{\forall d_{c} \in \mathbf{d}^{i}} \Delta_{d_{c}}^{i} \left[ 1 - J \left( \sqrt{(d_{c} - 1) \cdot \left[ J^{-1} (1 - I_{A,CND}) \right]^{2} + \left[ J^{-1} (1 - I_{E,ACC} (I_{A,ACC})) \right]^{2}} \right) \right] (8)$$



Fig. 3. The decision tree for the encoding strategy used by the  $\mathrm{DDS}_\mathrm{T}$  of Figure 1.

with an inaccurate  $\hat{\psi}_0$  and so, a modification of the encoding strategy (thus a modification of the degree distribution  $\delta_0(x)$ and  $v_0(x)$ ) is required. Therefore, if an ACK is still not received after transmitting according to the degree distribution  $\delta_0(x)$ , then the DDS<sub>T</sub> of Figure 1 can reasonably assume that its next estimate is  $\hat{\psi}_1 \leq 5$  dB. This can be verified from Figure 2, which demonstrates that  $\delta_0(x)$  is the optimal distribution up to an SNR of about 5 dB. The immediate problem that has to be tackled by the DDS<sub>T</sub> is that of calculating an improved degree distribution  $\delta_1(x)$  for the improved estimate  $\hat{\psi}_1$ , given that the previous distribution was  $\delta_0(x)$ . This can be viewed as an optimization problem, i.e. given that having an unsuccessful  $\delta_i(x)$  was attributed to the inaccurate channel quality estimate  $\hat{\psi}_i$ , the next degree distribution  $\delta_{i+1}(x)$  can be determined by:

$$\delta_{i+1}(x) = \max \sum_{\forall d_c \in \mathbf{d}^{i+1}} \frac{d_c}{\Delta_{d_c}^{i+1}} \tag{9}$$

subject to the equality constraint

$$\sum_{\forall d_c \in \mathbf{d}^{i+1}} \Delta_{d_c}^{i+1} = 1 \tag{10}$$

and to the *inequality constraints* given by

$$I_{E,ACC\&CND}(\mathcal{I}, \mathbf{d}^{i+1}, \hat{\psi}_{i+1}) > I_{A,VND}(\mathcal{I}, d_v^{i+1}),$$
(11)

and

$$\Delta_{d_c}^{i+1}|_{\forall d_c \in (\mathbf{d}^{i+1} \setminus \mathbf{d}^i)} > 0, \tag{12}$$

where  $\mathbf{d}^{i+1}$  contains all the parity-check degree values of the next degree distribution  $\delta_{i+1}(x)$ ,  $\mathbf{d}^i \subseteq \mathbf{d}^{i+1}$ , and  $\hat{\psi}_{i+1} < \hat{\psi}_i$ is the new channel quality estimate. In (11),  $\mathcal{I}$  is a discrete set of gradually increasing values in the interval [0, 1] over which the functions  $I_{E,ACC\&CND}(\cdot)$  and  $I_{A,VND}(\cdot) = I_{E,VND}^{-1}(\cdot)$ (please refer to (8) and (7)) are calculated. The specific value of  $d_v^{i+1}$  is selected by considering the smallest variable node degree value that satisfies both  $d_v^{i+1} > d_v^i$  as well as (11). We further note that the maximization of the objective function in (9) is equivalent to maximizing the code-rate.

An important step to consider is that the newly calculated

degree distribution  $\delta_{i+1}(x)$  must take into account the previous  $\delta_i(x)$ , since the bits connected to the degrees  $d_c \in \mathbf{d}^i$  coined from  $\delta_i(x)$  have already been transmitted and thus will still affect the rateless decoding. Due to this, we introduce an additional inequality constraint, in addition to that given by (11) and (12), expressed by:

$$\Delta_{d_c}^{i+1}|_{\forall d_c \in (\mathbf{d}^i \cap \mathbf{d}^{i+1})} > \frac{d_{\mathbf{v}}^i}{d_{\mathbf{v}}^{i+1}} \cdot \Delta_{d_c}^i.$$
(13)

The adaptive incremental distribution denoted by  $\delta_{adap}(x, \hat{\psi})$  employed by the proposed reconfigurable rateless codes instead of a fixed one can be formulated as:

$$\delta_{\text{adap}}(x,\hat{\psi}) := \delta_0(x) \mathbf{1} \left\{ \hat{\psi} \ge \hat{\psi}_0 \right\} + \delta_1(x) \mathbf{1} \left\{ \hat{\psi}_0 > \hat{\psi} \ge \hat{\psi}_1 \right\} + \ldots + \delta_z(x) \mathbf{1} \left\{ \hat{\psi}_{z-1} > \hat{\psi} \ge \hat{\psi}_z \right\},$$
(14)

where the DDS<sub>T</sub> channel quality estimate is  $\hat{\psi} \in (\hat{\psi}_0, \hat{\psi}_1, \dots, \hat{\psi}_z)$  and where  $\mathbf{1} \{\cdot\}$  denotes the indicator function returning a value of one, if the argument is true, and zero otherwise. As a further example, the next incremental distribution  $\delta_1(x)$  (and  $\upsilon_1(x)$ ) determined by relying on the distribution  $\delta_0(x)$ , is calculated by solving the linear programming problem outlined in (9)-(13), which leads to  $\delta_1(x) = 0.0010 + 0.6400x + 0.1375x^2 + 0.1281x^4 + 0.0364x^5 + 0.0188x^7 + 0.0023x^8 + 0.0221x^{20} + 0.0138x^{99}$  and  $\upsilon_1(x) = x^4$ .

In conclusion, the adaptive incremental distribution  $\delta_{adap}(x, \hat{\psi})$  would then correspond to the particular degree distribution that yields the  $Pr_{out}$  tending to zero. From (14), we also note that in contrast to the conventional rateless codes, the reconfigurable rateless codes adapt their communication strategy by shaping their degree distribution in order to better match the rate requirements imposed by the channel quality encountered. Furthermore, it can be readily demonstrated that the more promptly the  $DDS_T$  estimates the channel quality, the more accurately the adaptive incremental degree distribution  $\delta_{adap}(x, \hat{\psi})$  matches the optimal distribution derived using the idealized assumptions presented in III-A.

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Fig. 4. Average throughput (bits/channel use) versus SNR (dB) for the proposed reconfigurable rateless codes as well as for Raptor codes for transmission using BPSK modulation over the quasi-static fading channel. The rateless decoder was limited to a maximum of 200 iterations.

#### **IV. SIMULATION RESULTS**

The results presented in this section were obtained using BSPK modulation, when transmitting over QSF channels. We compared our results to both Raptor codes as well as to punctured regular and irregular LDPC codes. The Raptor code [11] was constructed as in [19] by serially concatenating a regular LDPC outer code described by a PCM having a column weight of 3 and a row weight of 30 and thus realizing a rate-0.9 code. This LDPC code was then concatenated with a non-systematic LT code having a fixed degree distribution given by  $\delta_{\rm LT}(x) = 0.05x + 0.5x^2 + 0.05x^3 + 0.25x^4 + 0.05x^4$  $0.05x^6 + 0.1x^8$  [19]. On the other hand, the proposed reconfigurable rateless codes employ an adaptive incremental degree distribution  $\delta_{adap}(x, \psi)$  represented in (14), which were initialized with the distributions  $\delta_0(x)$  and  $v_0(x)$ . The number of information bits K to be recovered was set to 9,500 bits and the incremental redundancy segment used for both schemes was set to 100 bits.

Figure 4 illustrates the exhibited average throughput performance versus the SNR for the proposed reconfigurable rateless codes. It can be observed that the proposed codes achieve a performance within approximately 1 dB of the discrete-input continuous-output memoryless channel's (DCMC) capacity across a diverse range of SNRs. Furthermore, it can be verified that the performance exhibited by the reconfigurable rateless codes is superior to that of the Raptor code for all SNRs higher than -4 dB. For example, at -3 dB and 0 dB, the proposed codes require on average 560 and 730 less redundant bits than the corresponding Raptor benchmarker code. On the other hand, Raptor codes excel at low SNR, and are suitable candidates to be used for signaling when the channel quality may become very poor [19].

The excellent performance exhibited by the proposed rateless reconfigurable codes at medium-to-high SNRs can be explained by their optimistic philosophy in calculating the channel quality estimate. The higher the average received SNR, the faster it is for the  $DDS_T$  to estimate the channel



Fig. 5. Average throughput (bits/channel use) versus SNR (dB) for the proposed reconfigurable rateless codes with respect to the maximum allowable number of iterations, assuming BPSK modulation transmission over the quasistatic fading channel.

quality and the more accurate the adaptive incremental degree distribution becomes. The effect is actually reversed, when the received SNR is very low, since the adaptive incremental degree distribution  $\delta_{adap}(x, \psi) = \delta_z(x)$  employed in this case is still taking into effect the previous distributions  $\delta_u(x)$ , for all  $0 \ge y < z$ , that were used to transmit a fraction of N bits, when the  $DDS_T$  had an optimistic channel quality estimate  $\psi_{y}$ . The effect of previous distributions  $\delta_{y}(x)$ , for all  $0 \ge y < z$  on the adaptive incremental degree distribution  $\delta_{\text{adap}}(x,\hat{\psi}) = \delta_z(x)$  is that of introducing a slight EXIT curve matching inaccuracy, thus resulting in a wider open tunnel between the two decoder's EXIT curves. However, this effect is beneficial in terms of reducing the maximum number of iterations required. In fact, it can be verified from Figure 5 that reducing the maximum number of allowable iterations from 200 to 30 resulted in a negligible throughput loss in the low-SNR region.

Soljanin *et al.* in [19] demonstrated that in the high-SNR region, the performance exhibited by punctured LDPC codes is superior to that of Raptor codes. Therefore, it was of interest to verify, whether the performance of punctured LDPC codes is also superior to that exhibited by the proposed rateless reconfigurable codes. We have considered the same scenario as in [19], i.e. used a high-rate regular LDPC code such as the previously described rate-0.9 outer LDPC code employed for the Raptor code as well a rate-0.8 LDPC code having a PCM of column-weight 3 and row-weight 15. We also considered a half-rate irregular LDPC code having a variable node distribution given by  $v(x) = 0.2199x + 0.2333x^2 + 0.2333x^2$  $0.0206x^3 + 0.0854x^4 + 0.0654x^6 + 0.0477x^7 + 0.0191x^8 +$  $0.0806x^{18} + 0.2280x^{19}$  and a check node distribution represented by  $\delta(x) = 0.6485x^7 + 0.3475x^8 + 0.0040x^9$ , where both distributions were optimized using density evolution [4].

Our performance comparison in terms of the average throughput (bits/channel use) versus SNR (dB) over the BI-AWGN channel between the proposed reconfigurable rateless



Fig. 6. Average throughput (bits/channel use) performance for transmission over the BIAWGN channel versus SNR (dB) using the proposed reconfigurable rateless codes as well as for the incremental-redundancy-based HARQ schemes employing punctured regular LDPC codes having R = 0.8 and 0.9 and an optimized [4] punctured half-rate irregular LDPC code. The rateless decoder was limited to a maximum of 200 iterations. The number of information bits used for all the simulated schemes was set to 9,500 bits.

codes as well as the incremental-redundancy-based HARQ schemes using punctured regular and irregular LDPCs is illustrated in Figure 6. It is demonstrated in Figure 6, that the performance of the proposed reconfigurable rateless codes is also superior to that of punctured regular and irregular LDPC codes.

#### V. SUMMARY AND CONCLUDING REMARKS

In this paper, we have proposed novel reconfigurable rateless codes, that are capable of not only varying the block length but also adaptively modify their encoding strategy according to the channel conditions. We have argued that the state-of-the-art rateless codes employ a fixed degree distribution; i.e. the degree distribution used for coining the degree  $d_c$  for each transmitted bit is time invariant and thus channel-independent. Consequently, such rateless codes can only alter the number of bits transmitted in order to cater for the variations of the channel conditions. However, it was also demonstrated that the optimal degree distribution, i.e. the distribution that has the ability to realize a near-capacity code is actually channel-quality dependent. We have then analyzed how the characteristics attributed to optimal channelquality controlled degree distributions depended on the channel conditions. Against this backdrop, we have proceeded to design what we referred to as an adaptive incremental degree distribution, which allowed the transmitter to imitate the attributes of the optimal channel-state dependent degree distributions across a diverse range of channel SNRs. The main difficulty is related to the fact that the transmitter has to operate blindly, i.e. calculate a distribution that reproduces the characteristics of the channel-quality dependent one without the knowledge of the channel. The only information available to the transmitter is a single-bit ACK feedback.

The transmitter starts by making an optimistic guess of

the channel quality, denoted by  $\hat{\psi}_0$ , in an attempt to maximize the achievable throughput. Following this,  $\overline{N}_0$  bits are transmitted using a degree distribution  $\delta_0(x)$  optimized for the hypothesized estimate  $\psi_0$ . If an acknowledgment is still not received after this first transmission, the transmitter can improve the previous channel quality estimate  $\psi_0$ , by making a improved conjecture  $\hat{\psi}_1$ , where  $\hat{\psi}_1 < \hat{\psi}_0$ . Based on the new estimate  $\hat{\psi}_1$  and by exploiting the knowledge that the previous  $N_0$  bits were transmitted using an (inappropriate) distribution  $\delta_0(x)$ , the transmitter can calculate a new distribution  $\delta_1$  that is optimized for achieving a near-capacity performance. From another perspective, the transmitter has to calculate a new distribution  $\delta_1(x)$  that will still maintain an infinitesimallysmall but open EXIT tunnel between the inner and outer decoder curves, given that the previous distribution was  $\delta_0(x)$ . Our method is therefore reminiscent of what is referred to as EXIT chart matching, however it is now applied in the context of rateless codes and therefore must also be performed "onthe-fly".

In this sense, the proposed rateless codes are capable of shaping their own degree distribution<sup>8</sup> according to requirements imposed by the channel and without the availability of the channel state information at the transmitter. A reconfigurable rateless code was characterized for transmission of 9500 information bits over quasi-static fading channels and achieves a performance that is approximately 1 dB away from the DCMC capacity over a diverse range of channel SNR ratios.

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