## Adaptive Simulated Annealing for Designing Finite-Precision PID Controller Structures

S. Chen<sup>†</sup>, R.H. Istepanian<sup>†</sup>, J.F. Whidborne<sup>‡</sup> and J. Wu<sup>§</sup>

† Department of Electrical and Electronic Engineering University of Portsmouth, Anglesea Building Portsmouth PO1 3DJ, U.K. schen@ee.port.ac.uk istepanr@ee.port.ac.uk

> ‡ Department of Mechanical Engineering King's College London, Strand London WC2R 2LS, UK james.whidborne@kcl.ac.uk

§ Institute of Industrial Process Control Zhejiang University Hangzhou, 310027, P.R. China jwu@iipc.zju.edu.cn

## Abstract

Many control applications pose optimisation problems with multimodal and nonsmooth cost functions. Gradient methods are ineffective in these situations. The adaptive simulated annealing (ASA) offers a viable optimisation tool for tackling these difficult constrained optimisation problems. We demonstrate the effectiveness of the ASA using an application, designing finite-precision PID controller structures with maximum stability robustness measure. The sparseness issue of controller structures is also discussed, and it is shown that the ASA can cope with this kind of constraints easily.

## 1 Introduction

Optimisation problems with multimodal and nonsmooth cost functions are commonly encountered in control applications. Gradient-based algorithms are ineffective in these applications due to the problem of local minima or the difficulty in calculating gradients. Optimisation methods that require no gradient and can achieve a global optimal solution offer considerable advantages in solving these difficult optimisation problems. Two classes of such global optimisation methods are the genetic algorithm (GA) [1]–[3] and the simulated annealing (SA) [4]–[6]. While the GA seems to have attracted considerable attention (e.g. [7]–[9]), the SA by contrast has not received similar interests.

The SA is an optimisation technique with some strikingly positive and negative features. An attractive feature of SA is that it is very easy to program and the algorithm typically has few

parameters that require tuning. A serious drawback of SA is that the standard SA can be very slow, often requiring much more number of cost-function evaluations to converge, compared with a carefully designed and tuned GA. The ASA [10]–[14], also known as the very fast simulated reannealing, overcomes this drawback by using a much faster annealing schedule and adopting a reannealing scheme to adapt itself. The algorithm also maintains all the advantages of standard SA algorithms.

Controller implementations with fixed-point arithmetic offer the advantages of speed, memory space, cost and simplicity over floating-point arithmetic [15]. However, a designed stable closed-loop system may become unstable when the infinite-precision controller is implemented using a fixed-point processor due to finite-word-length (FWL) effects. This poses the problem of finding an optimal controller realization, which has a maximum tolerance to round-off error, by maximizing a stability robustness measure [16],[17]. For the PID controller structure, the problem can be solved as an optimisation problem with four variables [18],[19]. However, the optimisation criteria are nonsmooth and nonconvex functions. This offers an ideal testing case for applying the ASA.

It is desirable that a controller realization has a sparse structure, namely containing many elements of 0, 1 and -1. A true optimal controller realisation with a maximum stability bound is a fully parameterized structure and usually destroys the sparse structure. A sparse structure is particularly important for high-order controllers. Although a PID controller is a low-order one, we use it to illustrate that sparseness requirement can be imposed as simple constraints and the ASA can cope with these constraints easily.

## References

- J.H. Holland, Adaptation in Natural and Artificial Systems. Ann Arbor, MI.: University of Michigan Press, 1975.
- [2] D.E. Goldberg, Genetic Algorithms in Search, Optimization, and Machine Learning. Reading, MA.: Addison-Wesley, 1989.
- [3] L. Davis, Ed., Handbook of Genetic Algorithms. Van Nostrand Reinhold, 1991.
- [4] S. Kirkpatrick, C.D. Gelatt Jr. and M.P. Vecchi, "Optimization by simulated annealing," Science, Vol.220, No.4598, pp.671-680, 1983.
- [5] A. Corana, M. Marchesi, C. Martini and S. Ridella, "Minimizing multimodal functions of continuous variables with the simulated annealing algorithm," ACM Trans. Mathematical Software, Vol.13, No.3, pp.262-280, 1987.
- [6] P.J.M. van Laarhoven and E.H.L. Aarts, Simulated Annealing: Theory and Applications. Dordrecht, Netherlands: D. Reidel, 1987.
- [7] A.J. Chipperfield and P.J. Fleming, "Gas turbine engine controller design using multiobjective genetic algorithms," in *Proc. GALESIA*'95 (Sheffield, UK), Sept.12-14, 1995, pp.214-219.

- [8] K.S. Tang, K.F. Man and D.W. Gu, "Structured genetic algorithm for robust  $H^{\infty}$  control system design," *IEEE Trans. Industrial Electronics*, Vol.43, No.15, pp.575-582, 1996.
- [9] K.F. Man, K.S. Tang, S. Kwong and W.A. Halang, Genetic Algorithms for Control and Signal Processing. Advances in Industrial Control. London: Springer, 1997.
- [10] L. Ingber and B. Rosen, "Genetic algorithms and very fast simulated reannealing: a comparison," Mathematical and Computer Modelling, Vol.16, No.11, pp.87-100, 1992.
- [11] L. Ingber, "Simulated annealing: practice versus theory," Mathematical and Computer Modelling, Vol.18, No.11, pp.29-57, 1993.
- [12] L. Ingber, "Adaptive simulated annealing (ASA): lessons learned," J. Control and Cybernetics, Vol.25, No.1, pp.33-54, 1996.
- [13] B.E. Rosen, "Rotationally parameterized very fast simulated reannealing," submitted to IEEE Trans. Neural Networks, 1997.
- [14] S. Chen, B.L. Luk and Y. Liu, "Application of adaptive simulated annealing to blind channel identification with HOC fitting," *Electronics Letters*, Vol.34, No.3, pp.234-235, 1998.
- [15] M.K. Masten and I. Panahi, "Digital signal processors for modern control systems," Control Eng. Practice, Vol.5, No.4, pp.449-458, 1997.
- [16] G. Li and M. Gevers, "On the structure of digital controllers in sampled data systems with FWL consideration," in Proc. 35th IEEE Conf. Decision and Control (Kobe, Japan), 1996, pp.919-920.
- [17] R.H. Istepanian, G. Li, J. Wu and J. Chu, "Analysis of sensitivity measures of finite-precision digital controller structures with closed-loop stability bounds," *IEE Proc. Control Theory and Applications*, accepted for publications, 1998.
- [18] J. Wu and R.H. Istepanian, "Stability issues of finite precision PID controller structures for sampled data systems," submitted to Int. J. Control, 1997.
- [19] R.H. Istepanian, J. Wu, J. Chu and J.F. Whidborne, "Maximizing lower bound stability measure of finite precision PID controller realizations by nonlinear programming," in *Proc.* 1998 American Control Conf. (Philadelphia, USA), 1998, pp.2596-2600.
- [20] Y. Hori, "A review of torsional vibration control methods and a proposal of disturbance observer-based new techniques," in Proc. 13th IFAC World Congress (San Francisco, USA), 1996, pp.7-13.
- [21] G. Ami and U Shaked, "Small roundoff realization of fixed-point digital filters and controllers," IEEE Trans. Acoustics, Speech, and Signal Processing, Vol.36, No.6, pp.880-891, 1988.
- [22] G. Li, "On the structure of digital controllers with finite word length consideration," IEEE Trans. Automatic Control, Vol.43, No.5, pp.689-693, 1998.

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