

UNIVERSITY OF
Southampton

Gravity seminar

Quark-hadron continuity
under rotation

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Based on the work

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Continuity of vortices from the hadronic to the color-flavor locked phase in dense matter

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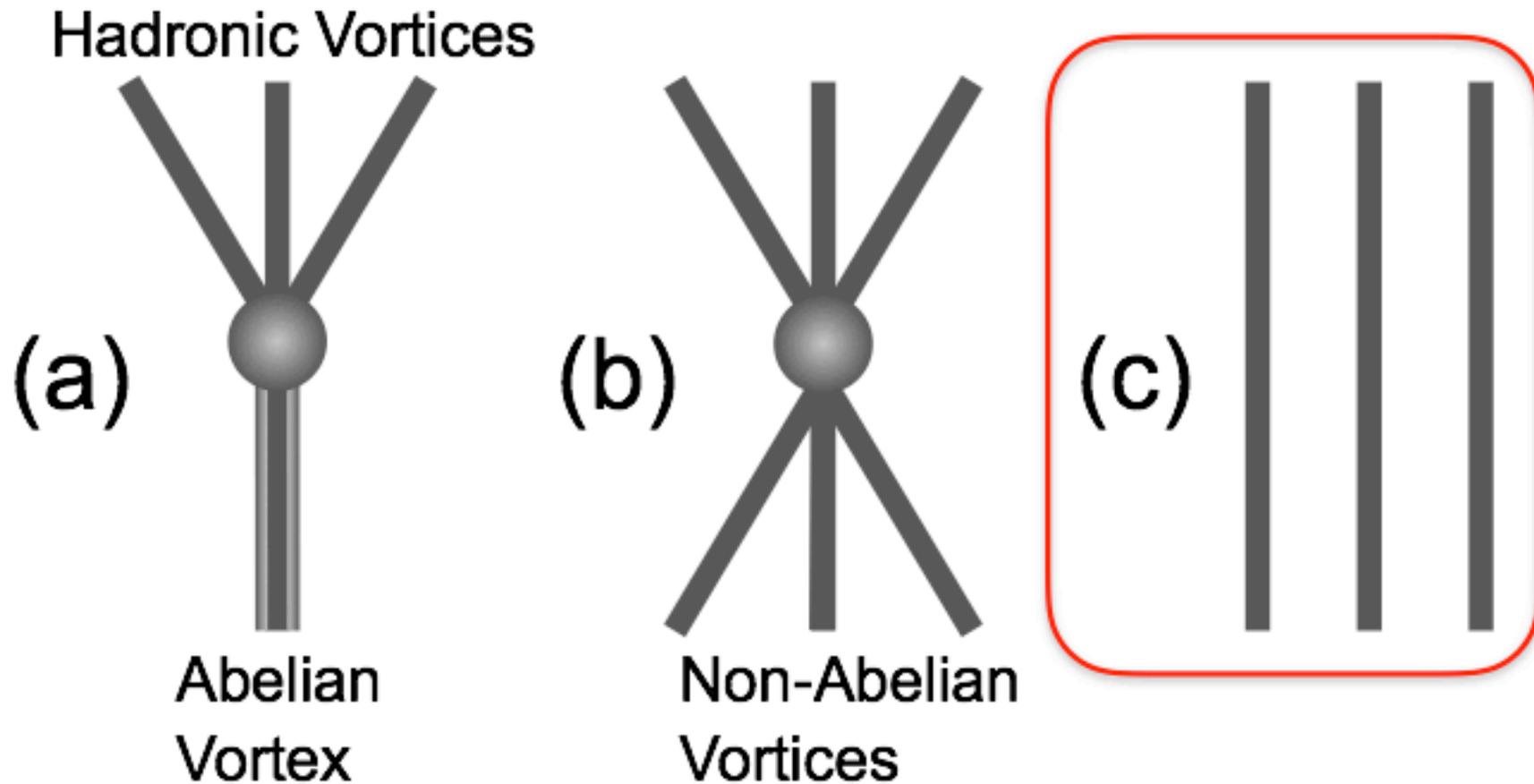


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We study how vortices in dense superfluid hadronic matter can connect to vortices in superfluid quark matter, as in rotating neutron stars, focusing on the extent to which quark-hadron continuity can be maintained. As we show, a singly quantized vortex in three-flavor symmetric hadronic matter can connect smoothly to a singly quantized non-Abelian vortex in three-flavor symmetric quark matter in the color-flavor locked phase, without the necessity for boojums appearing at the transition.

Question

Non-Abelian CFL vortices ~ Hadronic vortices



Physics = Fertile research arena of Matters and Space-time

- ★ What matters are made of?
- ★ How matters are created and change in different conditions?
- ★ How the universe was born and will be?

Approaches: **Experiment**, **Observation**,
Theory, **Computer**

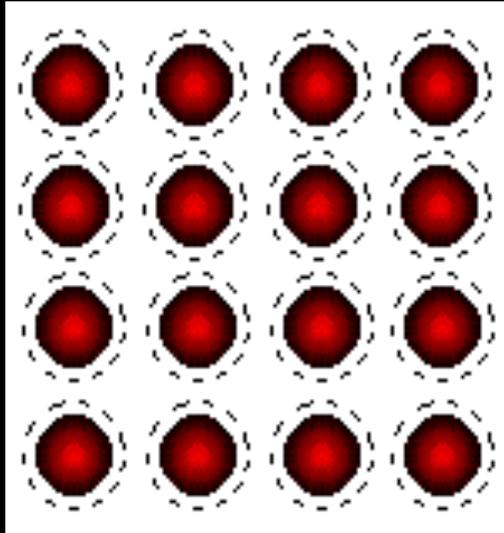
A child-like question:

What happens to matter
as we squeeze it harder and harder,
and/or make it hotter and hotter?

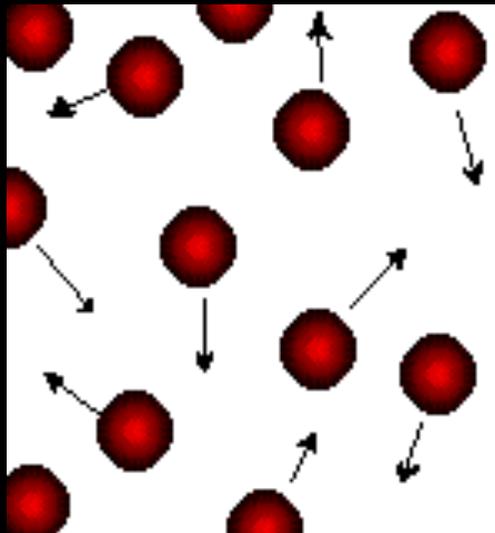


Phases of Matter

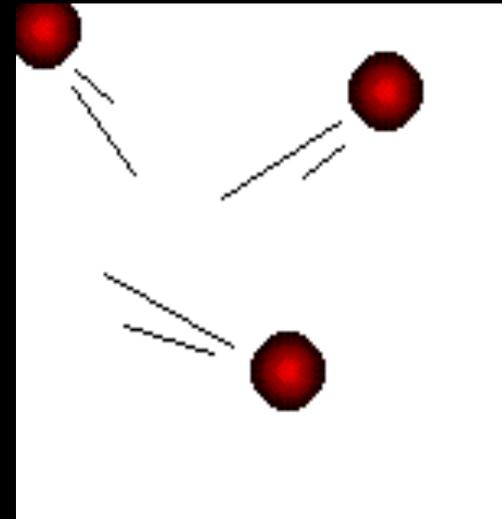
Ex.) H₂O



Solid(ice)



Liquid(water)

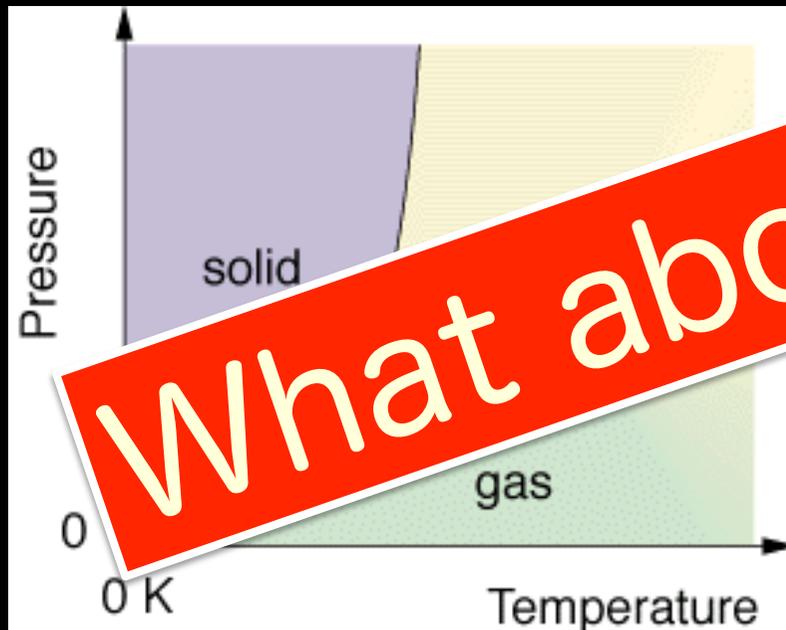


Gas(vapor)

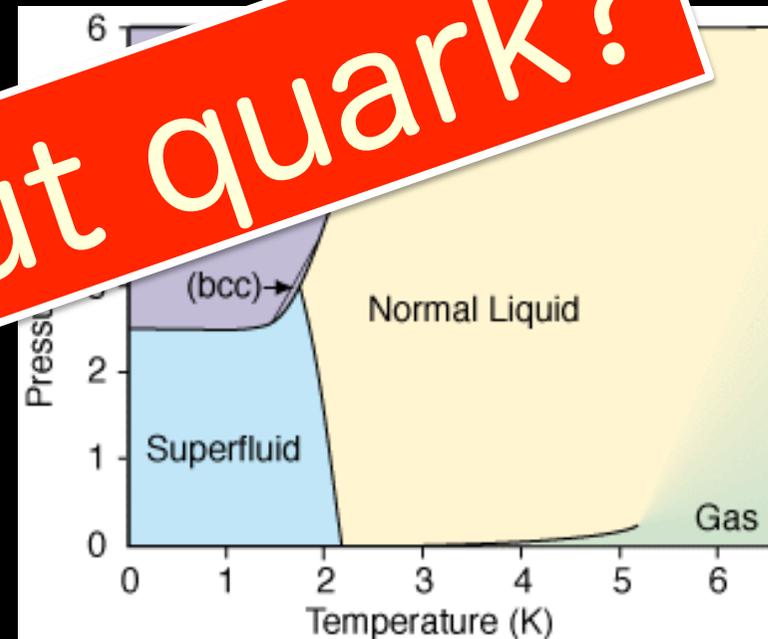
T, P

Phase diagrams

H_2O



$4He$



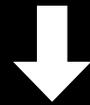
What about quark?

<http://boojum.hut.fi/research/theory/typicalpt.html>

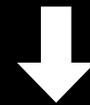
Convention

- ★ Phases are described by symmetries of underlying theory
- ★ What is the theory of quarks?
What are the symmetries?

Properties of
strongly-interacting matter



Quantum field theory
with Non-Abelian symmetry



Quantum Chromo Dynamics

QCD



QCD Lagrangian (Han-Nambu, 1965)



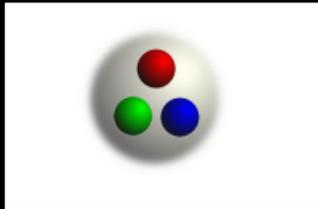
$$L_{QCD} = \bar{q}^{\alpha} \left(i\gamma_{\mu} D^{\mu} - m_q \right)_{\alpha\beta} q^{\beta} - \frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu}$$

Just one line, but very rich in physics and math

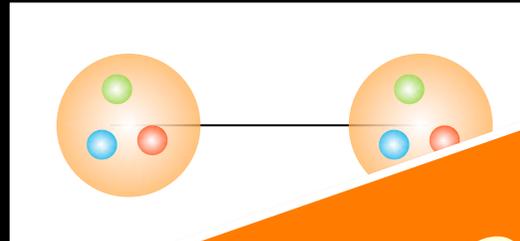
Yes! We love QCD ❤️
... kind of new ideas

Grand Challenge

- Space-time evolution of QCD matter -



Hadrons



Nuclear force

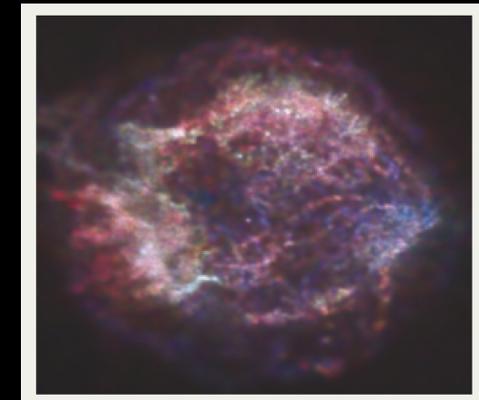
Nuclei



Early universe



Neutron/quark star



Supernovae

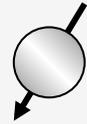
No QCD, no life

The answer to the ultimate question

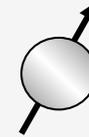
“Why the matter of our universe can be stable?”

■ Symmetries of QCD and their breaking patterns

Chiral basis :



$$q_L = \frac{1}{2}(1 - \gamma_5)q, \quad q_R = \frac{1}{2}(1 + \gamma_5)q$$



QCD Lagrangian :

$$\mathcal{L}_{\text{cl}} = \mathcal{L}_{\text{cl}}(q_L, A) + \mathcal{L}_{\text{cl}}(q_R, A) - (\bar{q}_L m q_R + \bar{q}_R m q_L)$$

classical QCD symmetry (m=0)

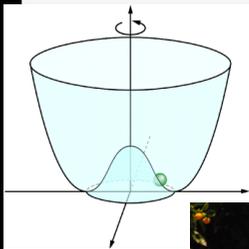
$$\mathcal{G} = SU(3)_C \times [SU(N_f)_L \times SU(N_f)_R] \times U(1)_B \times U(1)_A$$



Quantum QCD vacuum (m=0)

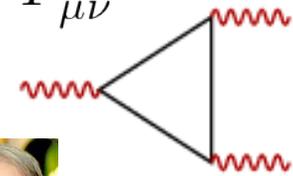
**Chiral condensate :
spontaneous mass generation**

**Axial anomaly :
quantum violation of $U(1)_A$**



$$\langle \bar{q}_R q_L \rangle \neq 0$$

$$\partial_\mu J_A^\mu = -2N_f \frac{\alpha_s}{8\pi} F_a^{\mu\nu} \tilde{F}_{\mu\nu}^a$$

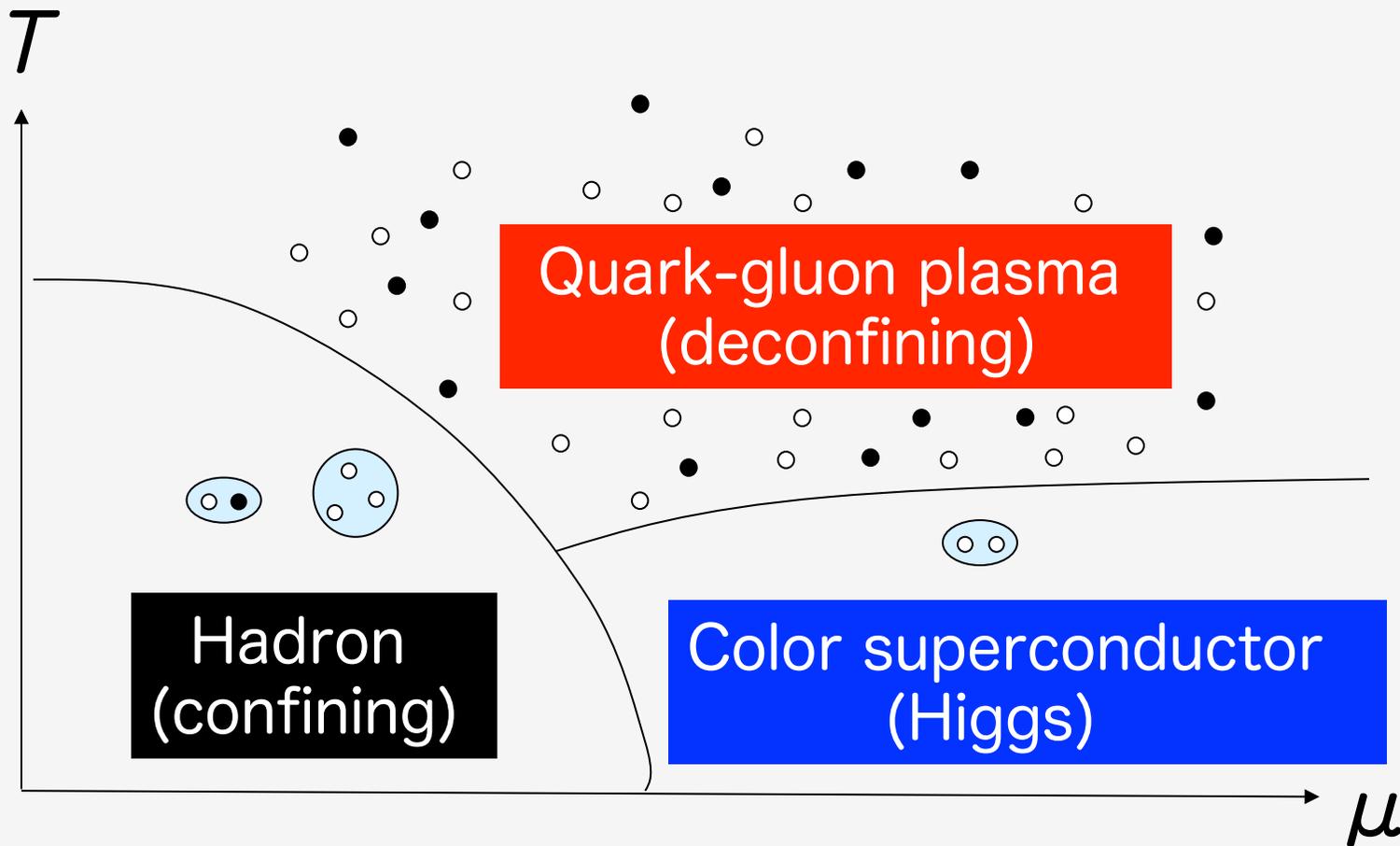


$$SU(3)_C \times SU(N_f)_{L+R} \times U(1)_B$$

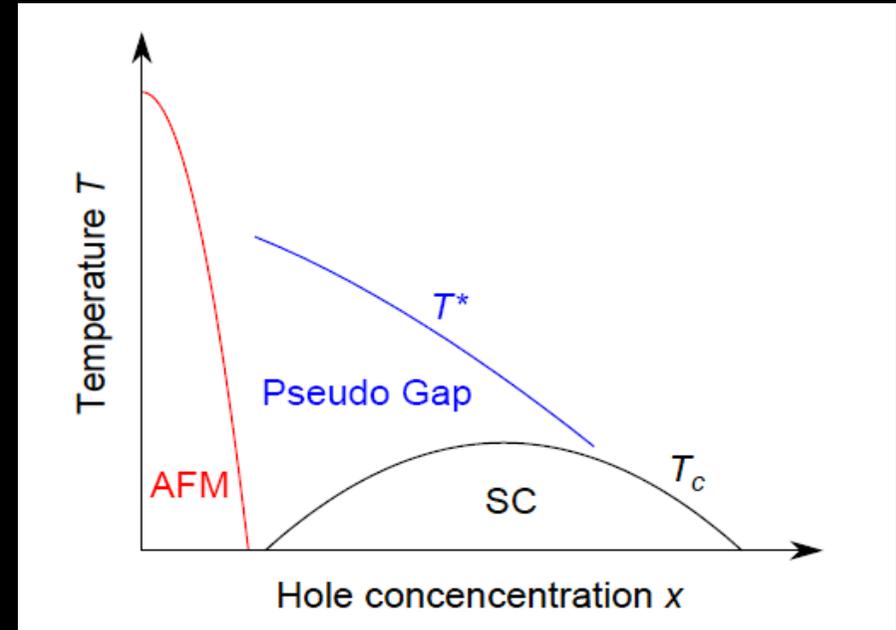
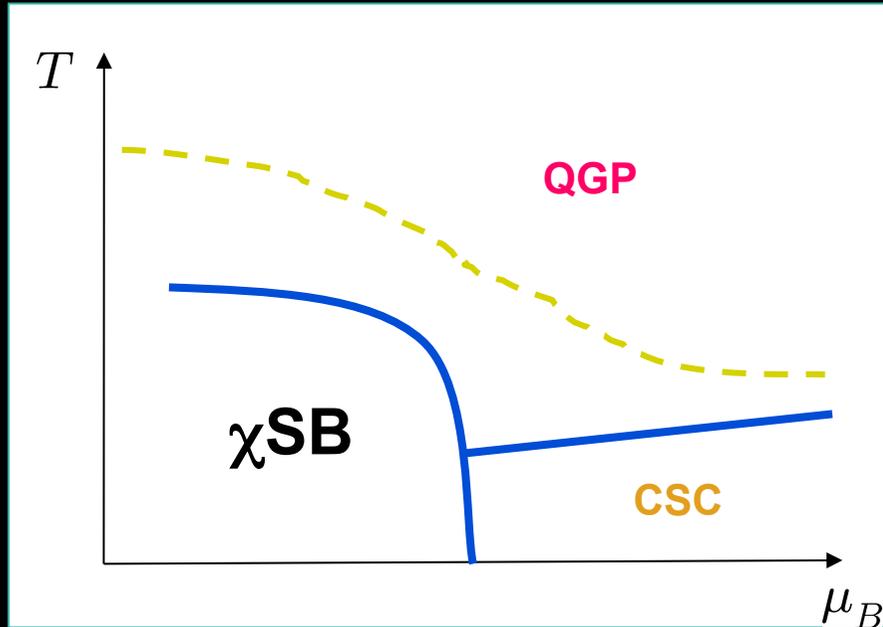


QCD phase diagram via Occam's razor

“Schematic phase diagram”



Similarity between QCD and High T_c Superconductor



Common features in QCD, HTS, and ultracold atoms

1. Competition among different orders
2. Strong coupling/correlation

Idea of Quark-Hadron continuity

hep-ph/9811473

3 flavor hadron matter
is smoothly connected to
a quark matter
as baryon density is increased

Impacts on NS physics?

Table of Quark-Hadron continuity

Phase	Hadronic (confinement)	Color-flavor locked(Higgs)
Symmetry breaking Pattern	$SU(3)_L \times SU(3)_R \times U(1)_B$ $\rightarrow SU(3)_{L+R}$	$SU(3)_L \times SU(3)_R \times SU(3)_C \times U(1)_B$ $\rightarrow SU(3)_{L+R+C}$
Order parameter	chiral condensate	diquak condensate
$U(1)_B$	broken in the dibaryon channels	broken by d
Elementary Excitations	Pseudo-scalar mesons (π etc)	NG bosons
	vector mesons (ρ etc)	massive gluons
	baryons	massive quarks (CFL gap)

A realization of Fradkin-Shenker complementarity

Diquark condensations

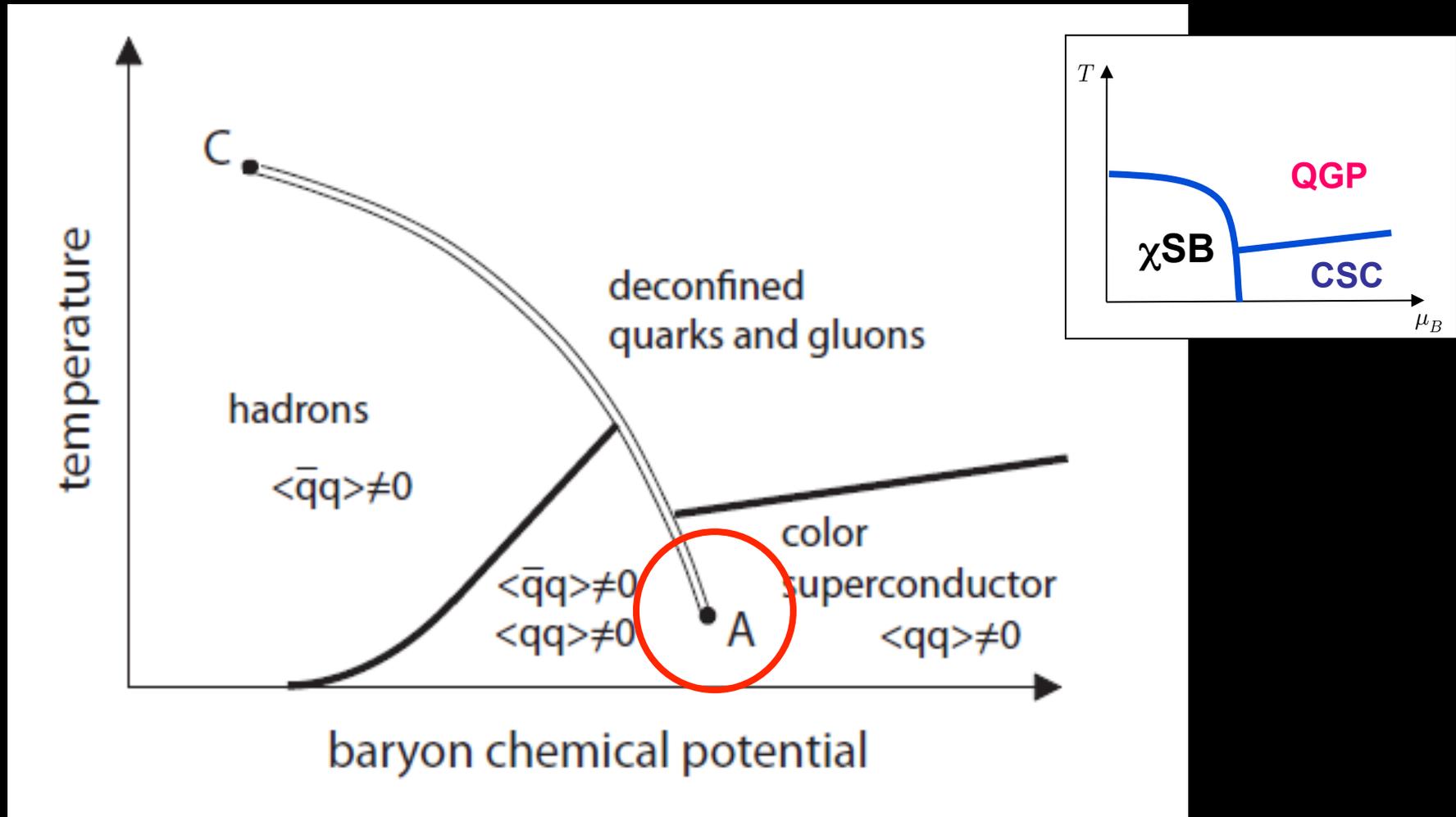
$N_f=2$ (2-flavor color superconductivity [2SC])

$$\langle q_{\alpha i} C \gamma_5 q_{\beta j} \rangle \propto \Delta_{2SC} \varepsilon^{\alpha\beta 3} \varepsilon^{ij}$$

$N_f=3$ (Color-flavor locking [CFL])

$$\langle q_{\alpha i} C \gamma_5 q_{\beta j} \rangle = \Delta_{CFL} \varepsilon_{\alpha\beta I} \varepsilon^{ijI} \propto \Delta_{CFL} \left(\delta_{\alpha}^i \delta_{\beta}^j - \delta_{\alpha}^j \delta_{\beta}^i \right)$$

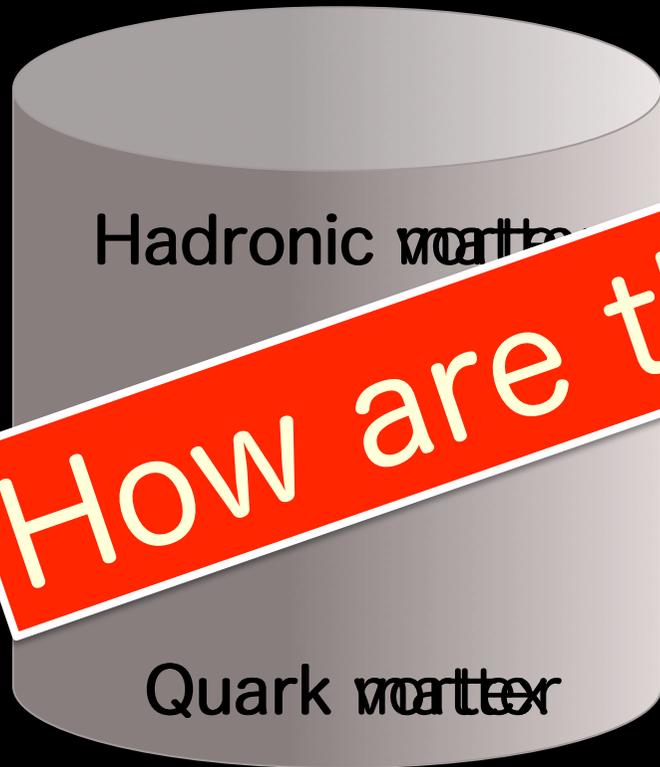
“Anomaly driven critical point in high density QCD as a realization of quark-hadron continuity”



Yamamoto, Hatsuda, Baym & Tachibana, PRL 97 ('06)

Thought experiment

Pour quarks
into



How are they connected?

Upper: Hadronic matter
Lower: Quark matter

Then, rotate the bucket

Upper: Hadronic vortex
Lower: Quark vortex

Notations

$$\Phi(\vec{r}, t) = |\Phi(\vec{r})| e^{i\phi(\vec{r}) - i\mu t} : \text{complex scalar}$$

$$\phi(\vec{r}, t) = p_\nu x^\nu = \vec{p} \cdot \vec{r} - \mu t, \quad \vec{v} = \frac{\vec{p}}{\mu}$$

$$C \equiv \oint_C \vec{v} \cdot d\vec{l} = 2\pi \frac{\nu}{\mu} \quad \nu : \text{winding \#}$$

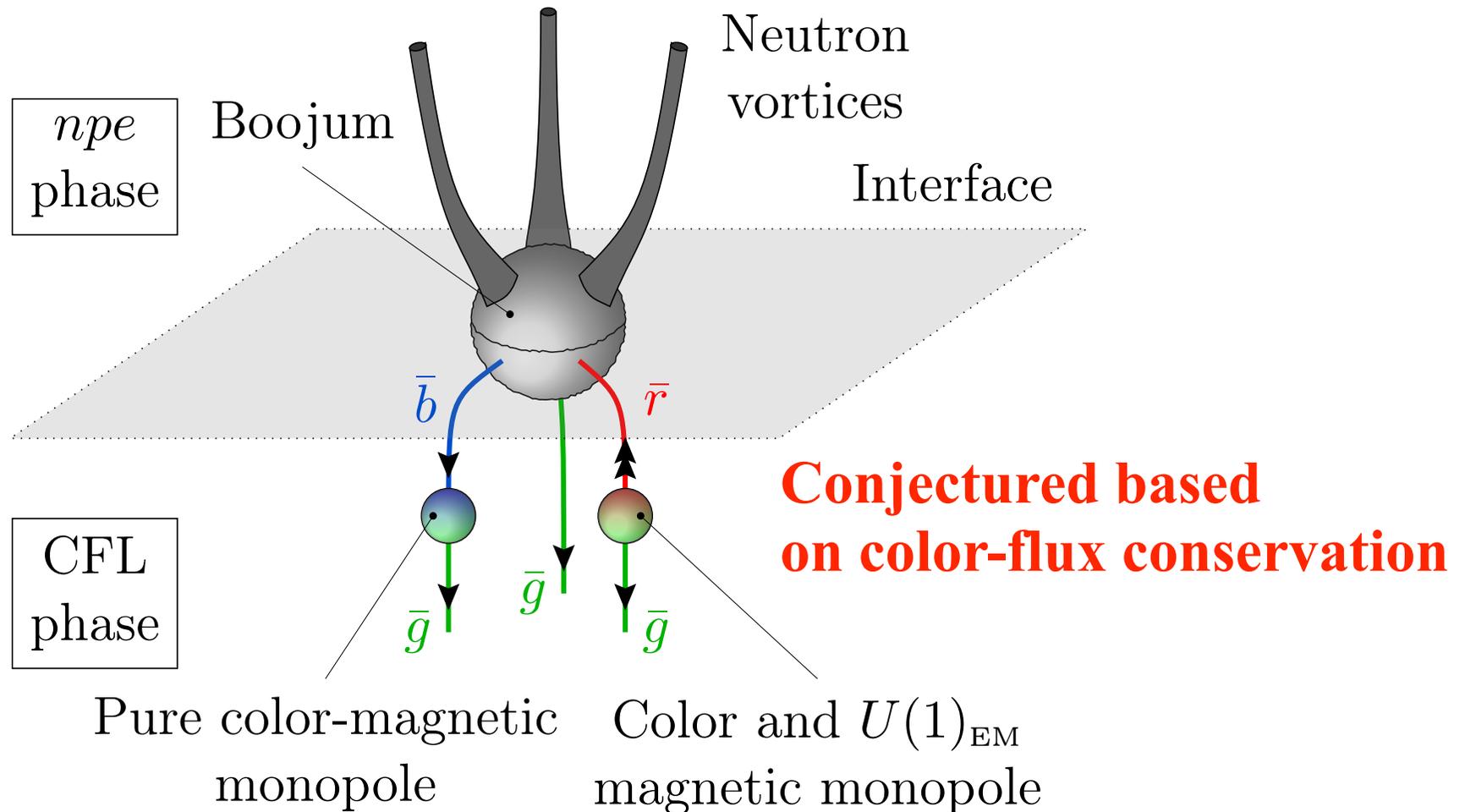
Circulation matching

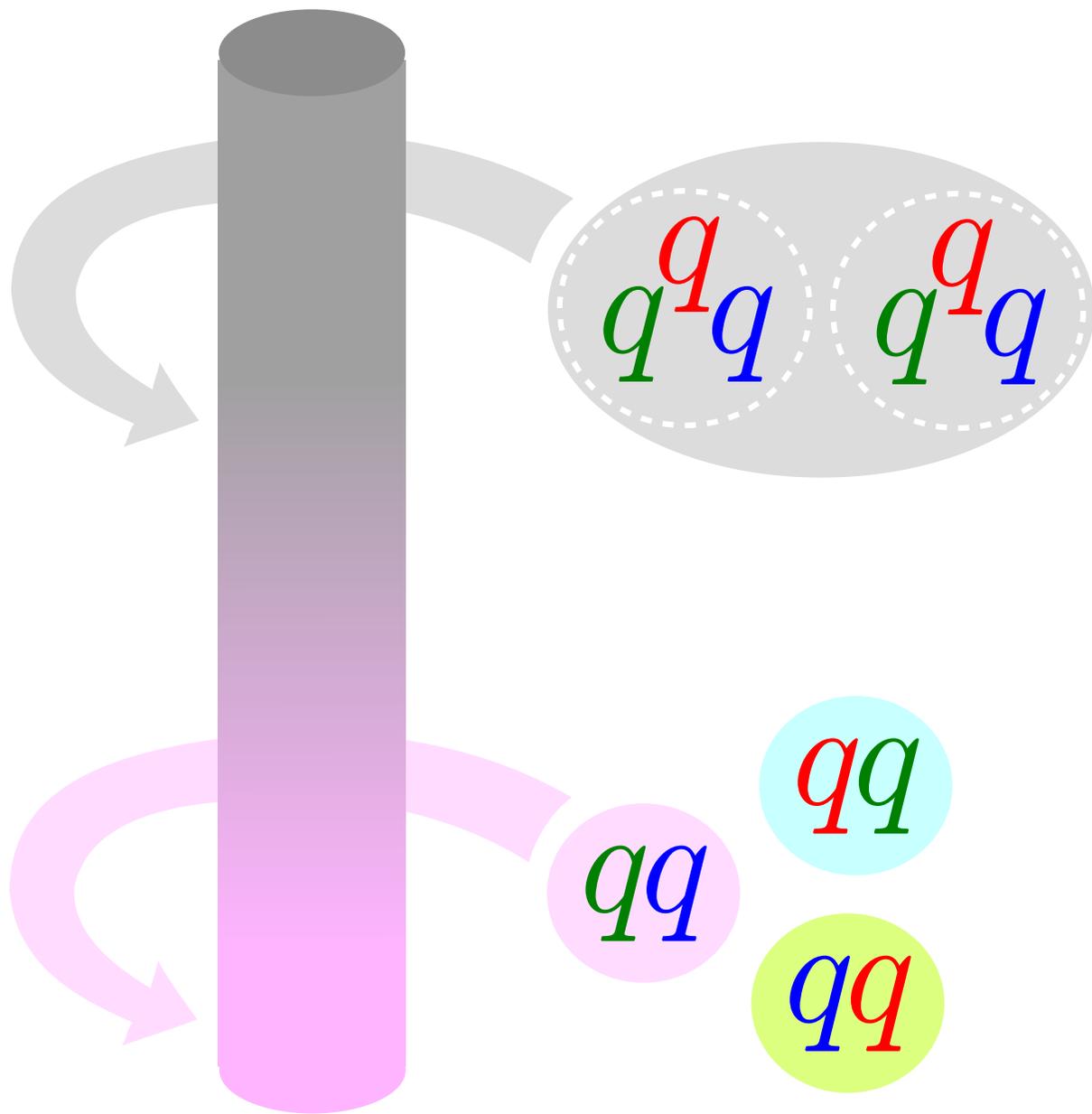


Boojum
(Wikipedia)

Non-Abelian CFL vortex

Cipiriani-Vinci-Nitta (2012)





Some more details

Color and flavor 3plet diquark order parameter

$$\hat{\Phi}^{\alpha i} \propto \varepsilon^{\alpha\beta\gamma} \varepsilon^{ijk} q_{\beta j} C \gamma_5 q_{\gamma k}$$

Φ diagonalized via color-flavor space rotation

$$\Phi = \begin{pmatrix} \Phi^{\bar{r}\bar{u}} & 0 & 0 \\ 0 & \Phi^{\bar{g}\bar{d}} & 0 \\ 0 & 0 & \Phi^{\bar{b}\bar{s}} \end{pmatrix}$$

Some more details

In this case,

$$C_{NA} = 2\pi \frac{\frac{1}{3} v_{NA}}{2\mu_q} = 2\pi \frac{v_{NA}}{2 \cdot 3\mu_q} = 2\pi \frac{v_{NA}}{2\mu_B}$$



$$v_H = v_{NA}$$

Some more details

What we (Alford *et al.*) discussed:

$$\begin{aligned}\hat{\Upsilon}^{ijk}(\vec{r}) &\equiv \frac{1}{6} \epsilon_{\alpha\beta\gamma} \hat{\Phi}^{\alpha i} \hat{\Phi}^{\beta j} \hat{\Phi}^{\gamma k} \\ &= \frac{1}{3} \epsilon^{kmn} (C\gamma_5)_{ab} \hat{B}_m^{i a} \hat{B}_n^{j b}\end{aligned}$$

6 quark objects = 3 diquarks = 2 baryons

Quantum numbers match

Non-Abelian vortices = Flavor singlet + Non-singlets
($\sim \Lambda\Lambda$)

Other topics

1. Flavor symmetry (breaking)

Flavor structure of vortices
(e.g. Neutron superfluidity)

MWHC theorem

2. Vortex interaction

Ginzburg-Landau analysis

Summary of today's talk

- ① Quark-hadron continuity hypothesis
(Fradkin/Shenker=Schafer/Wilczek)
- ② Study of superfluid vortices in light
of QH continuity
- ③ Possible applications of our findings

Thank you !

感謝！