

Revealing the Physics of R-modes in Low-Mass X-ray Binaries

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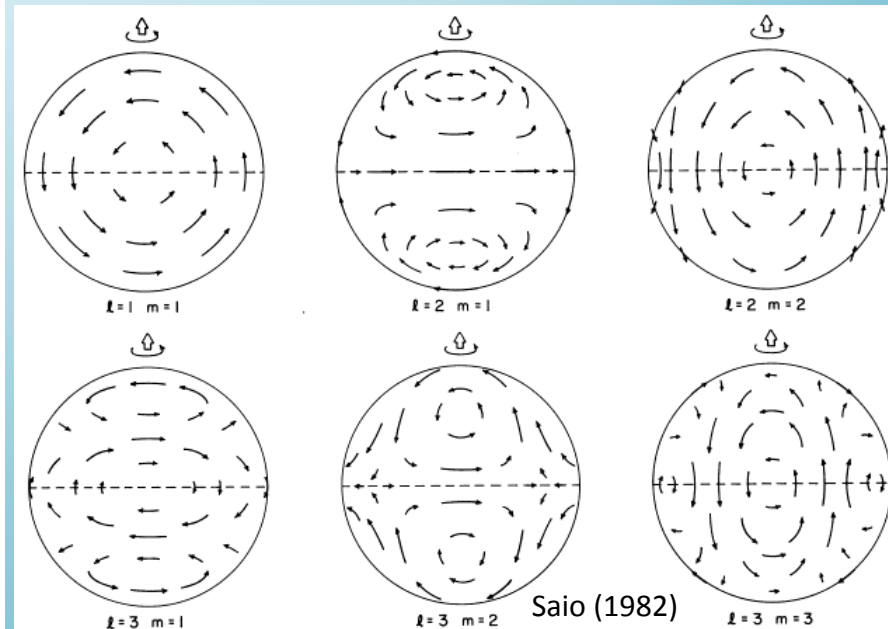
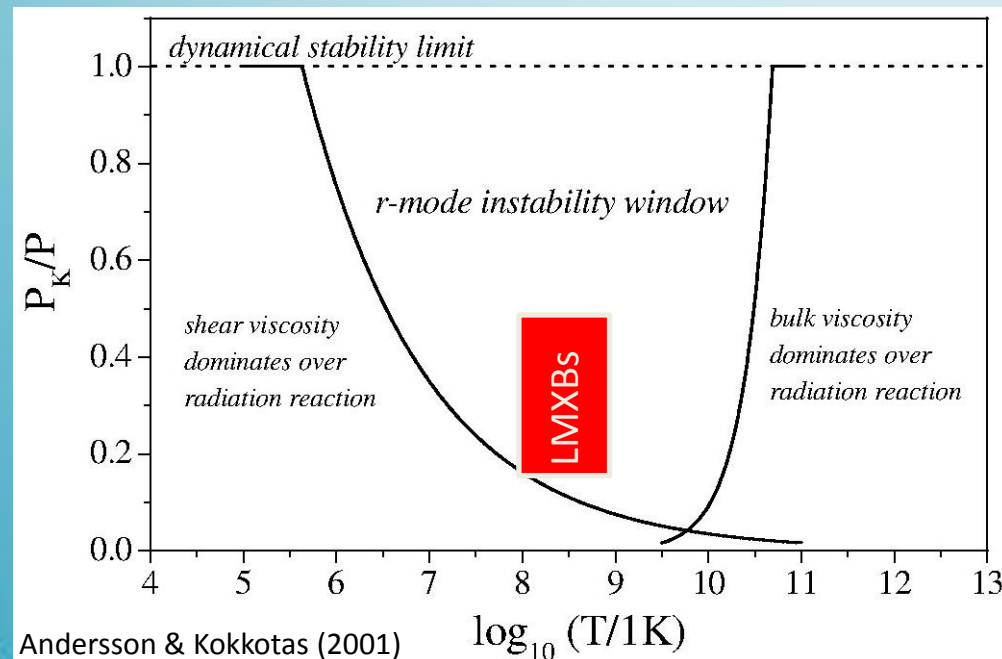
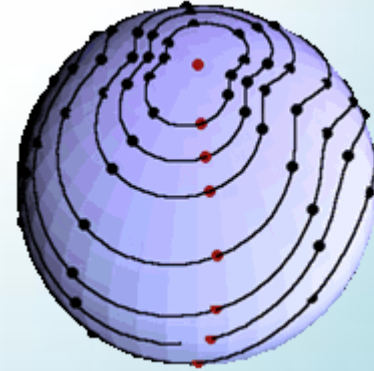
University of Michigan, USA

Brynmor Haskell

University of Amsterdam, Netherlands

R-mode Oscillations and Instability

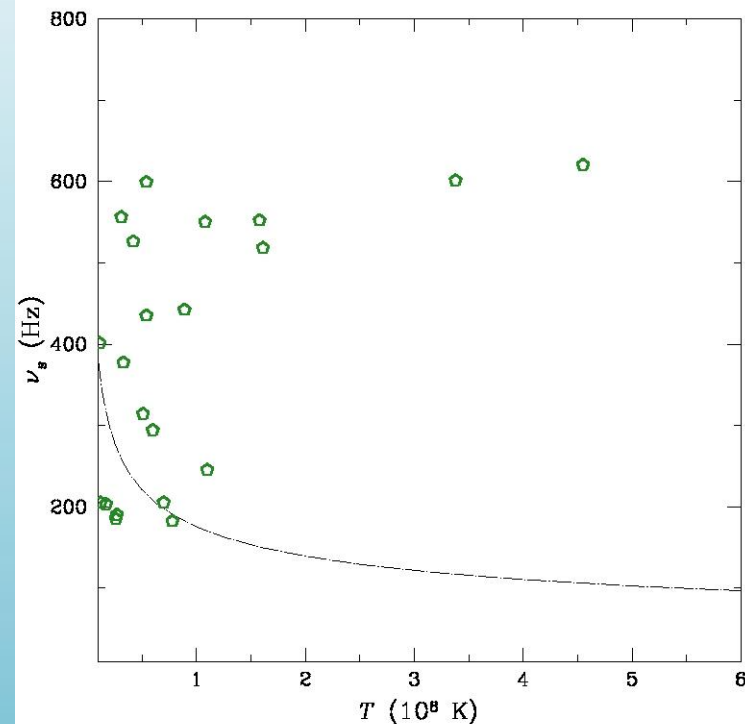
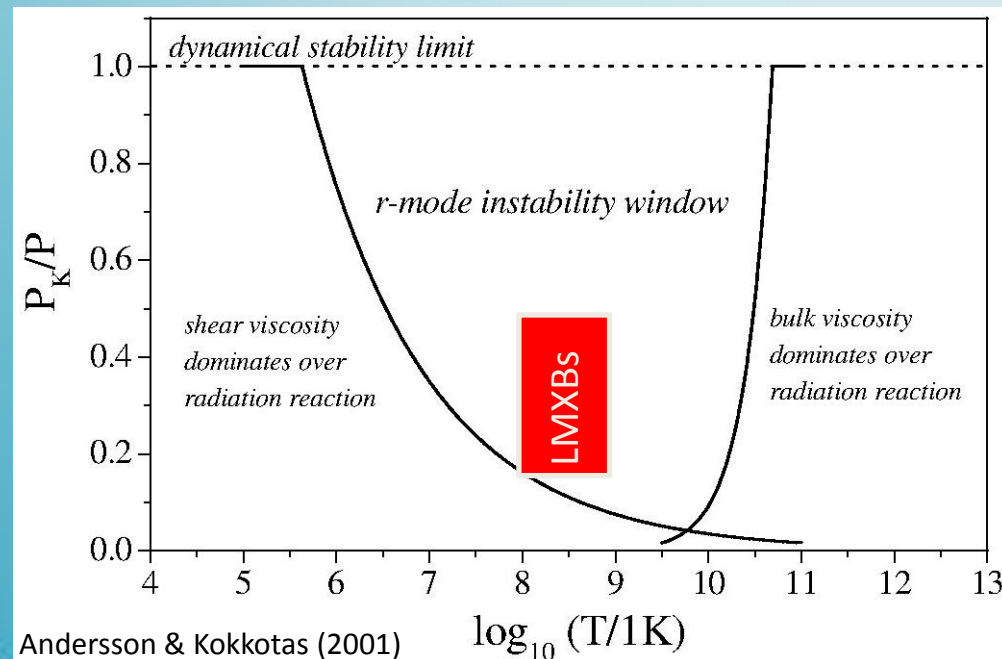
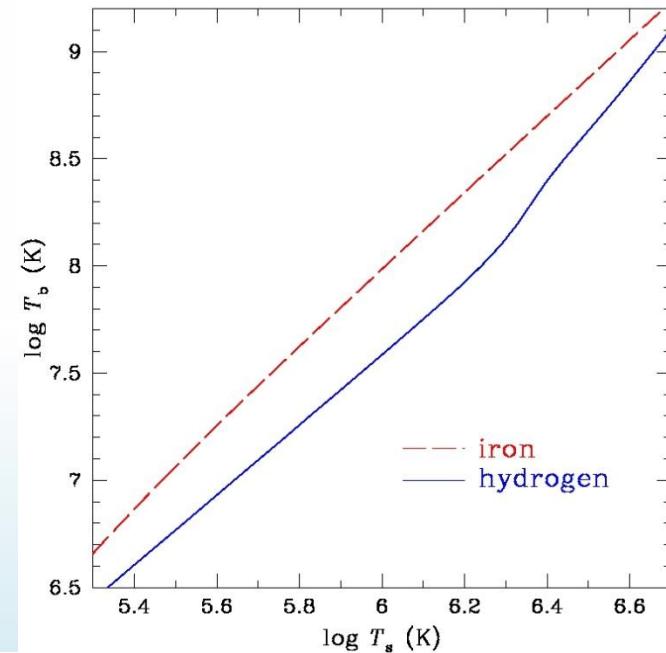
- Fluid oscillations in rotating stars
- Generically unstable:
 - Gravitational waves drive r-mode **growth**
 - Viscosity **damps** r-mode
 - shear viscosity at low temperatures
 - bulk viscosity at high temperatures
 - R-mode evolution: $t_{\text{gw}}(\nu_s) = t_{\text{visc}}(\nu_s, T)$



Inferring NS Core Temperature

- Quiescent Low-Mass X-ray Binaries (LMXBs)
 - surface temperature T_{surface} from spectrum
 - from envelope composition: $T_{\text{core}} (T_{\text{surface}})$
- Accreting LMXBs
 - measure accretion luminosity $L_{\text{acc}} = 4\pi d^2 F_{\text{X}}$
 - accretion spin-up balances GW spin-down
 - from heating = cooling, where
 - r-mode/accretion heating: $L_{\text{heat}} \propto \nu_s \times L_{\text{acc}}$
 - neutrino cooling: $L_{\nu} (T_{\text{core}})$

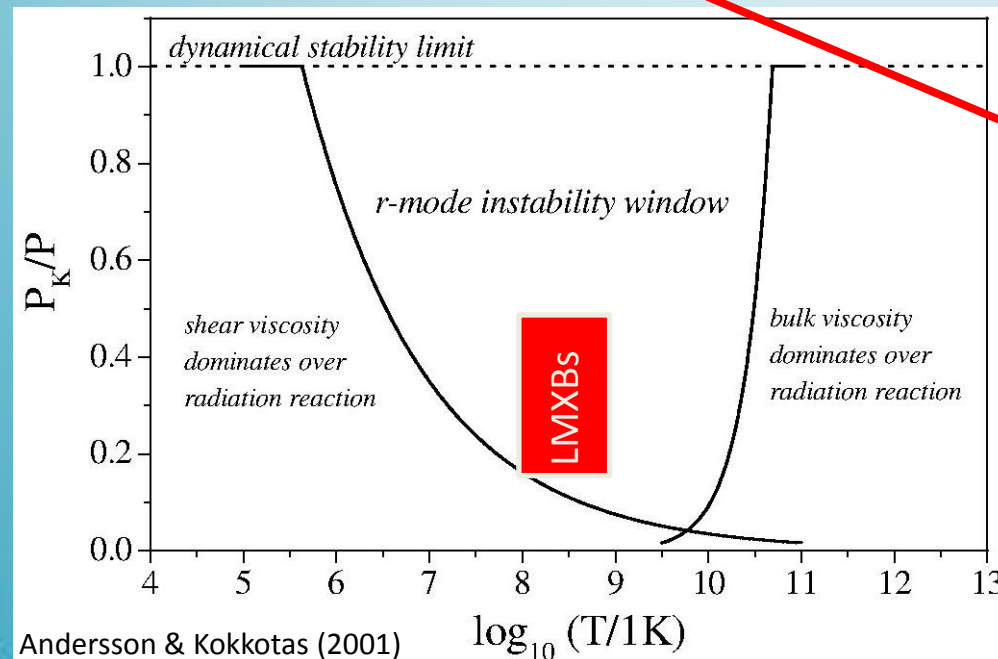
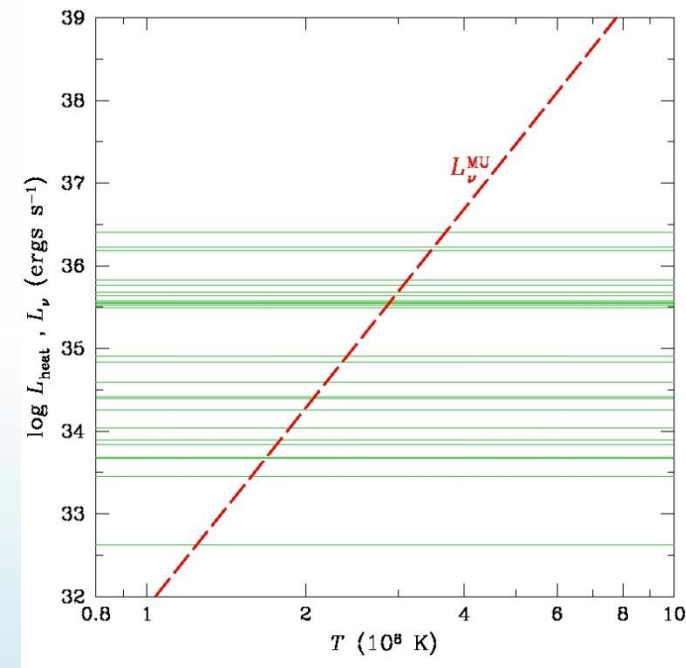
thermal conductivity



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need to know distance



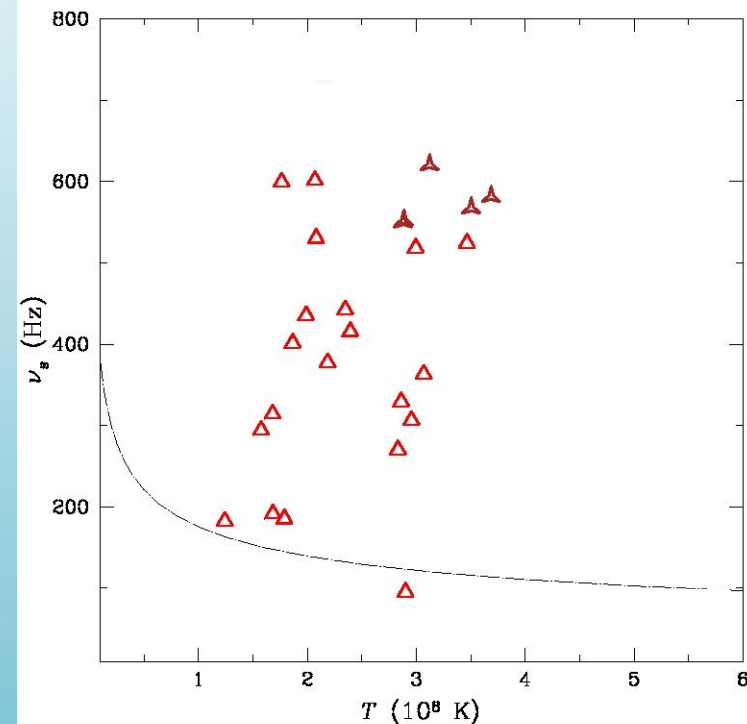
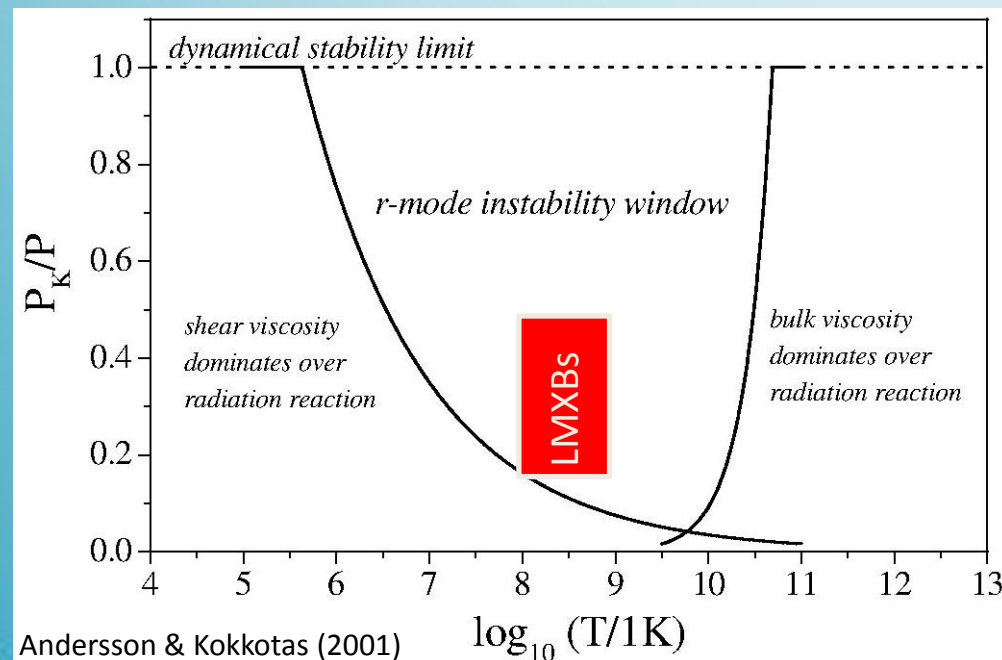
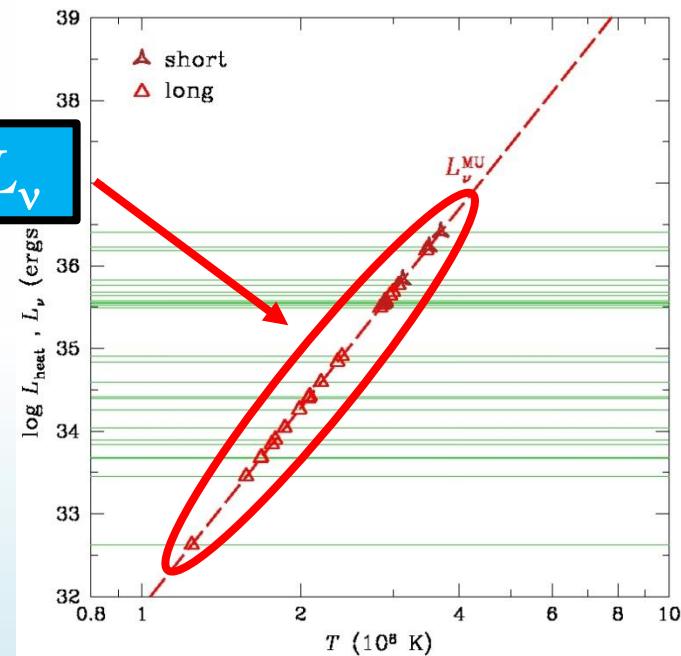
standard/slow cooling
(by modified Urca):

$$L_{\nu}^{\text{MU}} \propto T^8$$

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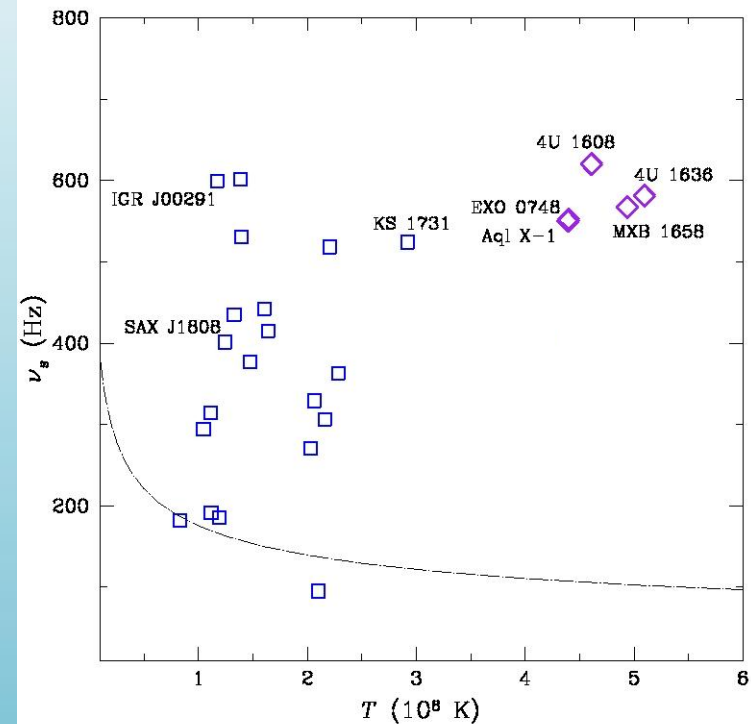
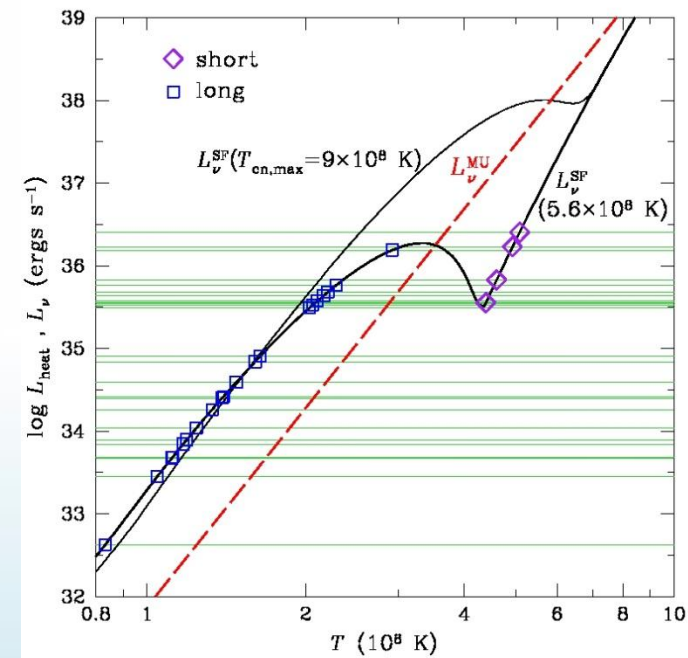
$$L_{\text{heat}} = L_{\nu}$$



Inferring NS Core Temperature

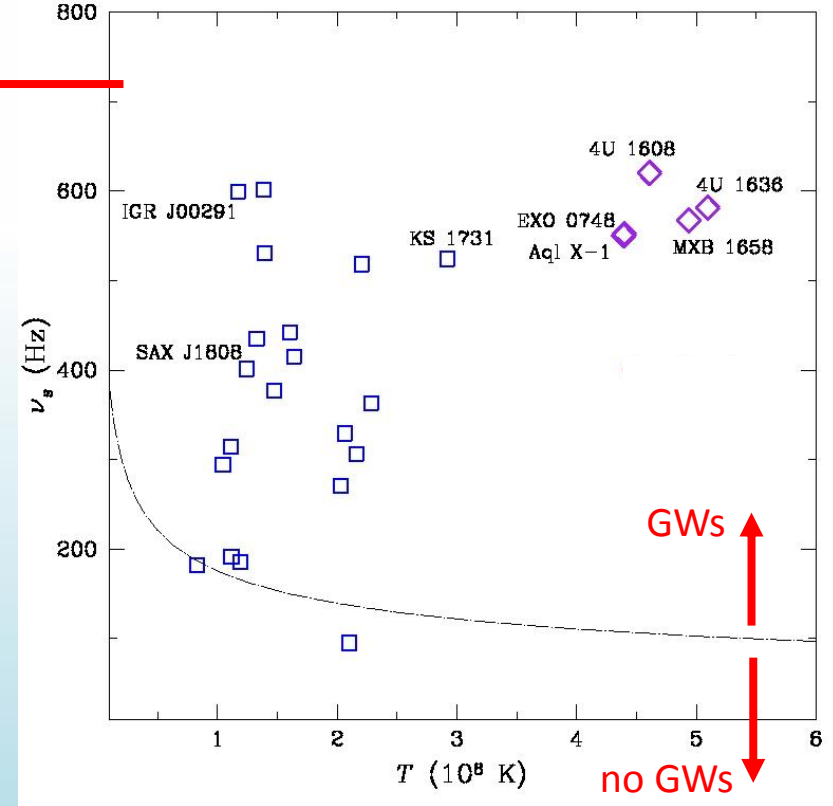
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superfluid cooling
[Cas A NS: $T_c \approx (5-9) \times 10^8$ K]



R-mode Instability vs Observations

- Unstable r-mode
 - spin-temperature limit cycle
 - large amplitude: short time in window
 - small amplitude: not deep in window
 - cannot produce high ν_s
 - spin-down by magnetic dipole w/o GWs
- Stable r-mode
 - crustal physics
 - viscous boundary layer
 - mode resonance with elastic crust
 - magnetic field shortens τ_{VBL}
 - $B > 10^{11}$ G to stabilize
 - high viscosity at high T
 - superfluid-suppressed hyperon bulk viscosity
 - but spin-down vs. $\nu_s = 716$ Hz
 - superfluid mutual friction
 - e^- scatter off superfluid vortices (too weak)
 - but (strong enough?) friction from vortex-fluxtube interaction



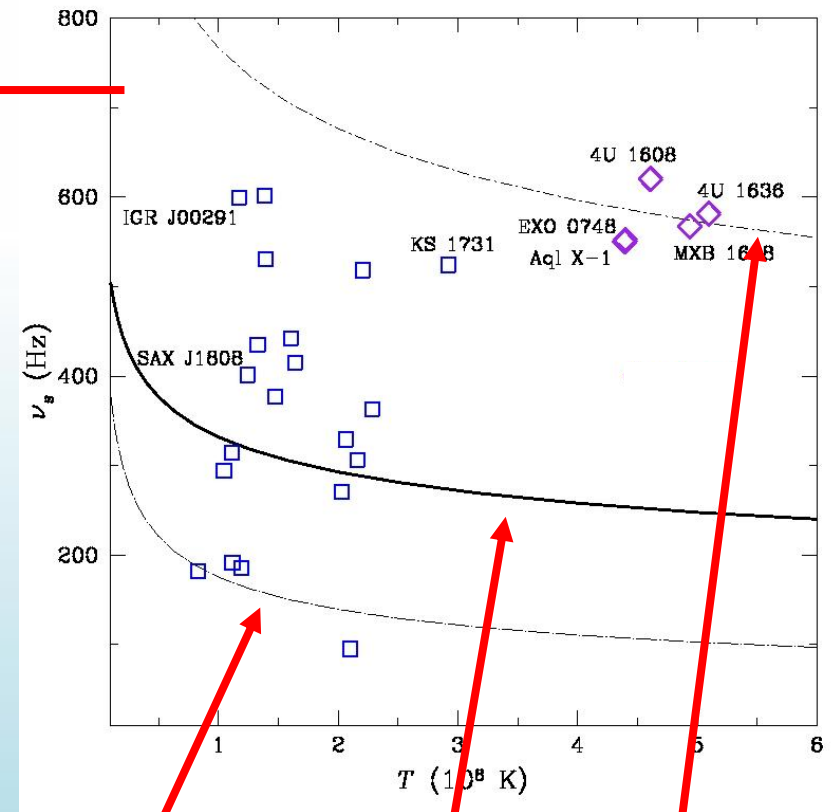
Closing the Window? (Crust-Core Boundary)

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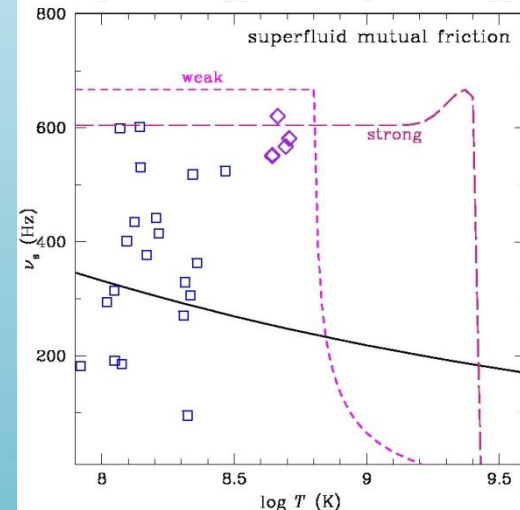
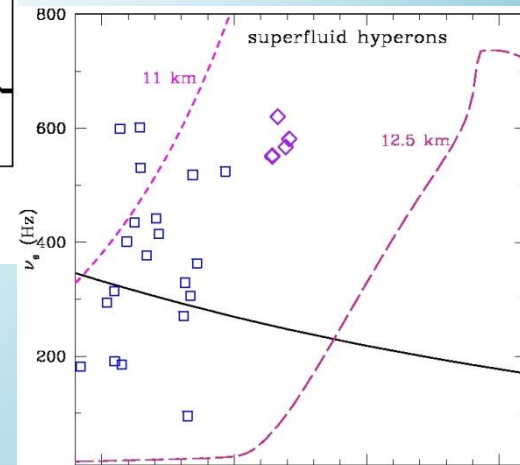
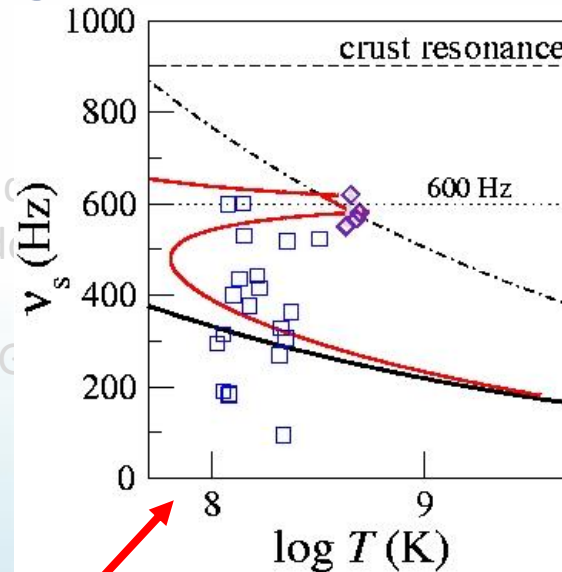
Closing the Window

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Status of R-mode Instability

- Window for gravitational radiation not well-understood
- Some systems should be GW emitters but counter to expectations
- Relevant astrophysics/physics
 - core temperature estimates:
 - envelope composition
 - neutrino emission
 - LMXB distances
 - window shape:
 - **crust elasticity**
 - **superfluidity** (critical temperature, hyperons, mutual friction)
 - **magnetic field** (damping and estimates from LMXBs)

