

Workshop on the Standard Model and Beyond
Corfu Summer Institute
24 August - 3 September 2025

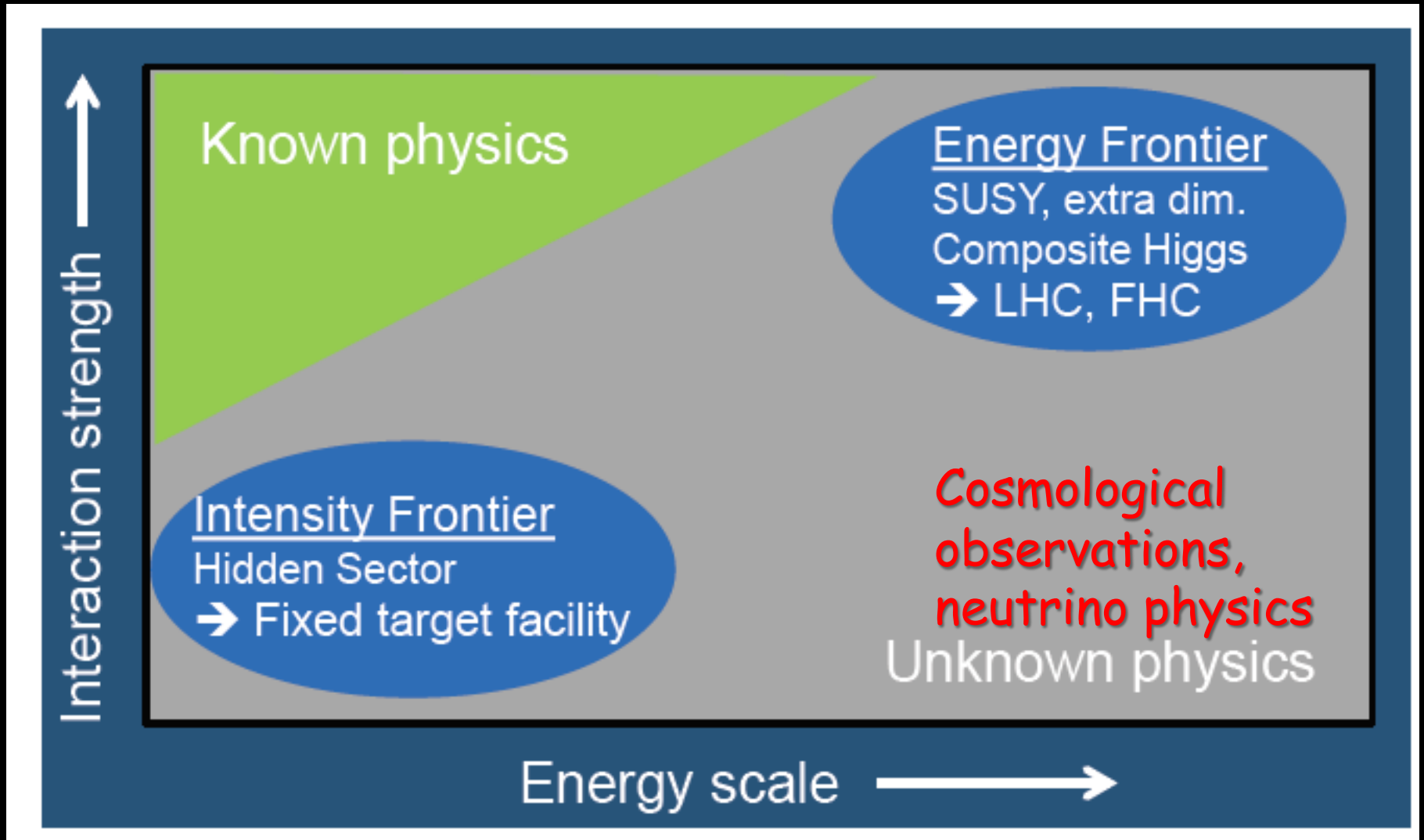
$SO(10)$ -inspired
Leptogenesis

(mainly based on 2507.06144 with Xubin Hu)

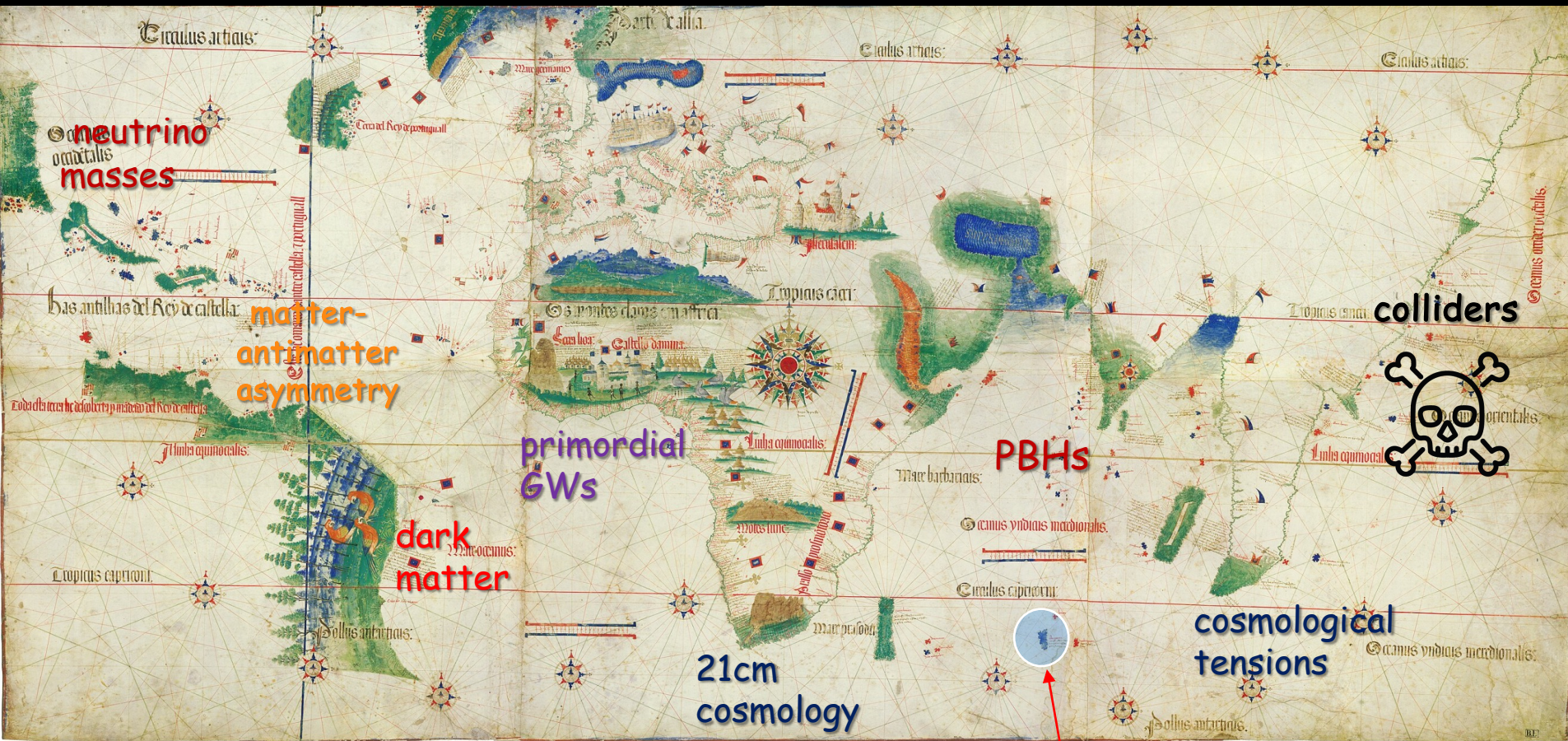
Pasquale Di Bari
(University of Southampton)

New frontiers

(SHIP proposal, 1504.04855)



A map to new physics?



(Cantino planisphere, 1502, Biblioteca Estense Modena)

excess radio
background
(CORFU24)

Fitting the ARCADE 2 excess radio background

(Dev, PDB, Martinez-Soler, Roshan 2312.03082)

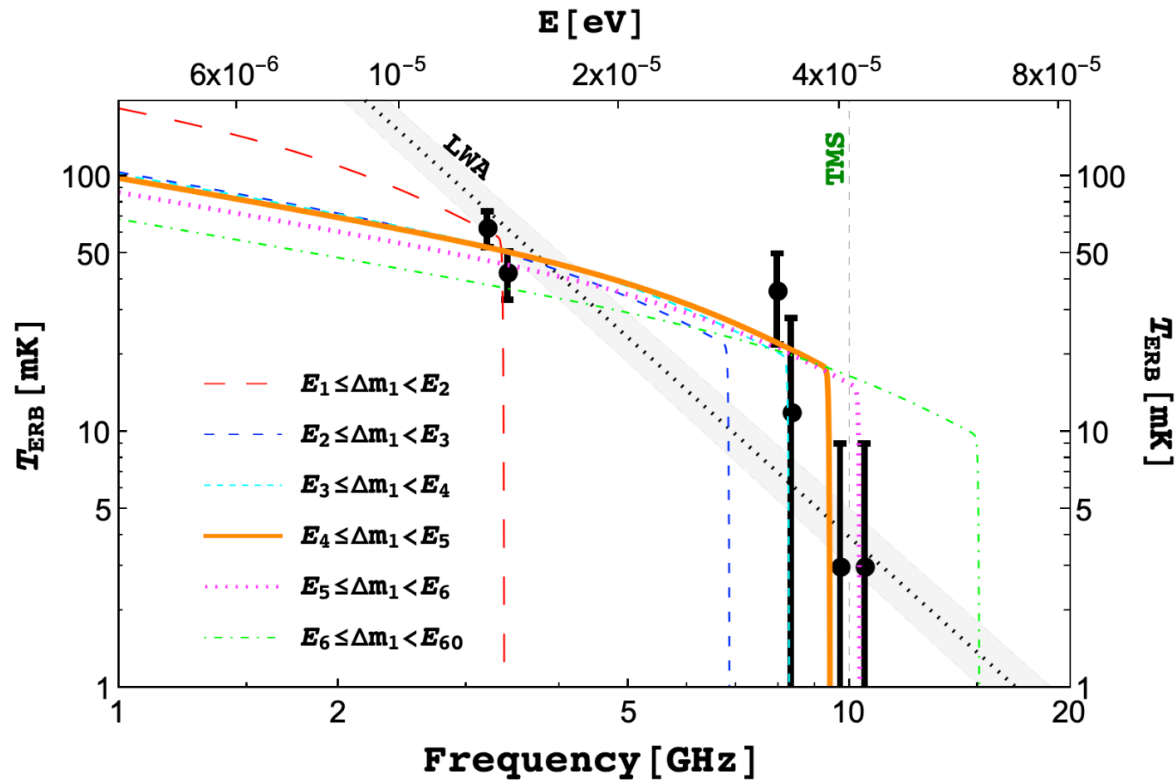
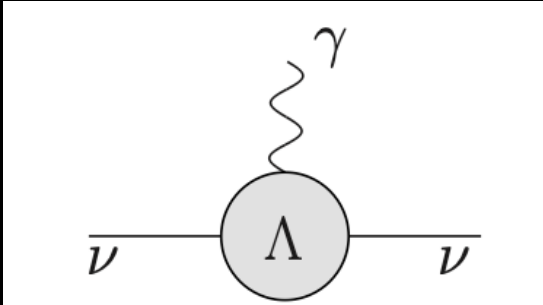


Figure 2. Best fit curves for T_{ERB} obtained with Eq. (3.2). The thick solid orange curve corresponds to a solution very close to the best global fit ($\Delta m_1 = 4.0 \times 10^{-5}$ eV and $\tau_1 = 1.46 \times 10^{21}$ s). The ARCADE 2 data points are taken from Ref. [1], while the power-law fit $\beta = -2.58 \pm 0.05$ (dotted line with grey shade) is from [3].

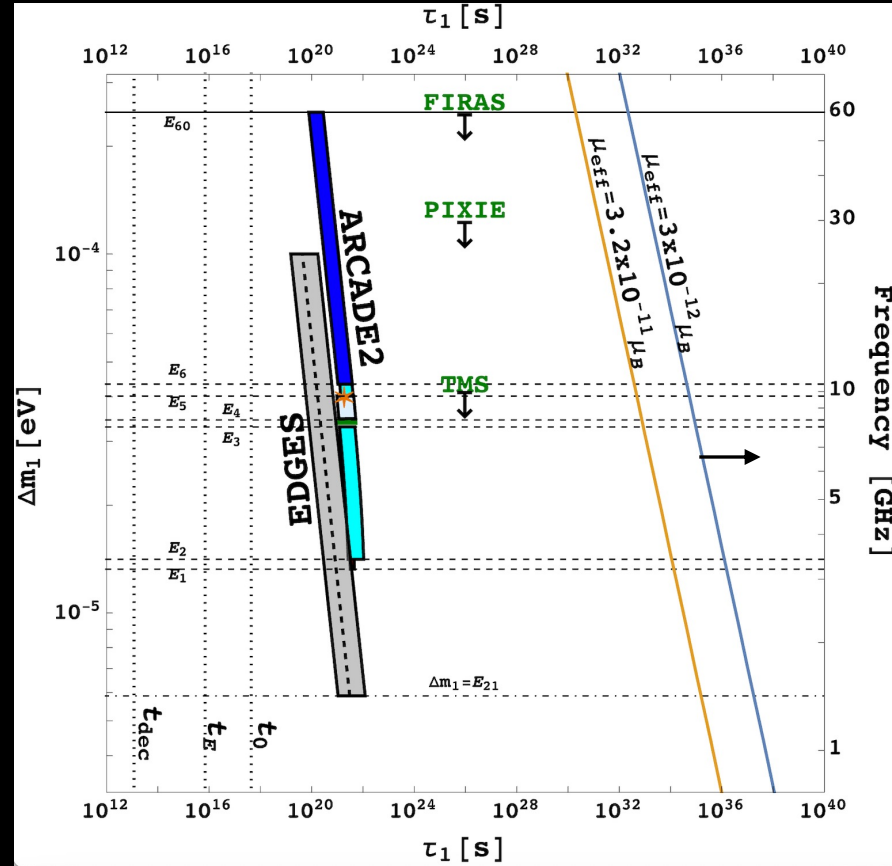
For our best fit we find $\chi^2/4\text{d.of.} = 0.96$, to be compared with $\chi^2/4\text{d.of.} = 2.5$ for the power law

A clash with the upper limits on the effective magnetic moment

(Dev, PDB, Martinez-Soler, Roshan in preparation)



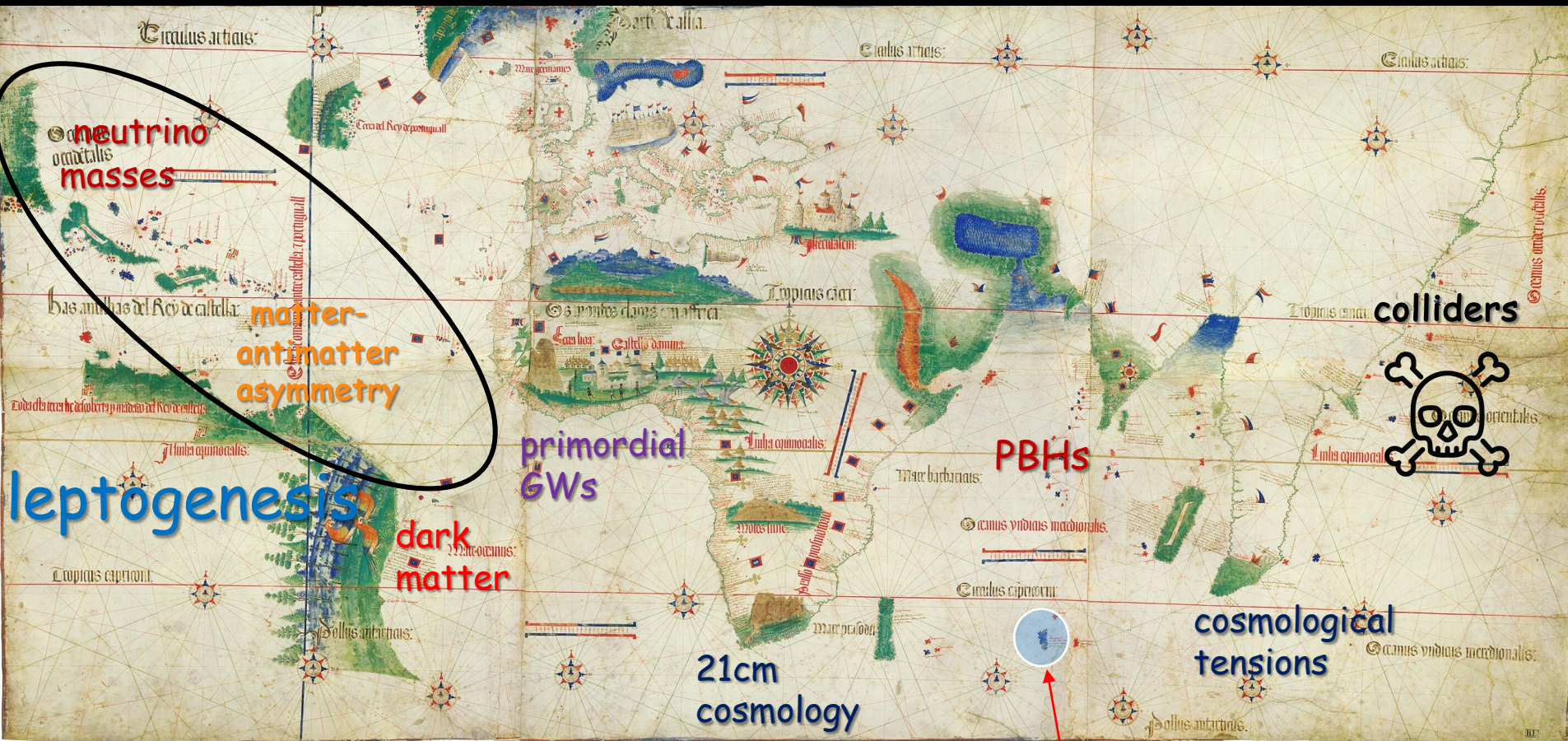
$$\Gamma_{\nu_j \rightarrow \nu_i + \gamma} = \frac{\mu_{\text{eff},ij}^2}{8\pi} \left(\frac{m_j^2 - m_i^2}{m_j} \right)^3$$



This clash is very challenging but certainly interesting: which way to solve it? Stay tuned.

Talk at Tensions in Cosmology this
Thursday paper likely out the same day

A map to new physics?

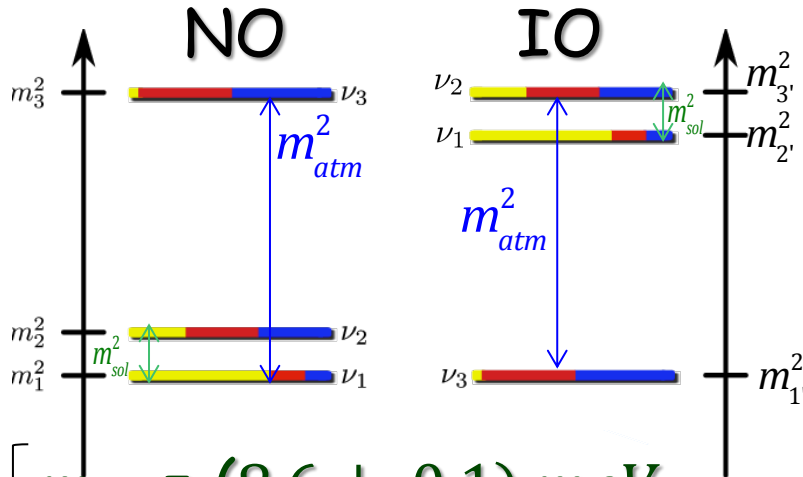


(Cantino planisphere, 1502, Biblioteca Estense Modena)

Preamble

- A common statement is that high scale leptogenesis is untestable.
- $SO(10)$ -inspired leptogenesis, especially in its **STRONG THERMAL** version, provides a counter-example clearly showing that, though challenging, it is possible, even just with standard low energy neutrino experiments, to have a high-scale leptogenesis scenario that is highly predictive, it is already getting tested now and has the potential for a high statistical significance support (or to be relatively quickly ruled out).
- Also, new phenomenological avenues toward tests of high scale scenarios are now possible and intensively explored, mainly thanks to GW discovery.

Neutrino masses ($m_1 < m_2 < m_3$)



$$NO: m_2 = \sqrt{m_1^2 + m_{sol}^2}, \quad m_3 = \sqrt{m_1^2 + m_{atm}^2}$$

$$IO: m_2 = \sqrt{m_1^2 + m_{atm}^2 - m_{sol}^2}, \quad m_3 = \sqrt{m_1^2 + m_{atm}^2}$$

$$m_{sol} = (8.6 \pm 0.1) \text{ meV}$$

$$m_{atm} = (50.0 \pm 0.3) \text{ meV}$$

$$\Rightarrow \sum m_i \gtrsim 58 \text{ meV (95\%CL)}$$

DESI DR2 (BAO) + Planck18 (2503.147438):

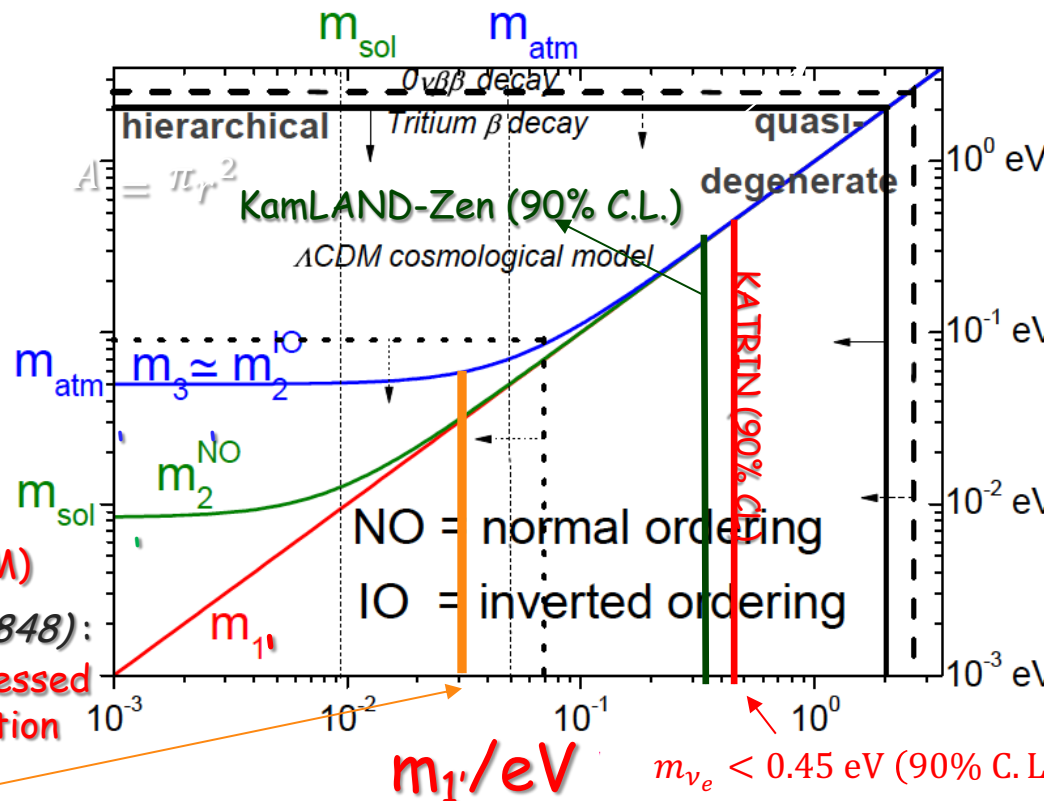
$$\Rightarrow \sum m_i \lesssim 64 \text{ meV (95\%CL)} \quad (\text{assuming } \Lambda\text{CDM})$$

$$\Rightarrow \sum m_i \lesssim 117 \text{ meV (95\%CL)} \quad (+\text{Pantheon SNe assuming } w_0 w_a \text{CDM})$$

DESI DR2 (BAO) + Planck18 + Pantheon (2507.01848):

$$\Rightarrow \sum m_i \lesssim 134 \text{ meV (95\%CL)} \quad (\text{assuming suppressed matter perturbation growth rate})$$

for NO: $m_1 < 30 \text{ meV}$ (95\% C.L.) (this talk)



Neutrino mixing parameters:

$$U_{\alpha i} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} e^{i\rho} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{i\sigma} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\rho} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{i\sigma} \end{pmatrix}$$

PDG :
 $\alpha_{31} = 2(\sigma - \rho)$
 $\alpha_{21} = -2\rho$

Atmospheric, LB

Reactors, LB
(CP violation)

Solar, Reactors

$\beta\beta 0\nu$ decay

$c_{ij} \equiv \cos\theta_{ij}$, $s_{ij} \equiv \sin\theta_{ij}$

3 σ ranges (NO)

$$\theta_{12} = [31.63^\circ, 35.95^\circ]$$

$$\theta_{13} = [8.19^\circ, 8.89^\circ]$$

$$\theta_{23} = [41.3^\circ, 49.9^\circ]$$

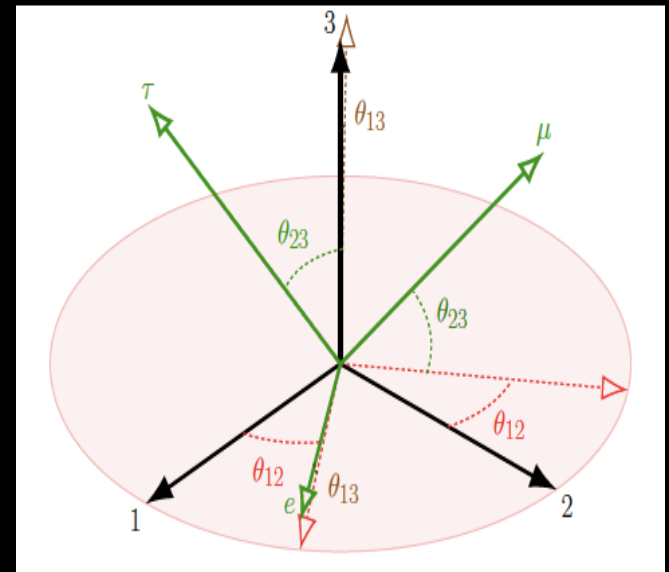
$$\delta = [-236^\circ, 4^\circ]$$

$$\rho, \sigma = [0^\circ, 360^\circ]$$

(vfit September 2024,
with SK atm. data)

NO favoured over IO:

$$\Delta\chi^2(\text{IO-NO}) = 6.1$$



Minimally extended SM

$$\mathcal{L} = \mathcal{L}_{SM} + \mathcal{L}_Y^\nu$$

$$-\mathcal{L}_Y^\nu = \overline{\nu}_L h^\nu \nu_R \phi \Rightarrow -\mathcal{L}_{\text{mass}}^\nu = \overline{\nu}_L m_D \nu_R$$

Dirac
Mass

(in a basis where charged lepton mass matrix is diagonal)

diagonalising m_D :

$$m_D = V_L^\dagger D_{m_D} U_R$$
$$D_{m_D} \equiv \begin{pmatrix} m_{D1} & 0 & 0 \\ 0 & m_{D2} & 0 \\ 0 & 0 & m_{D3} \end{pmatrix}$$

\Rightarrow neutrino masses: $m_i = m_{Di}$

leptonic mixing matrix: $U = V_L^\dagger$

But many unanswered questions:

- Why neutrinos are much lighter than all other fermions?
- Why large mixing angles (differently from CKM angles)?
- Cosmological puzzles?
- Why not a Majorana mass term as well?

Minimal seesaw mechanism (type I)

- Dirac + (right-right) Majorana mass terms

(Minkowski '77; Gell-mann, Ramond, Slansky; Yanagida; Mohapatra, Senjanovic '79)

$$-\mathcal{L}_{\text{mass}}^{\nu} = \overline{\nu}_L m_D \nu_R + \frac{1}{2} \overline{\nu}_R^c M \nu_R + \text{h.c.}$$

violates
lepton
number

In **the see-saw limit** ($M \gg m_D$) the mass spectrum splits into 2 sets:

- 3 light **Majorana neutrinos** with masses (seesaw formula):

$$\text{diag}(m_1, m_2, m_3) = -U^\dagger m_D \frac{1}{M} m_D^T U^*$$

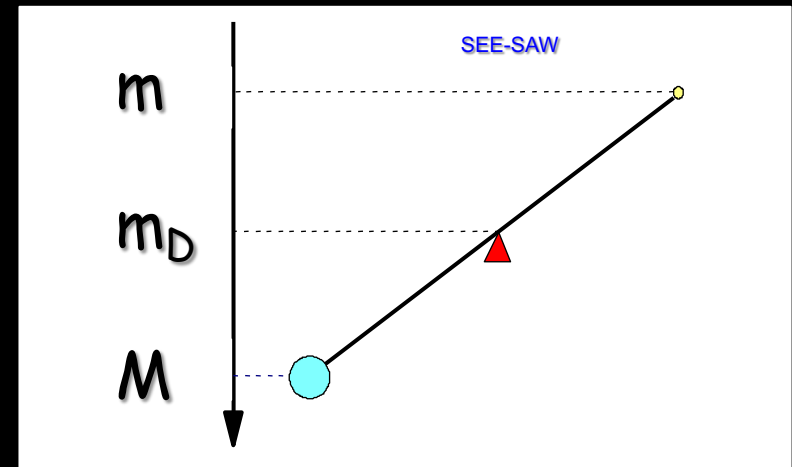
- 3(?) very heavy Majorana neutrinos N_I, N_{II}, N_{III} with $M_{III} > M_{II} > M_I \gg m_D$

1 generation toy model :

$$m_D \sim m_{\text{top}},$$

$$m \sim m_{\text{atm}} \sim 50 \text{ meV}$$

$$\Rightarrow M \sim M_{\text{GUT}} \sim 10^{16} \text{ GeV}$$



3 generation seesaw models: two limits

In the flavour basis (both charged lepton mass and Majorana mass matrices are diagonal):

$$-\mathcal{L}_{\text{mass}}^{\nu+\ell} = \overline{\alpha_L} m_\alpha \alpha_R + \overline{\nu_{L\alpha}} m_{D\alpha I} \nu_{RI} + \frac{1}{2} \overline{\nu_{RI}^c} M_I \nu_{RI} + \text{h.c.}$$

$$\alpha = e, \mu, \tau$$

$$I = 1, 2, 3$$

bi-unitary parameterisation: $m_D = V_L^\dagger D_{m_D} U_R$ $D_{m_D} \equiv \text{diag}(m_{D1}, m_{D2}, m_{D3})$

FIRST (EASY) LIMIT: ALL MIXING FROM THE LEFT-HANDED SECTOR

• $U_R = I \Rightarrow$ again $U = V_L^\dagger$ and neutrino masses: $m_i = \frac{m_{Di}^2}{M_I}$

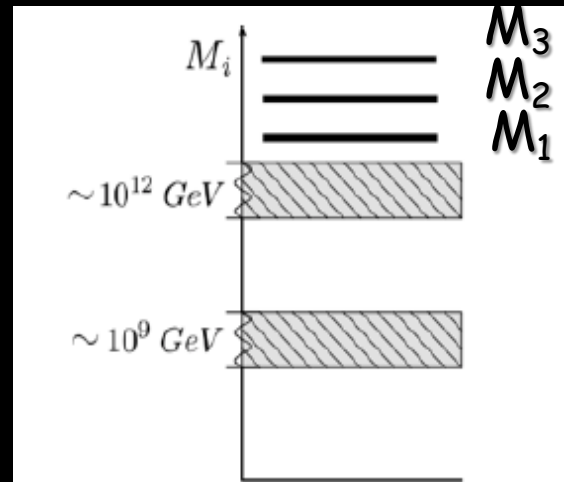
If also $m_{D1} = m_{D2} = m_{D3} = \lambda$ then simply: $M_I = \frac{\lambda^2}{m_i}$

Exercise: $\lambda \sim 100 \text{ GeV}$

$$m_1 \sim 10^{-4} \text{ eV} \Rightarrow M_3 \sim 10^{17} \text{ GeV}$$

$$m_2 = m_{\text{sol}} \sim 10 \text{ meV} \Rightarrow M_2 \sim 10^{15} \text{ GeV}$$

$$m_3 = m_{\text{atm}} \sim 50 \text{ meV} \Rightarrow M_1 \sim 10^{14} \text{ GeV}$$



Typically RH neutrino mass spectrum emerging in simple discrete flavour symmetry models

A SECOND LIMIT: ALL MIXING FROM THE RH SECTOR

(Branco et al. '02; Nezri, Orloff '02; Akhmedov, Frigerio, Smirnov '03; PDB, Riotto '08; PDB, Re Fiorentin '12)

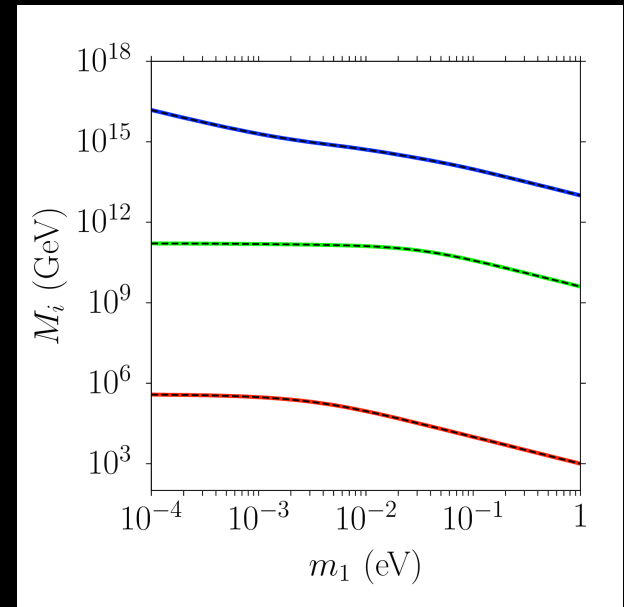
$$\bullet \quad V_L = I \Rightarrow M_1 = \frac{m_{D1}^2}{m_{\beta\beta}}; \quad M_2 = \frac{m_{D2}^2}{m_1 m_2 m_3} \frac{m_{\beta\beta}}{|(m_v^{-1})_{\tau\tau}|}; \quad M_3 = m_{D3}^2 |(m_v^{-1})_{\tau\tau}|$$

If one also imposes (SO(10))-inspired models)

$$m_{D1} = \alpha_1 m_{up}; \quad m_{D2} = \alpha_2 m_{charm}; \quad m_{D3} = \alpha_3 m_{top}; \quad \alpha_i = O(1)$$

Barring very fine-tuned solutions,
one obtains a very hierarchical
RH neutrino mass spectrum

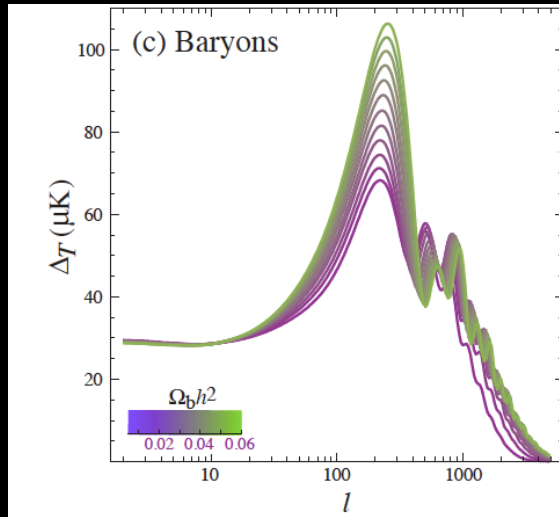
Combining discrete flavour + grand
unified symmetries one can obtain
all mass spectra between
these two limits



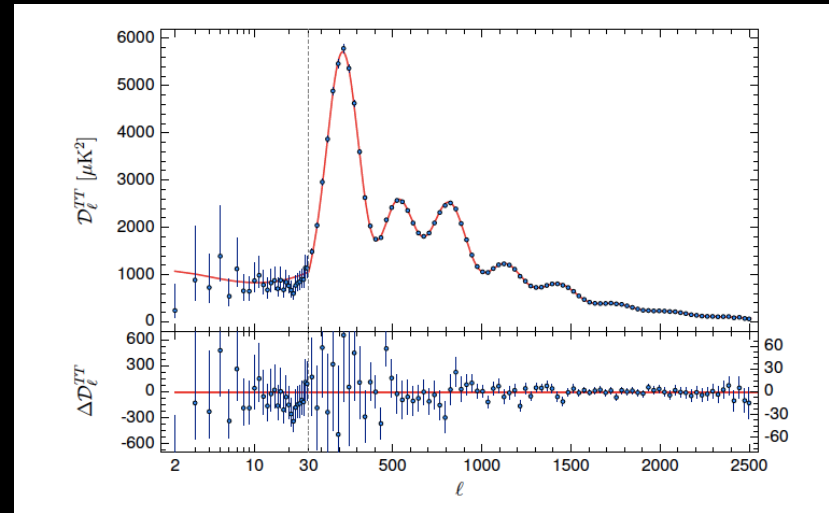
How can we test the existence of these very heavy seesaw neutrinos
and their mass spectrum?

Baryon asymmetry of the universe

(Hu, Dodelson, astro-ph/0110414)



(Planck 2018, 1807.06209)



(CMB+BAO)

$$\Omega_{B0} h^2 = 0.02242 \pm 0.00014$$

$$\eta_{B0} \equiv \frac{n_{B0} - \bar{n}_{B0}}{n_{\gamma 0}} \simeq \frac{n_{B0}}{n_{\gamma 0}} \simeq 273.5 \Omega_{B0} h^2 \times 10^{-10} = (6.12 \pm 0.04) \times 10^{-10} = \eta_{B0}^{CMB}$$

- Consistent with (older) BBN determination but more precise and accurate
- Today the asymmetry coincides with the matter abundance since there is no evidence of primordial antimatter
- Even though all 3 Sakharov conditions are satisfied in the SM, any attempt to reproduce the observed value fails by many orders of magnitude \Rightarrow it requires NEW PHYSICS!

Minimal scenario of leptogenesis

(Fukugita, Yanagida '86)

- Type I seesaw mechanism

- Thermal production of RH neutrinos: $T_{RH} \gtrsim T_{lep} \simeq M_i / (2 \div 10)$

heavy neutrinos decay

$$N_I \xrightarrow{\Gamma_I} L_I + \phi^\dagger \quad N_I \xrightarrow{\bar{\Gamma}} \bar{L}_I + \phi$$

total CP asymmetries

$$\varepsilon_I \equiv -\frac{\Gamma - \bar{\Gamma}}{\Gamma + \bar{\Gamma}}$$

$$\Rightarrow N_{B-L}^{fin} = \sum_{I=1,2,3} \varepsilon_I \times K_I^{fin}$$

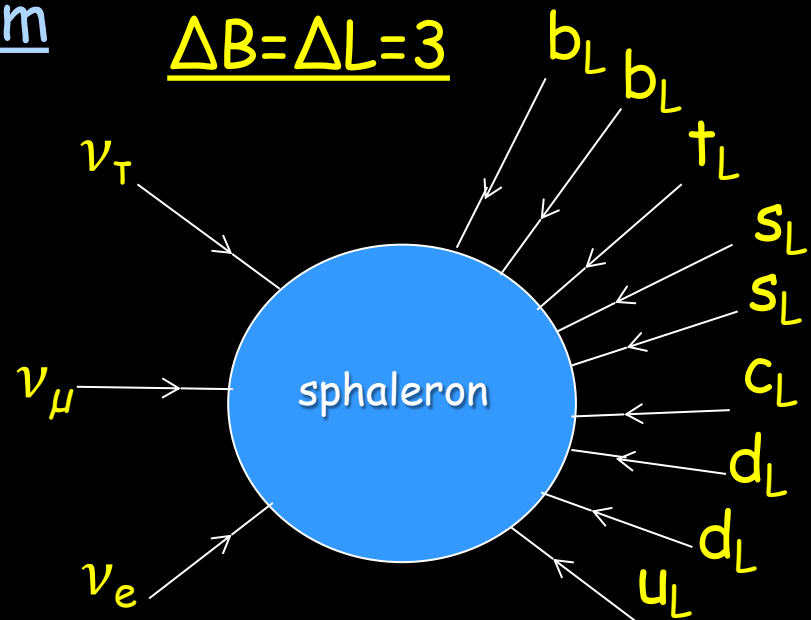
efficiency factors

- Sphaleron processes in equilibrium

$$\Rightarrow T_{lep} \gtrsim T_{sphalerons}^{off} \simeq 132 \text{ GeV}$$

(Kuzmin, Rubakov, Shaposhnikov '85
D'Onofrio, Rummukainen, Tranberg 1404.3565)

$$\Rightarrow \eta_{B0}^{lep} = \frac{a_{sph} N_{B-L}^{fin}}{N_\gamma^{rec}} \simeq 0.01 N_{B-L}^{fin}$$



Seesaw parameter space

Combining $\eta_{B0}^{lep} \simeq \eta_{B0}^{CMB} \simeq 6 \times 10^{-10}$ with low energy neutrino data
can we test seesaw and leptogenesis?

(Casas, Ibarra'01) $m_\nu = -m_D \frac{1}{M} m_D^T \Leftrightarrow \boxed{\Omega^T \Omega = I}$ **Orthogonal parameterisation**

$m_D = U \begin{pmatrix} \sqrt{m_1} & 0 & 0 \\ 0 & \sqrt{m_2} & 0 \\ 0 & 0 & \sqrt{m_3} \end{pmatrix} \Omega \begin{pmatrix} \sqrt{M_1} & 0 & 0 \\ 0 & \sqrt{M_2} & 0 \\ 0 & 0 & \sqrt{M_3} \end{pmatrix}$ (in a basis where charged lepton and Majorana mass matrices are diagonal)

light neutrino parameters

heavy neutrino parameters escaping experimental information

- ❑ Popular solution: *low-scale* leptogenesis, potential direct discovery of RH neutrinos in lab neutrino experiments (no signs so far).
- ❑ *High-scale* leptogenesis is challenging to test but there are a few strategies able to reduce the number of parameters in order to obtain testable predictions on low energy neutrino parameters

Vanilla leptogenesis \Rightarrow upper bound on ν masses

(Buchmüller, PDB, Plümacher '04; Blanchet, PDB '07, Garbrecht et al 2025)

1) Lepton flavor composition is neglected

2) Hierarchical spectrum ($M_2 \gtrsim 2M_1$)

3) Strong lightest RH neutrino wash-out

$$\eta_{B0} \simeq 0.01 N_{B-L}^{final} \simeq 0.01 \varepsilon_1 \kappa_1^{fin}(K_1, m_1)$$

decay parameter: $K_1 \equiv \frac{\Gamma_{N_1}(T=0)}{H(T=M_1)}$

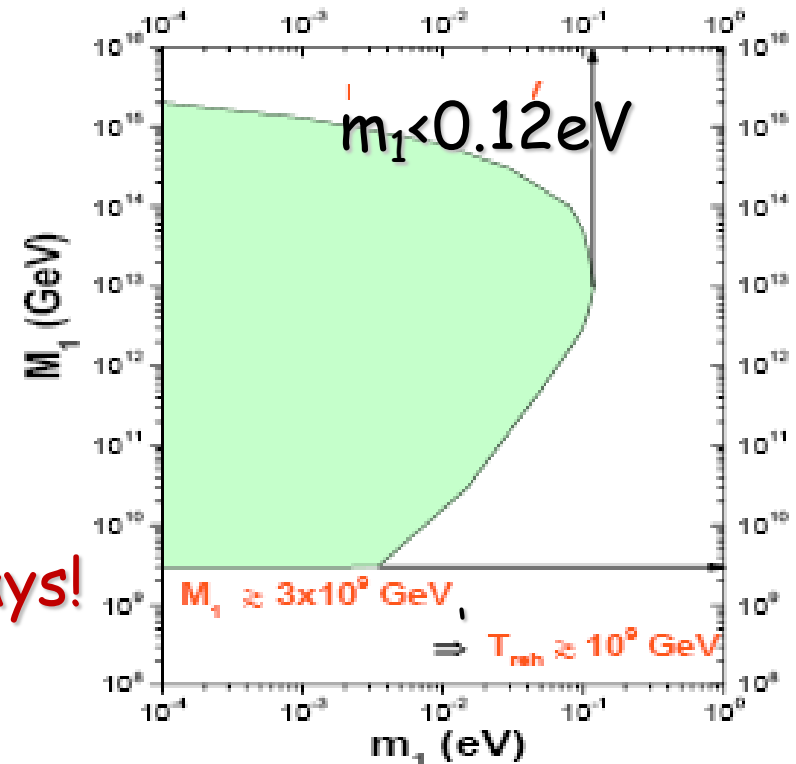
All the asymmetry is generated by the lightest RH neutrino decays!

4) Barring fine-tuned cancellations

(Davidson, Ibarra '02)

$$\varepsilon_1 \leq \varepsilon_1^{\max} \simeq 10^{-6} \left(\frac{M_1}{10^{10} \text{ GeV}} \right) \frac{m_{\text{atm}}}{m_1 + m_3}$$

$$\eta_B^{\max}(m_1, M_1) \geq \eta_B^{\text{CMB}}$$



No dependence on the leptonic mixing matrix U : it cancels out!

IS SO(10)-INSPIRED LEPTOGENESIS RULED OUT?

Independence of the initial conditions (strong thermal leptogenesis)

(Buchmüller, PDB, Plümacher '04)

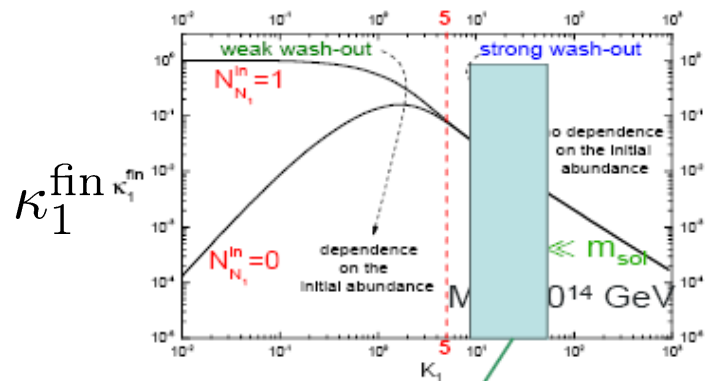
wash-out of a pre-existing asymmetry N_{B-L}^p

$$N_{B-L}^{p, \text{final}} = N_{B-L}^{p, \text{initial}} e^{-\frac{3\pi}{8} K_1} \ll N_{B-L}^{f, N_1}$$

decay parameter: $K_1 \equiv \frac{\Gamma_{N_1}}{H(T = M_1)} \sim \frac{m_{\text{sol, atm}}}{m_* \sim 10^{-3} \text{ eV}} \sim 10 \div 50$ Just a coincidence?

equilibrium neutrino mass: $m_* = \frac{16\pi^{5/2} \sqrt{g_*}}{3\sqrt{5}} \frac{v^2}{M_{\text{Pl}}} \simeq 1.08 \times 10^{-3} \text{ eV}$

Independence of the
initial N_1 abundance



$$K_{\text{sol}} \simeq 9 \lesssim K_1 \lesssim 50 \simeq K_{\text{atm}}$$

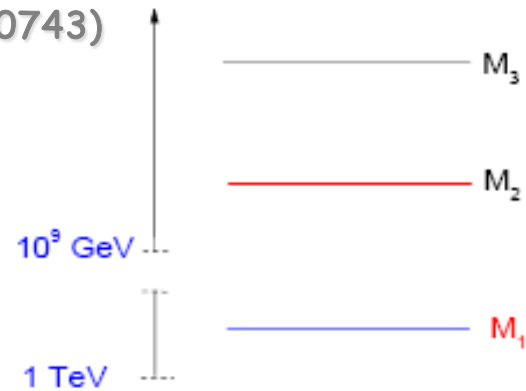
N₂-leptogenesis

(PDB hep-ph/0502082, Vives hep-ph/0512160; Blanchet, PDB 0807.0743)

- **Unflavoured case:** asymmetry produced from N₂ - RH neutrinos is typically washed-out

$$\eta_{B0}^{lep(N_2)} \simeq 0.01 \cdot \varepsilon_2 \cdot \kappa^{fin}(K_2) \cdot e^{-\frac{3\pi}{8}K_1} \ll \eta_{B0}^{CMB}$$

- **Adding flavour effects:** lightest RH neutrino wash-out acts on individual flavour \Rightarrow much weaker: $K_{1e} + K_{1\mu} + K_{1\tau} = K_1$



$$N_{B-L}^f(N_2) = P_{2e}^0 \varepsilon_2 \kappa(K_2) e^{-\frac{3\pi}{8} K_{1e}} + P_{2\mu}^0 \varepsilon_2 \kappa(K_2) e^{-\frac{3\pi}{8} K_{1\mu}} + P_{2\tau}^0 \varepsilon_2 \kappa(K_2) e^{-\frac{3\pi}{8} K_{1\tau}}$$

- With flavor effects the domain of successful N₂ dominated leptogenesis greatly enlarges: the probability that $K_1 < 1$ is less than 0.1% but the probability that either K_{1e} or $K_{1\mu}$ or $K_{1\tau}$ is less than 1 is ~50% (taking into account experimental data)

(PDB, Michele Re Fiorentin, Rome Samanta 1812.07720)

- Existence of the heaviest RH neutrino N₃ is necessary for the ε_{2a} 's not to be negligible
- It is the only hierarchical scenario that can realise strong thermal leptogenesis (independence of the initial conditions) if the asymmetry is **tauon-dominated** and if $m_1 \gtrsim 10$ meV (corresponding to $\Sigma_i m_i \gtrsim 80$ meV)

(PDB, Michele Re Fiorentin, Sophie King arXiv 1401.6185)

- **Does N₂-leptogenesis (with flavour effects) rescue SO(10)-inspired models?**

Imposing $SO(10)$ -inspired conditions

(Branco et al. '02; Nezri, Orloff '02; Akhmedov, Frigerio, Smirnov '03; PDB, Riotto '08; PDB, Re Fiorentin '12)

Seesaw formula

$$m_\nu = -m_D \frac{1}{D_M} m_D^T.$$

Leptonic mixing matrix

$$U^\dagger m_\nu U^* = -D_m$$

Bi-unitary
parameterisation

$$m_D = V_L^\dagger D_{m_D} U_R$$

$SO(10)$ -inspired conditions

$$m_{D1} = \alpha_1 m_u, m_{D2} = \alpha_2 m_c, m_{D3} = \alpha_3 m_t, \quad (\alpha_i = \mathcal{O}(1))$$

Majorana mass matrix
(in the Yukawa basis)

$$U_R^* D_M U_R^\dagger = \textcircled{M} = D_{m_D} V_L^* U^* D_m^{-1} U^\dagger V_L^\dagger D_{m_D} \simeq -D_{m_D} m_\nu^{-1} D_{m_D}$$

using $V_L \simeq I$

RH neutrino mass spectrum ($V_L \simeq I$)

(Akhmedov, Frigerio, Smirnov, 2005; PDB, Re Fiorentin, Marzola, 1411.5478)

$$U_R \simeq \begin{pmatrix} 1 & -\frac{m_{D1}}{m_{D2}} \frac{m_{\nu e\mu}^*}{m_{\nu ee}^*} & \frac{m_{D1}}{m_{D3}} \frac{(m_\nu^{-1})_{e\tau}^*}{(m_\nu^{-1})_{\tau\tau}^*} \\ \frac{m_{D1}}{m_{D2}} \frac{m_{\nu e\mu}}{m_{\nu ee}} & 1 & \frac{m_{D2}}{m_{D3}} \frac{(m_\nu^{-1})_{\mu\tau}^*}{(m_\nu^{-1})_{\tau\tau}^*} \\ \frac{m_{D1}}{m_{D3}} \frac{m_{\nu e\tau}}{m_{\nu ee}} & -\frac{m_{D2}}{m_{D3}} \frac{(m_\nu^{-1})_{\mu\tau}}{(m_\nu^{-1})_{\tau\tau}} & 1 \end{pmatrix} D_\Phi \quad D_\phi \equiv (e^{-i\frac{\Phi_1}{2}}, e^{-i\frac{\Phi_2}{2}}, e^{-i\frac{\Phi_3}{2}})$$

$$M_1 \simeq \frac{m_{D1}^2}{|m_{\nu ee}|} \simeq \frac{\alpha_1^2 m_u^2}{|m_{\nu ee}|} \simeq \alpha_1^2 10^5 \text{ GeV} \left(\frac{m_u}{1 \text{ MeV}} \right)^2 \left(\frac{10 \text{ meV}}{|m_{\nu ee}|} \right)$$

$$\Phi_1 = \text{Arg}[-m_{\nu ee}^*].$$

$0\nu\beta\beta$ neutrino mass

$$M_2 \simeq \frac{\alpha_2^2 m_c^2}{m_1 m_2 m_3} \frac{|m_{\nu ee}|}{|(m_\nu^{-1})_{\tau\tau}|} \simeq \alpha_2^2 10^{11} \text{ GeV} \left(\frac{m_c}{400 \text{ MeV}} \right)^2 \left(\frac{|m_{\nu ee}|}{10 \text{ meV}} \right)$$

$$\Phi_2 = \text{Arg} \left[\frac{m_{\nu ee}}{(m_\nu^{-1})_{\tau\tau}} \right] - 2(\rho + \sigma)$$

$$M_3 \simeq \alpha_3^2 m_t^2 |(m_\nu^{-1})_{\tau\tau}| \simeq \alpha_3^2 10^{15} \text{ GeV} \left(\frac{m_t}{100 \text{ GeV}} \right)^2 \left(\frac{\text{meV}}{m_1} \right).$$

$$\Phi_3 = \text{Arg}[-(m_\nu^{-1})_{\tau\tau}].$$

Decrypting $SO(10)$ -inspired leptogenesis ($V_L=I$)

(PDB, Re Fiorentin, Marzola, 1411.5478)

Finally, putting all together, one arrives to an expression for the final asymmetry:

$$\begin{aligned}
 N_{B-L}^{\text{lep,f}} &\simeq \frac{3}{16\pi} \frac{\alpha_2^2 m_c^2}{v^2} \frac{|m_{\nu ee}| (|m_{\nu\tau\tau}^{-1}|^2 + |m_{\nu\mu\tau}^{-1}|^2)^{-1}}{m_1 m_2 m_3} \frac{|m_{\nu\tau\tau}^{-1}|^2}{|m_{\nu\mu\tau}^{-1}|^2} \sin \alpha_L \\
 &\times \kappa \left(\frac{m_1 m_2 m_3}{m_\star} \frac{|(m_\nu^{-1})_{\mu\tau}|^2}{|m_{\nu ee}| |(m_\nu^{-1})_{\tau\tau}|} \right) \\
 &\times e^{-\frac{3\pi}{8} \frac{|m_{\nu e\tau}|^2}{m_\star |m_{\nu ee}|}}.
 \end{aligned}$$

$K_{1\tau}$ ←

$SO(10)$ -inspired
leptogenesis phase

$$\alpha_L = \text{Arg}[m_{\nu ee}] - 2 \text{Arg}[(m_\nu^{-1})_{\mu\tau}] + \pi - 2(\rho + \sigma).$$

successful
leptogenesis
condition

$$\eta_B^{SO10lep}(m_1, m_{sol}, m_{atm}, \theta_{12}, \theta_{23}, \theta_{13}, \delta, \rho, \sigma; \alpha_2) = \eta_B^{\text{obs}}$$

This condition identifies an hypersurface in the space of low energy neutrino parameters

All numerical results are accurately reproduced for $V_L=I$

In particular, one has a
strong tau-dominance:

$$\varepsilon_{2\tau} : \varepsilon_{2\mu} : \varepsilon_{2e} = \alpha_3^2 m_t^2 : \alpha_2^2 m_c^2 : \alpha_1^2 m_u^2 \frac{\alpha_3 m_t}{a_2 m_c} \frac{\alpha_1^2 m_u^2}{\alpha_2^2 m_c^2}.$$

Turning on a mismatch between neutrino Yukawa and weak basis ($V_L \neq 1$)

$$V_L = \begin{pmatrix} c_{12}^L c_{13}^L & s_{12}^L c_{13}^L & s_{13}^L e^{-i\delta_L} \\ -s_{12}^L c_{23}^L - c_{12}^L s_{23}^L s_{13}^L e^{i\delta_L} & c_{12}^L c_{23}^L - s_{12}^L s_{23}^L s_{13}^L e^{i\delta_L} & s_{23}^L c_{13}^L \\ s_{12}^L s_{23}^L - c_{12}^L c_{23}^L s_{13}^L e^{i\delta_L} & -c_{12}^L s_{23}^L - s_{12}^L c_{23}^L s_{13}^L e^{i\delta_L} & c_{23}^L c_{13}^L \end{pmatrix} \begin{pmatrix} e^{i\rho_L} & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{i\sigma_L} \end{pmatrix}$$

$$s_{ij}^L \equiv \sin \theta_{ij}^L, \quad c_{ij}^L \equiv \cos \theta_{ij}^L$$

By definition in $SO(10)$ -inspired leptogenesis: $0 \leq \theta_{ij}^L \lesssim \theta_{ij}^{\text{CKM}} (\Leftrightarrow I \leq V_L \lesssim V_{\text{CKM}})$

The upper bounds are not strictly determined, as far as the RH neutrino mass spectrum is such that one can assume N_2 -dominated leptogenesis.

Full analytical solution (V_L arbitrary): RH neutrino mass spectrum and mixing matrix

light neutrino mass
matrix in the Yukawa
basis

$$m_\nu \rightarrow \tilde{m}_\nu = V_L m_\nu V_L^T$$

RH neutrino masses

$$M_1 \simeq \frac{\alpha_1^2 m_u^2}{|(\tilde{m}_\nu)_{11}|}, \quad M_2 \simeq \frac{\alpha_2^2 m_c^2}{m_1 m_2 m_3} \frac{|(\tilde{m}_\nu)_{11}|}{|(\tilde{m}_\nu^{-1})_{33}|}, \quad M_3 \simeq \alpha_3^2 m_t^2 |(\tilde{m}_\nu^{-1})_{33}|$$

RH neutrino phases

$$\Phi_1 \simeq -\text{Arg}[-(\tilde{m}_\nu)_{11}^*], \quad \Phi_2 \simeq \text{Arg}\left[\frac{(\tilde{m}_\nu)_{11}}{(\tilde{m}_\nu^{-1})_{33}}\right] - 2(\rho + \sigma) - 2(\rho_L + \sigma_L), \quad \Phi_3 \simeq \text{Arg}[(\tilde{m}_\nu^{-1})_{33}]$$

RH neutrino
mixing matrix

$$U_R \simeq \begin{pmatrix} 1 & -\frac{m_{D1}}{m_{D2}} \frac{(\tilde{m}_\nu)_{12}^*}{(\tilde{m}_\nu)_{11}^*} & \frac{m_{D1}}{m_{D3}} \frac{(\tilde{m}_\nu^{-1})_{13}^*}{(\tilde{m}_\nu^{-1})_{33}^*} \\ \frac{m_{D1}}{m_{D2}} \frac{(\tilde{m}_\nu)_{12}}{(\tilde{m}_\nu)_{11}} & 1 & \frac{m_{D2}}{m_{D3}} \frac{(\tilde{m}_\nu^{-1})_{23}^*}{(\tilde{m}_\nu^{-1})_{33}^*} \\ \frac{m_{D1}}{m_{D3}} \frac{(\tilde{m}_\nu^{-1})_{13}}{(\tilde{m}_\nu^{-1})_{33}} & -\frac{m_{D2}}{m_{D3}} \frac{(\tilde{m}_\nu^{-1})_{23}}{(\tilde{m}_\nu^{-1})_{33}} & 1 \end{pmatrix} D_\Phi, \quad D_\Phi \equiv \begin{pmatrix} e^{-i\frac{\Phi_1}{2}}, e^{-i\frac{\Phi_2}{2}}, e^{-i\frac{\Phi_3}{2}} \end{pmatrix}$$

Full analytical solution for the asymmetry ($I \leq V_L \lesssim V_{CKM}$)

Flavoured decay
parameters

$$K_{I\alpha} = \frac{\sum_{k,l} m_{Dk} m_{Dl} V_{Lk\alpha} V_{Ll\alpha}^* U_{Rkl}^* U_{Rli}}{M_I m_*}$$

Flavoured CP
asymmetries

$$\epsilon_{2\alpha} = \frac{3}{16\pi v^2} \frac{|(\tilde{m}_\nu)_{11}|}{m_1 m_2 m_3} \frac{\sum_{k,l} m_{Dk} m_{Dl} \text{Im}[V_{Lk\alpha} V_{Ll\alpha}^* U_{Rk2}^* U_{Rl3} U_{R32}^* U_{R33}]}{|(\tilde{m}_\nu^{-1})_{33}|^2 + |(\tilde{m}_\nu^{-1})_{23}|^2}$$

Final B-L
asymmetry

$$N_{B-L}^{\text{lep,f}} = \epsilon_{2e} \kappa(K_{2e} + K_{2\mu}) e^{-\frac{3\pi}{8} K_{1e}} + \epsilon_{2\mu} \kappa(K_{2e} + K_{2\mu}) e^{-\frac{3\pi}{8} K_{1\mu}} + \epsilon_{2\tau} \kappa(K_{2\tau}) e^{-\frac{3\pi}{8} K_{1\tau}}$$

This time one has: $\eta_B^{SO10lep}(m_1, m_{sol}, m_{atm}, \theta_{12}, \theta_{23}, \theta_{13}, \delta, \rho, \sigma; \alpha_2, V_L) = \eta_B^{\text{obs}}$

The dependence on the 6 parameters in V_L give some thickness to the hypersurface that becomes a layer but the smallness of the θ_{ij}^L however still make in a way that constraints do relax but in general do not evaporate.

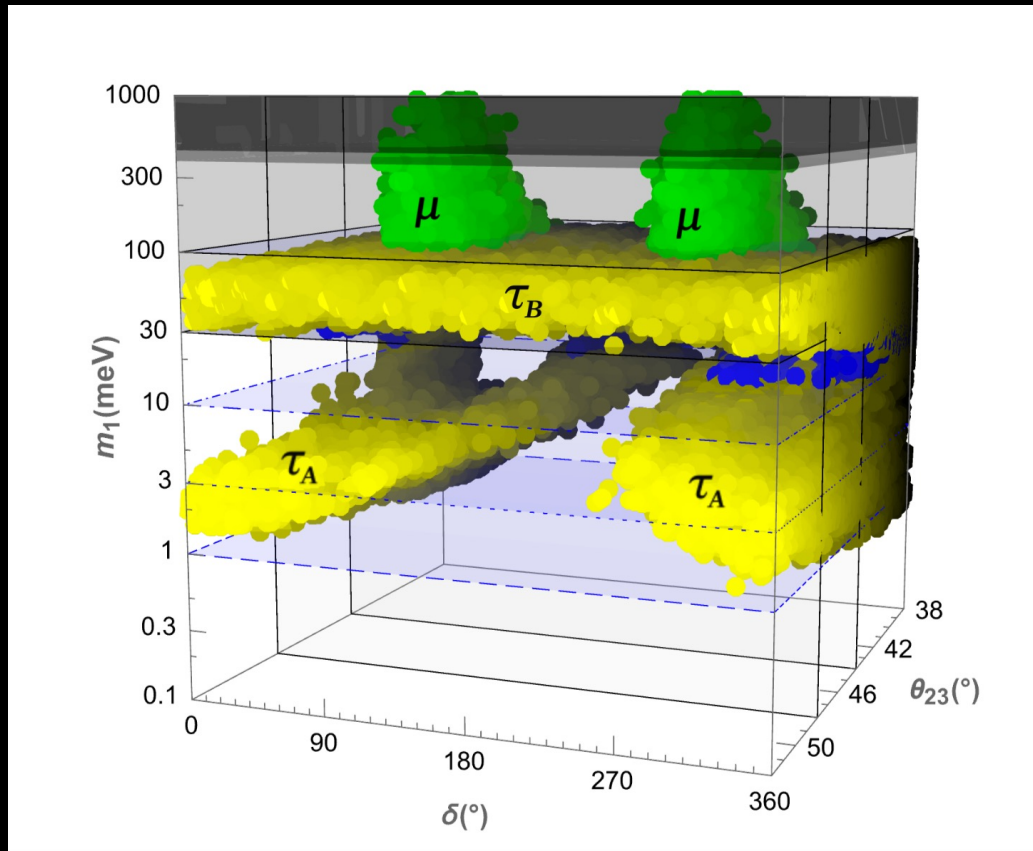
Also notice that now:

$$\epsilon_{2e}^{\max} : \epsilon_{2\mu}^{\max} : \epsilon_{2\tau}^{\max} \simeq 1 : |V_{L23}| : |V_{L21} V_{L31}|$$

This explains why tauon solutions are still favoured but this time also muon solutions appear and in the supersymmetric case even very marginal electron solutions

3-dim projection of the allowed region (NO)

$\alpha_2=5$ NORMAL ORDERING $I \leq V_L \leq V_{CKM}$



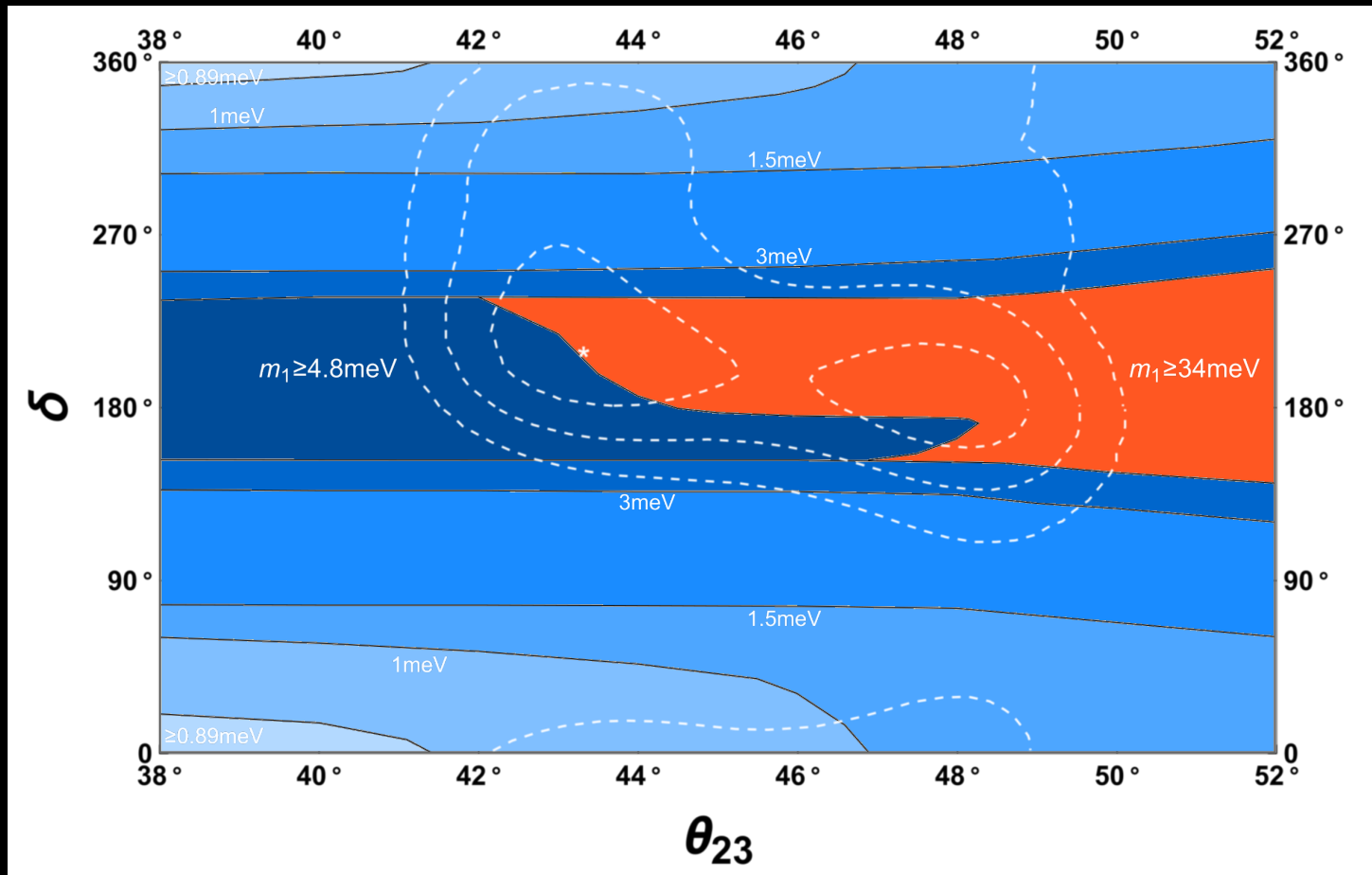
$\sim 2 \times 10^6$ points
out of
 $\sim 2 \times 10^9$ trials
(success rate is
 $\sim 0.1\%$)

(PDB, R. Samanta 2005.03057; PDB, Xubin Hu 2507.06144)

➤ N_2 -leptogenesis (with flavour effects) does rescue
SO(10)-inspired models! It works only for NO

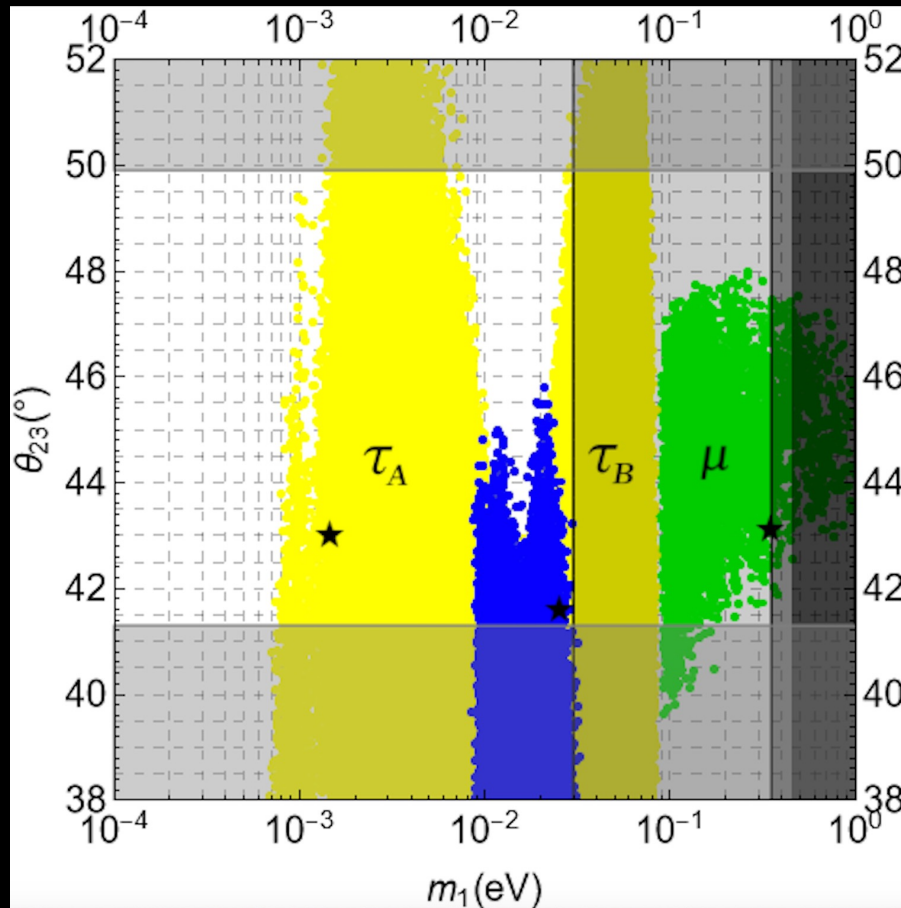
(PDB, Riotto 0809.2285 and 1012.2343;0810.1104)

SO(10)-inspired leptogenesis confronting long baseline and absolute neutrino mass experiments



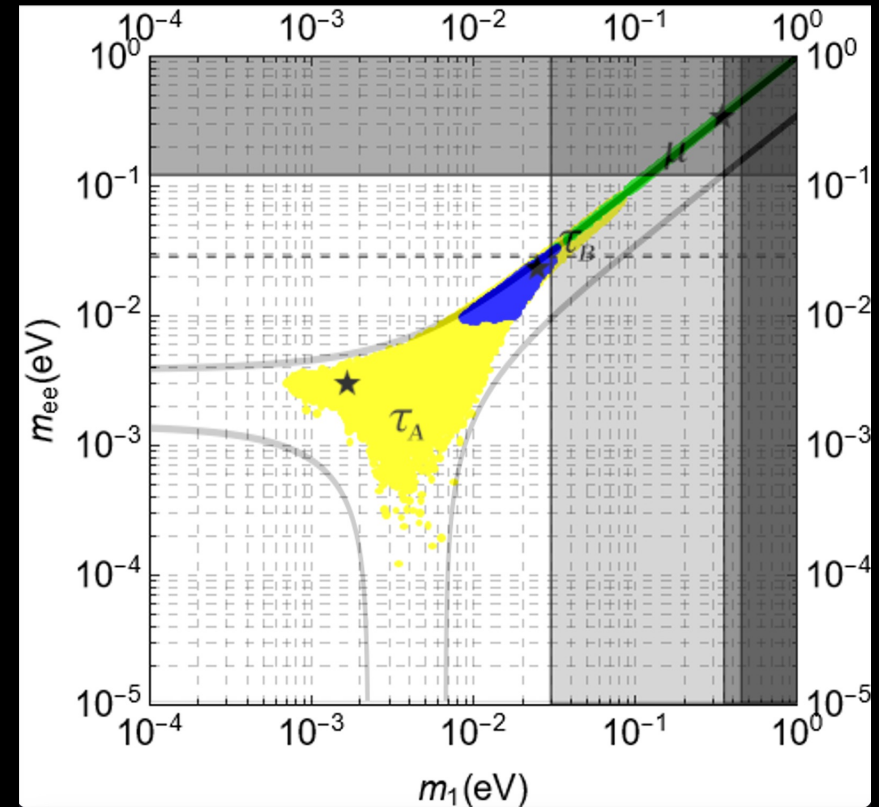
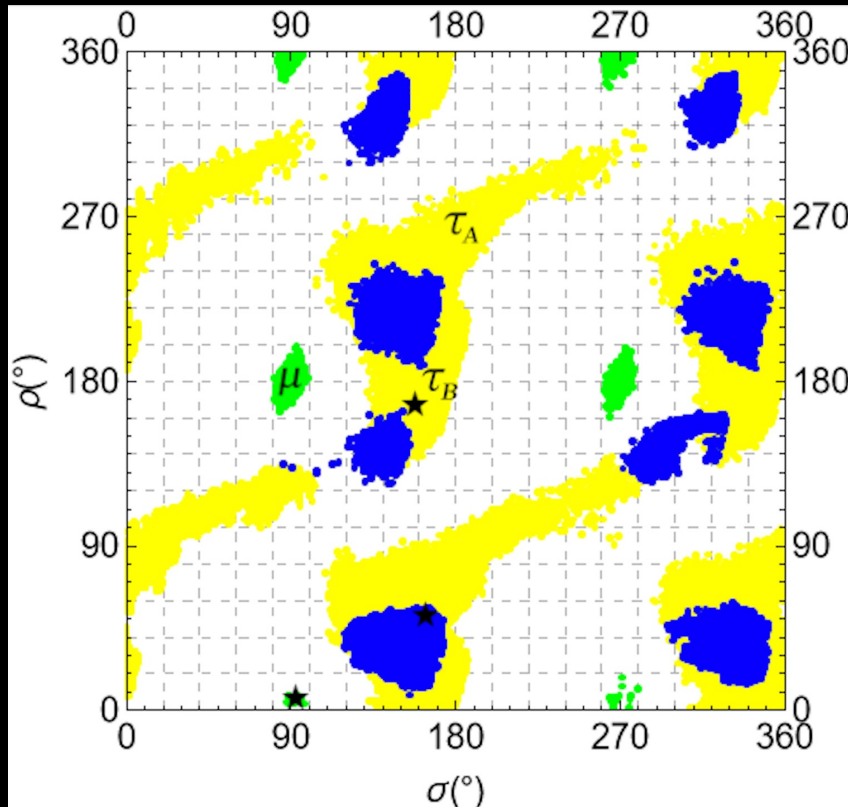
There is a large area in the plane δ vs. θ_{23} where current cosmological upper bound on m_1 would rule out SO(10)-inspired leptogenesis (clear example of testability but and predictive power of the scenario)

Upper bound on the atmospheric mixing angle



For $10 \text{ meV} \lesssim m_1 \lesssim 30 \text{ meV}$ the atmospheric mixing angle has to be in the first octant

Majorana phases and $0\nu\beta\beta$ effective neutrino mass



There are strong constraints on the Majorana phases and this yields a lower bound on m_{ee}

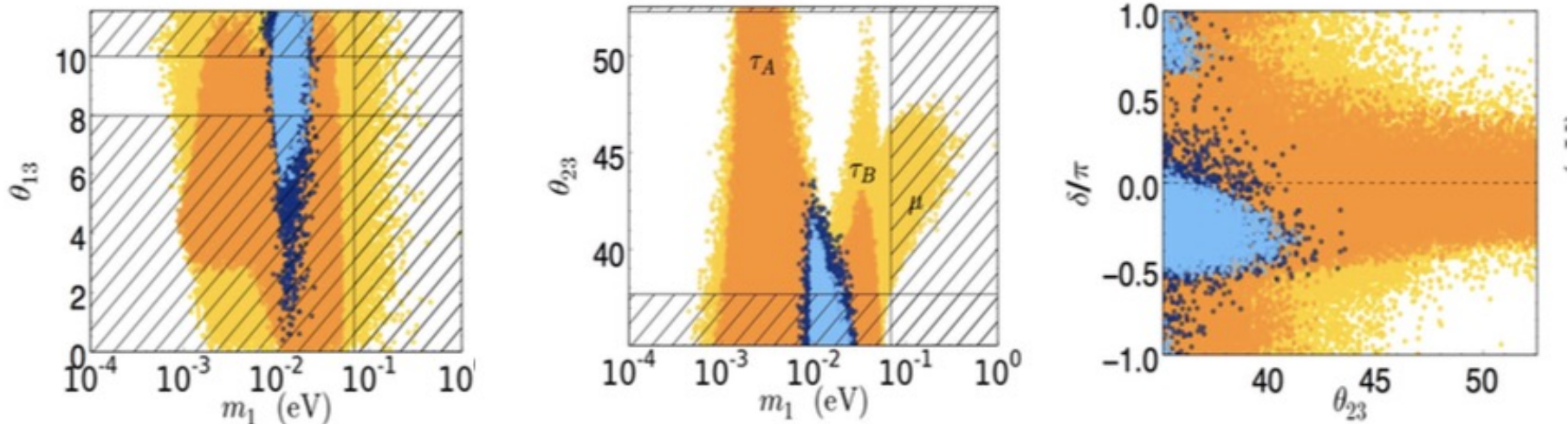
KamLAND2-Zen aims at starting in 2027 improving the upper bound to $m_{ee} < 20 \text{ meV}$ in 5 years (see talk by Shimizu at Neutrino 2024)

Strong thermal $SO(10)$ -inspired leptogenesis

(PDB, Marzola 09/2011, DESY workshop and 1308.1107; PDB, Re Fiorentin, Marzola 1411.5478)

- **Strong thermal leptogenesis** condition can be satisfied for a subset of the solutions only for NORMAL ORDERING

$\alpha_2=5$ □ blue regions: $N_{B-L}^{pre-ex} = 10^{-3}$ ($I \leq V_L \leq V_{CKM}$)



- Absolute neutrino mass scale: $8 \lesssim m_1/\text{meV} \lesssim 30 \Leftrightarrow 70 \lesssim \sum_i m_i/\text{meV} \lesssim 120$
- **Non-vanishing Θ_{13}** (first results presented before Daya Bay discovery)
- Θ_{23} preferably in the first octant;

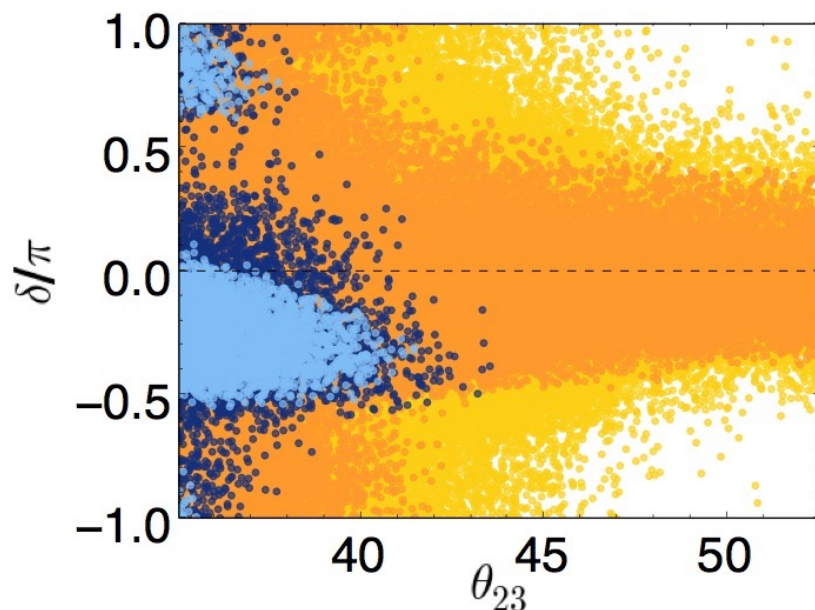
Why do we live in a matter (and not antimatter) dominated universe?

(PDB, Marzola, Re Fiorentin, 1411.5478)

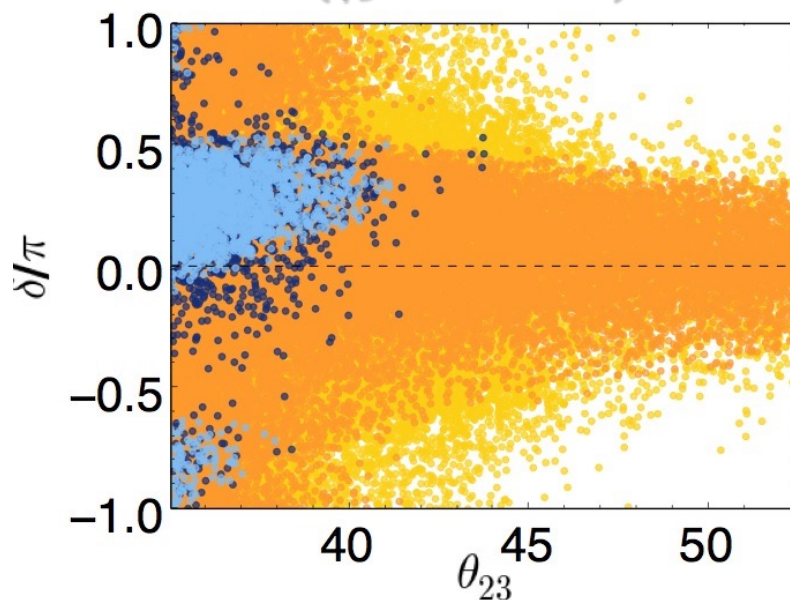
$$\alpha_2=5$$

□ blue regions: $N_{B-L}^{pre-ex} = 10^{-3}$ ($I \leq V_L \leq V_{CKM}$; $V_L = I$)

Matter dominated universe
($\eta_B \sim +6 \times 10^{-10}$)



Antimatter dominated universe
($\eta_B \sim -6 \times 10^{-10}$)



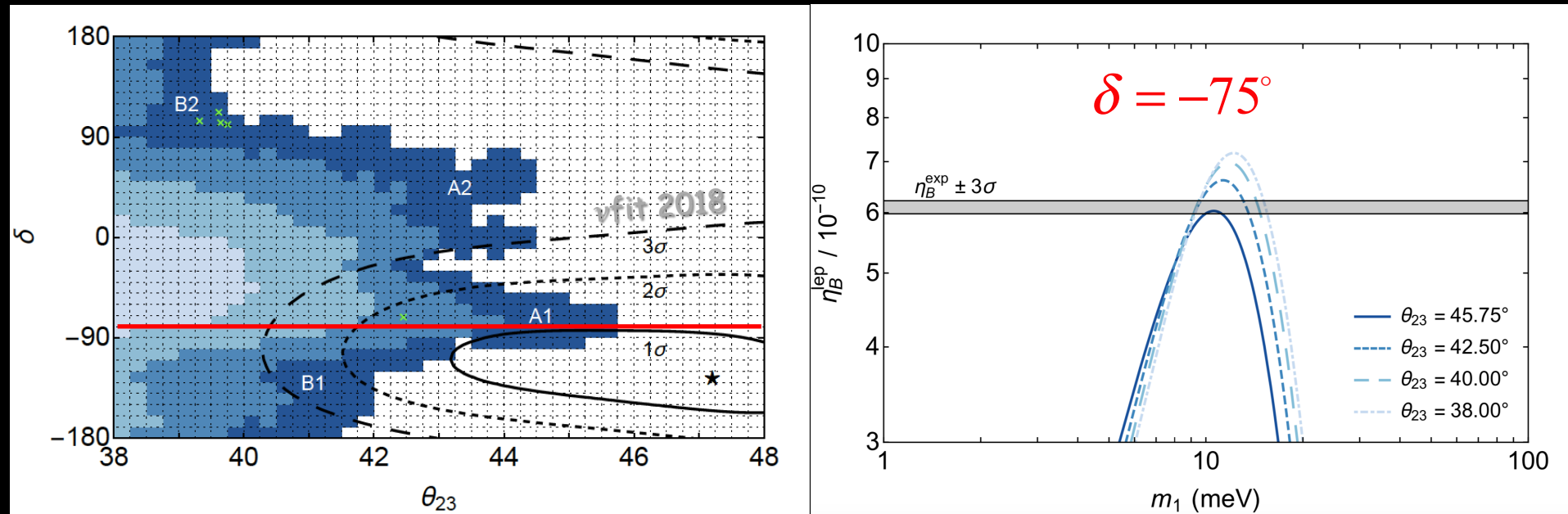
For sufficiently large θ_{23} one has $\text{sign}(\eta_B) = -\text{sign}(\sin \delta)$

\Rightarrow We would live in a matter dominated universe because $\sin \delta < 0$

Strong SO(10)-inspired leptogenesis confronting long baseline experiments (PDB, Marco Chianese 1802.07690)

Pre-existing initial asymmetry: $N_{B-L}^{p,i} = 10^{-3}$

$$\alpha_2 = m_{D2} / m_{charm} = 5$$



"The more stringent experimental lower bound on atmospheric mixing angle starts to corner STSO10-leptogenesis"

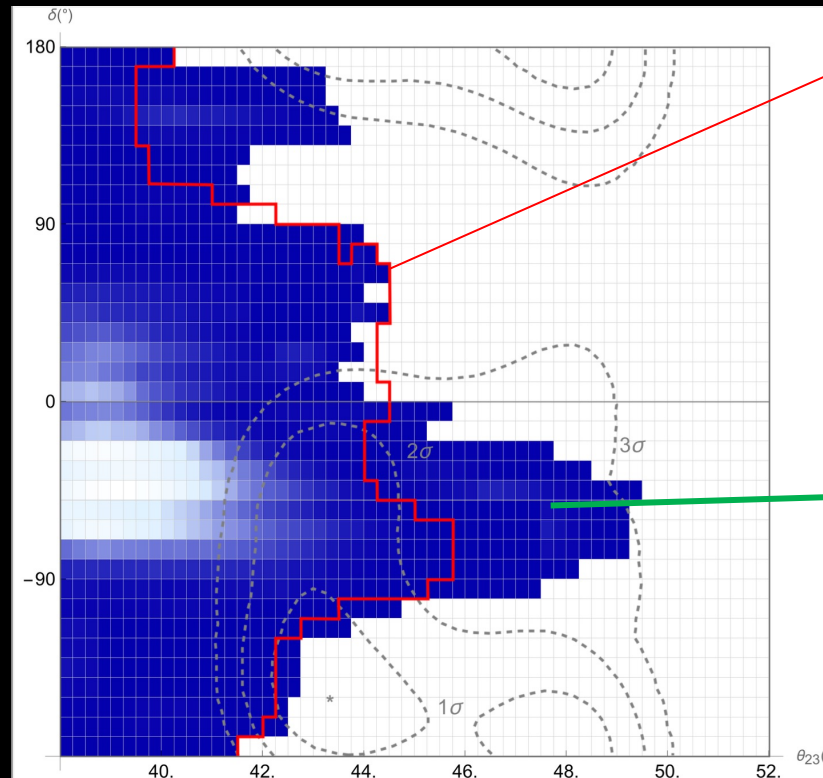
New atmospheric neutrino data seem to remove the tension

(PDB, Xubin Hu, in preparation)

The new SK atmospheric data seem to favour first octant when combined in global analysis (ν fit September 2024) and moreover $\Delta\chi^2(\text{IO-NO})=6.1$: there is a potential interesting overlap now

Pre-existing initial asymmetry: $N_{B-L}^{p,i} = 10^{-3}$

$$\alpha_2 = m_{D2} / m_{\text{charm}} = 5$$



"old" solutions confirmed (no flavour coupling effects)

new solutions found including flavour coupling

Is the asymmetry correctly calculated?

There are 4 main effects that are neglected in the calculation of the asymmetry:

- Flavour coupling effects from spectator processes
- Radiative corrections and running of the parameters
- Full density matrix calculation
- Momentum dependence

Each of these effects is expected to give corrections without changing the main features. At the same time they slow down the calculation and scatter plots with millions of points are hard to obtain including all of them.

Including flavour coupling

(Antusch, PDB, Jones and King 2010)

The Higgs asymmetry acts in inverse decays indistinctly on any flavour so if you produce an asymmetry in one flavour then inverse decays will **generate** an asymmetry also in the other two flavours

The evolution of the flavour asymmetries gets coupled:

$$\frac{dN_{\Delta_\alpha}}{dz_1} = -P_{1\alpha}^0 \sum_{\beta} C_{\alpha\beta}^{(3)} W_1^{\text{ID}} N_{\Delta_\beta} ,$$

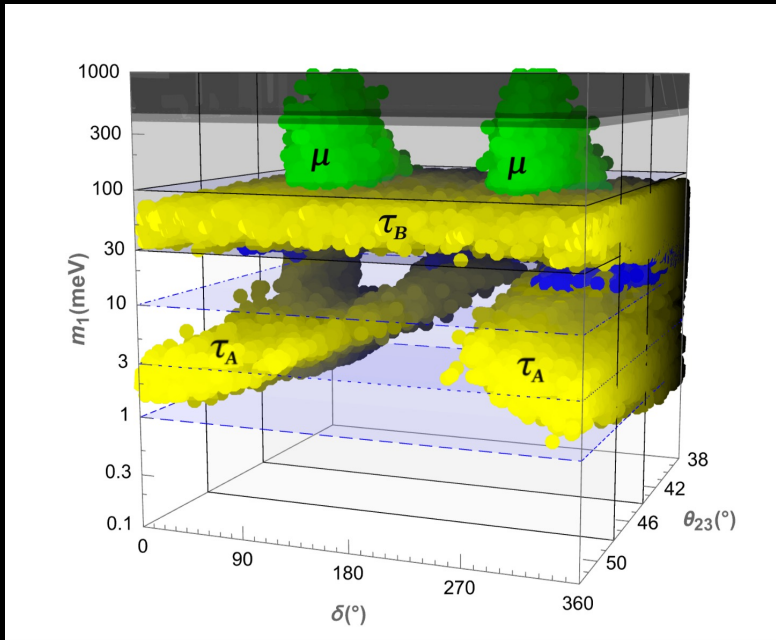
The solution for the asymmetry in one flavour now contains 9 terms instead of just one (i.e., the total B-L asymmetry contains 27 terms)

$$\begin{aligned} N_{\Delta_\alpha}^f &= V_{\alpha e''}^{-1} \left[\sum_{\beta} V_{e''\beta} N_{\Delta_\beta}^{T \sim T_L} \right] e^{-\frac{3\pi}{8} K_{1e''}} \\ &+ V_{\alpha \mu''}^{-1} \left[\sum_{\beta} V_{\mu''\beta} N_{\Delta_\beta}^{T \sim T_L} \right] e^{-\frac{3\pi}{8} K_{1\mu''}} \\ &+ V_{\alpha \tau''}^{-1} \left[\sum_{\beta} V_{\tau''\beta} N_{\Delta_\beta}^{T \sim T_L} \right] e^{-\frac{3\pi}{8} K_{1\tau''}} . \end{aligned}$$

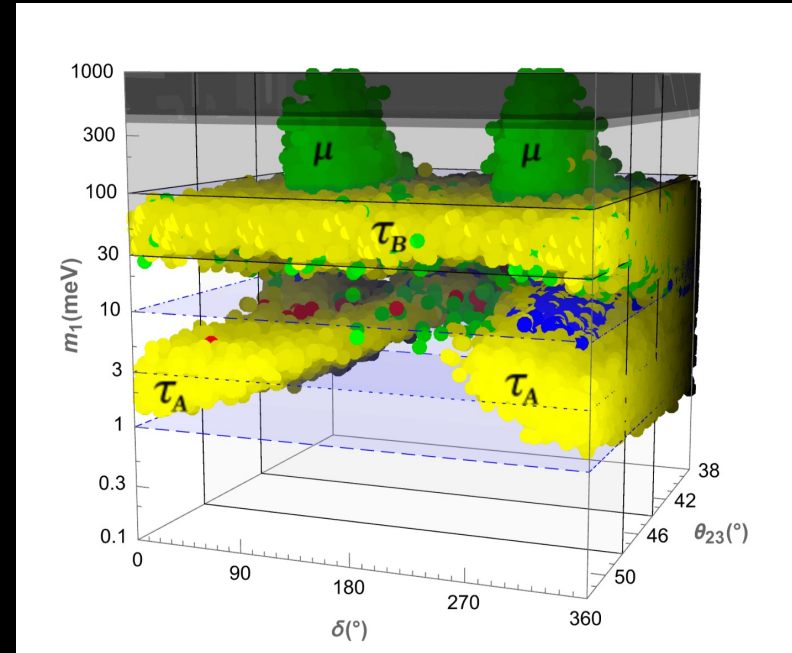
3-dim projection of the allowed region (NO)

$\alpha_2=5$ NORMAL ORDERING $I \leq V_L \leq V_{CKM}$

Without flavour coupling



With flavour coupling

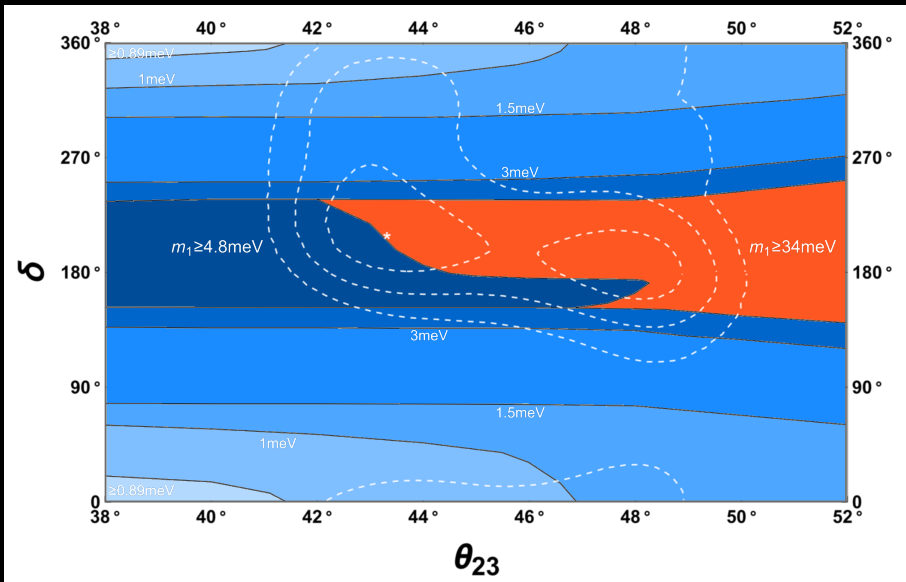


(PDB, Xubin Hu 2507.06144)

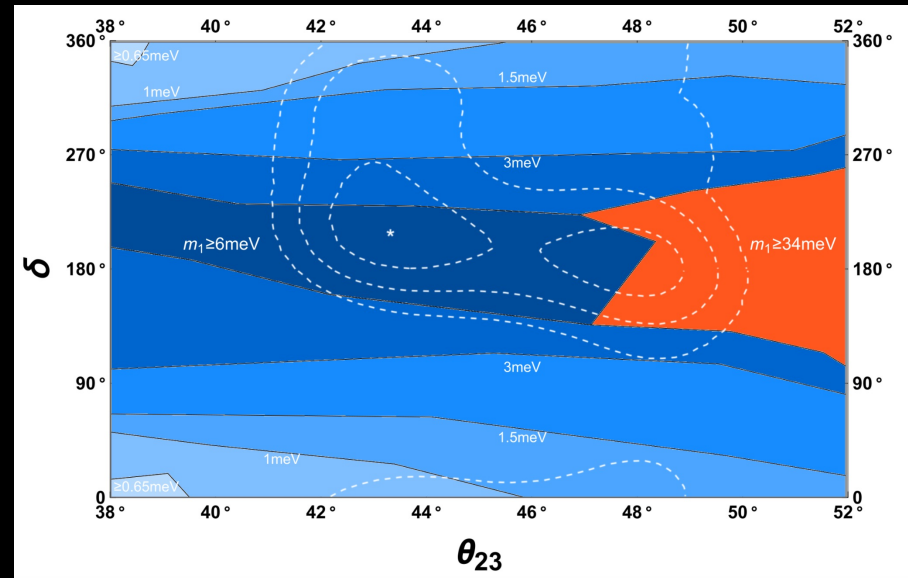
Including flavour coupling, new muonic solutions appear and even some very marginal electron solutions (red points)

SO(10)-inspired leptogenesis confronting long baseline and absolute neutrino mass experiments

Without flavour coupling



With flavour coupling



(PDB, Xubin Hu 2507.06144)

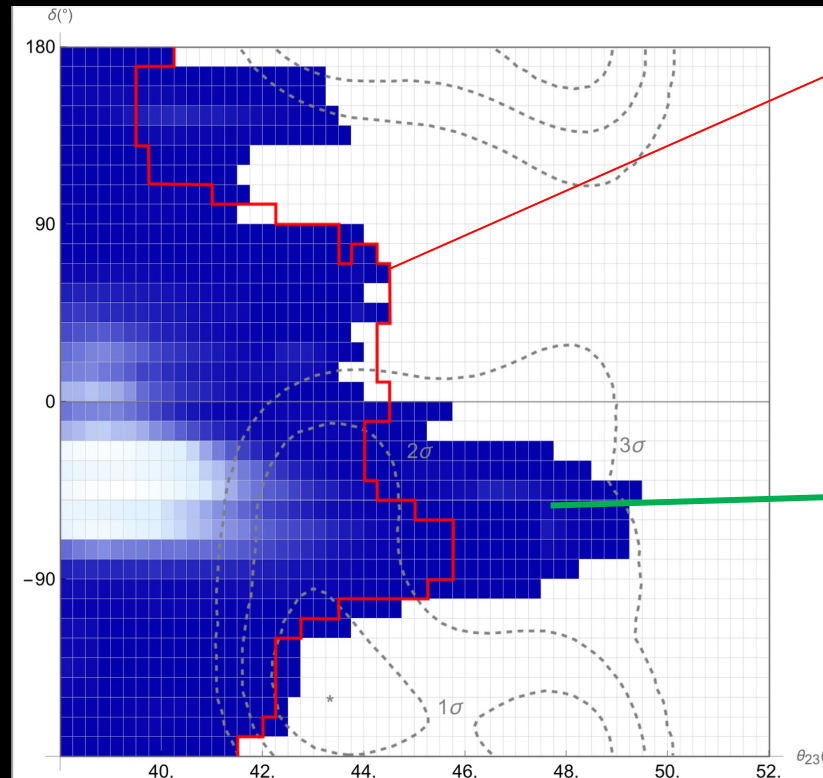
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"old" solutions confirmed (no flavour coupling effects)

new solutions found including flavour coupling

Leptogenesis in SO(10) with a minimal Yukawa sector

(Babu, Bajc, Saad, 1612.04329; K Babu, PDB, C.S. Fong, S. Saad 2409.03840)

- The most attractive models realizing SO(10)-inspired leptogenesis areSO(10) models !
- SO(10) unifies all fermions of a generation into a single spinorial 16-dimensional representation that, in addition to SM fermions, contains 1 RH neutrino: it naturally predicts 3 RH neutrino species
- Masses of fermions arise from Yukawa interactions of two 16s with vevs of suitable Higgs fields. Since:

$$16 \otimes 16 = 10_S \oplus \overline{126}_S \oplus 120_A$$

⇒ The Higgs fields of renormalizable SO(10) models can belong to 10-, 126-, 120-dim representations yielding Yukawa part of the Lagrangian

$$\mathcal{L}_Y = 16 (Y_{10} 10_H + Y_{126} \overline{126}_H + Y_{120} 120_H) 16.$$

- After SSB of the fermions at $M_{\text{GUT}} = 2 \times 10^{16}$ GeV one obtains the masses:

up-quark mass matrix

down-quark mass matrix

neutrino mass matrix

charged lepton mass matrix

RH neutrino mass matrix

$$\begin{aligned} M_u &= v_{10}^u Y_{10} + v_{126}^u Y_{126} + v_{120}^u Y_{120}, \\ M_d &= v_{10}^d Y_{10} + v_{126}^d Y_{126} + v_{120}^d Y_{120}, \\ M_D &= v_{10}^u Y_{10} - 3v_{126}^u Y_{126} + v_{120}^D Y_{120}, \\ M_l &= v_{10}^d Y_{10} - 3v_{126}^d Y_{126} + v_{120}^l Y_{120}, \\ M_R &= v_{126}^R Y_{126}, \end{aligned}$$

→ Simplest case but clearly non-realistic: it predicts no mixing at all (both in quark and lepton Sectors). For realistic models one has to add at least the 126 contribution

A recent realistic fit

(K Babu, PDB, C.S. Fong, S. Saad 2409.03840)

Observables (Δm_{ij}^2 in eV^2)	Values at M_Z scale		
	Input	Benchmark Fit: NO	Benchmark Fit: IO
$y_u/10^{-6}$	6.65 ± 2.25	7.30	10.0
$y_c/10^{-3}$	3.60 ± 0.11	3.59	3.57
y_t	0.986 ± 0.0086	0.986	0.986
$y_d/10^{-5}$	1.645 ± 0.165	1.636	1.635
$y_s/10^{-4}$	3.125 ± 0.165	3.122	3.148
$y_b/10^{-2}$	1.639 ± 0.015	1.639	1.637
$y_e/10^{-6}$	2.7947 ± 0.02794	2.7945	2.7906
$y_\mu/10^{-4}$	5.8998 ± 0.05899	5.9011	5.9080
$y_\tau/10^{-2}$	1.0029 ± 0.01002	1.0022	1.0023
$\theta_{12}^{\text{CKM}}/10^{-2}$	22.735 ± 0.072	22.729 ($\theta_{12}^{\text{CKM}} = 13.023^\circ$)	22.730 ($\theta_{12}^{\text{CKM}} = 13.023^\circ$)
$\theta_{23}^{\text{CKM}}/10^{-2}$	4.208 ± 0.064	4.206 ($\theta_{23}^{\text{CKM}} = 2.401^\circ$)	4.204 ($\theta_{23}^{\text{CKM}} = 2.408^\circ$)
$\theta_{13}^{\text{CKM}}/10^{-3}$	3.64 ± 0.13	3.64 ($\theta_{13}^{\text{CKM}} = 0.208^\circ$)	3.64 ($\theta_{13}^{\text{CKM}} = 0.208^\circ$)
δ_{CKM}	1.208 ± 0.054	1.209 ($\delta_{\text{CKM}} = 69.322^\circ$)	1.212 ($\delta_{\text{CKM}} = 69.457^\circ$)
$\Delta m_{21}^2/10^{-5}$	7.425 ± 0.205	7.413	7.506
$\Delta m_{31}^2/10^{-3}$ (NO)	2.515 ± 0.028	2.514	-
$\Delta m_{32}^2/10^{-3}$ (IO)	-2.498 ± 0.028	-	-2.499
$\sin^2 \theta_{12}$	0.3045 ± 0.0125	0.3041 ($\theta_{12} = 33.46^\circ$)	0.3067 ($\theta_{12} = 33.63^\circ$)
$\sin^2 \theta_{23}$ (NO)*	0.5705 ± 0.0205	0.4473 ($\theta_{23} = 41.98^\circ$)	-
$\sin^2 \theta_{23}$ (IO)*	0.576 ± 0.019	-	0.5784 ($\theta_{23} = 49.51^\circ$)
$\sin^2 \theta_{13}$ (NO)	0.02223 ± 0.00065	0.02223 ($\theta_{13} = 8.57^\circ$)	-
$\sin^2 \theta_{13}$ (IO)	0.02239 ± 0.00063	-	0.02238 ($\theta_{13} = 8.60^\circ$)
δ_{CP}° (NO)	207.5 ± 38.5	240.49	-
δ_{CP}° (IO)	284.5 ± 29.5	-	263.49
$\eta_B/10^{-10}$	$6.12 \pm 0.04^\dagger$	7.6 (7.6)	9.6 (51)
χ^2	-	1.45	5.76 [†]

For NO:

light neutrino masses

$$m_1 = 0.038 \text{ meV}$$

$$m_2 = 8.6 \text{ meV}$$

$$m_3 = 50.1 \text{ meV}$$

$$m_{ee} = 3.7 \text{ meV}$$

heavy neutrino masses

$$M_1 = 6.6 \times 10^4 \text{ GeV}$$

$$M_2 = 2.1 \times 10^{12} \text{ GeV}$$

$$M_3 = 8.1 \times 10^{14} \text{ GeV}$$

Why is the lower bound on m_1 violated? Because $\theta_{23}^L \simeq 45^\circ \Rightarrow$ extended $SO(10)$ -insp. lep.

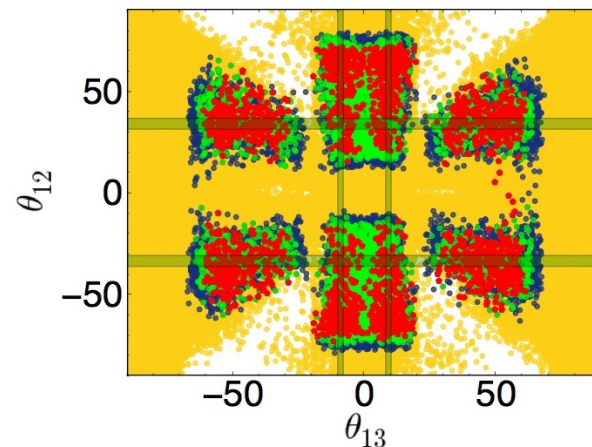
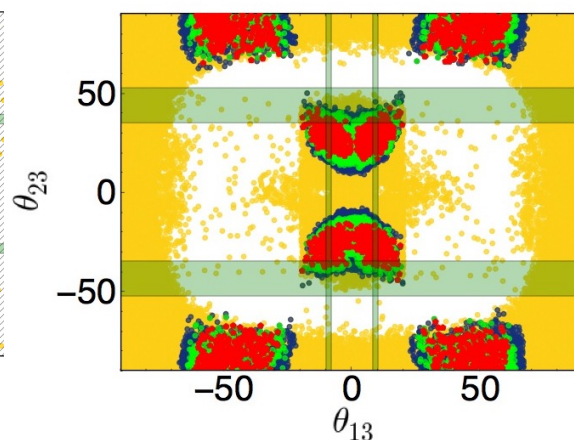
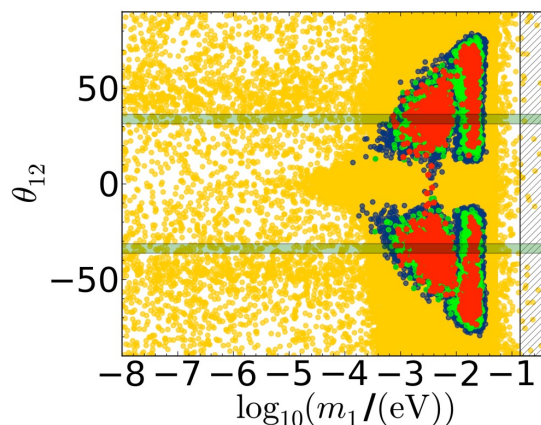
Conclusions

- The matter-antimatter asymmetry puzzle might be related to an explanation of neutrino masses that seems today the most attractive scenario. Discovery of $0\nu\beta\beta$ would be the crucial experimental discovery.
- $SO(10)$ -inspired leptogenesis provides a well motivated class of scenarios relying on N_2 -leptogenesis. They lead to interesting predictions, in particular there is a lower bound on the absolute neutrino mass scale and we are now starting to probe the bulk of the solutions with absolute neutrino mass scale experiments. NO should be confirmed.
- A subset of the solutions realizes strong thermal leptogenesis: highly non-trivial. In this case the atmospheric neutrino mixing angle should be strictly in the first octant and CP Dirac phase in the 4th quadrant. $0\nu\beta\beta$ signal should be within reach of next generation experiments.
- Account of flavour coupling introduces new solutions but does not change the overall picture.
- $SO(10)$ -inspired leptogenesis can be realized within a realistic minimal $SO(10)$ model. In this case the $\theta_{23,L} \sim 45^\circ$: does it signal the presence of additional discrete symmetry?

How significantly can the STSO10 solution be supported by data?

(PDB, Marzola '13)

($N_{B-L}^P = 0, 0.001, 0.01, 0.1$)



If θ_{23} is found in the first octant then $p \lesssim 10\%$

If NO is confirmed then $p \lesssim 5\%$

If δ is measured in the fourth quadrant $p \lesssim 1\%$

This would sum up to the coincidence $m_{\text{sol}}, m_{\text{atm}} \sim 10 m_*$

If also absolute neutrino mass scales (m_1 and m_{ee}) will fall within the expected range (implying $0\nu\beta\beta$ signal) then strong case for discovery (notice also that Majorana phases impose non arbitrary m_{ee}/m_1)

What about if one gives up strong thermal leptogenesis?

A popular class of SO(10) models

(Fritzsch, Minkowski, Annals Phys. 93 (1975) 193-266; R.Slansky, Phys.Rept. 79 (1981) 1-128; G.G. Ross, GUTs, 1985; Dutta, Mimura, Mohapatra, hep-ph/0507319; G. Senjanovic hep-ph/0612312)

In SO(10) models each SM particles generation + 1 RH neutrino are assigned to a single 16-dim representation. Masses of fermions arise from Yukawa interactions of two 16s with vevs of suitable Higgs fields. Since:

$$16 \otimes 16 = 10_S \oplus \overline{126}_S \oplus 120_A,$$

The Higgs fields of renormalizable SO(10) models can belong to 10-, 126-, 120-dim representations yielding Yukawa part of the Lagrangian

$$\mathcal{L}_Y = 16 (Y_{10} 10_H + Y_{126} \overline{126}_H + Y_{120} 120_H) 16.$$

After SSB of the fermions at $M_{\text{GUT}} = 2 \times 10^{16}$ GeV one obtains the masses:

up-quark mass matrix

$$M_u = v_{10}^u Y_{10} + v_{126}^u Y_{126} + v_{120}^u Y_{120},$$

down-quark mass matrix

$$M_d = v_{10}^d Y_{10} + v_{126}^d Y_{126} + v_{120}^d Y_{120},$$

neutrino mass matrix

$$M_D = v_{10}^u Y_{10} - 3v_{126}^u Y_{126} + v_{120}^D Y_{120},$$

charged lepton mass matrix

$$M_l = v_{10}^d Y_{10} - 3v_{126}^d Y_{126} + v_{120}^l Y_{120},$$

RH neutrino mass matrix

$$M_R = v_{126}^R Y_{126},$$

LH neutrino mass matrix

$$M_L = v_{126}^L Y_{126},$$

Simplest case but clearly non-realistic: it predicts no mixing at all (both in quark and lepton Sectors). For realistic models one has to add at least the 126 contribution

NOTE: these models do respect SO(10)-inspired conditions

Charged lepton flavour effects

(Barbieri et al '98; Abada et al '06; Nardi et al. '06; Blanchet, PDB, Raffelt '06; Riotto, De Simone '06)

Flavor composition of lepton quantum states matters!

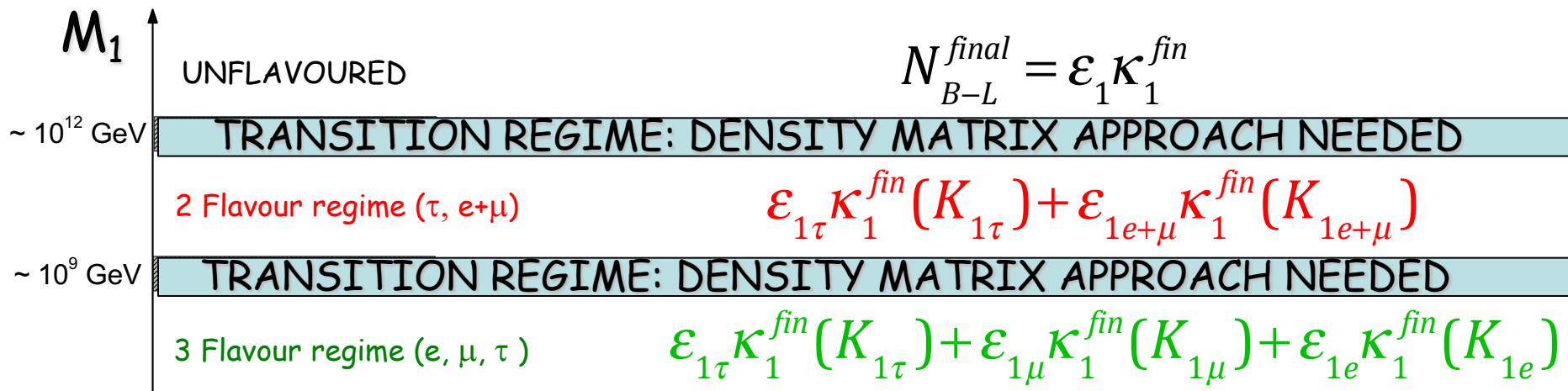
$$|l_1\rangle = \sum_{\alpha} \langle l_{\alpha} | l_1 \rangle |l_{\alpha}\rangle \quad (\alpha = e, \mu, \tau)$$

$$|\bar{l}_1\rangle = \sum_{\alpha} \langle l_{\alpha} | \bar{l}_1 \rangle |\bar{l}_{\alpha}\rangle$$

□ $T \ll 10^{12} \text{ GeV} \Rightarrow \tau$ -Yukawa interactions are fast enough break the coherent evolution of $|l_1\rangle$ and $|\bar{l}_1\rangle$

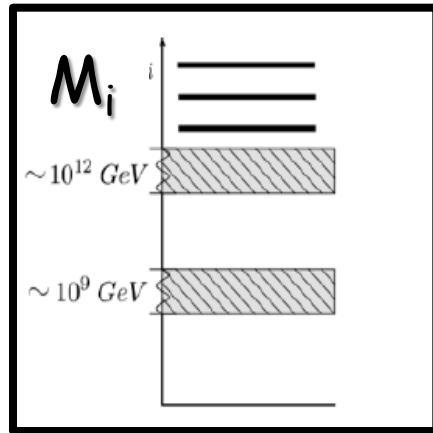
\Rightarrow incoherent mixture of a τ and of a $\nu + e$ components \Rightarrow 2-flavour regime

□ $T \ll 10^9 \text{ GeV}$ then also ν -Yukawas in equilibrium \Rightarrow 3-flavour regime



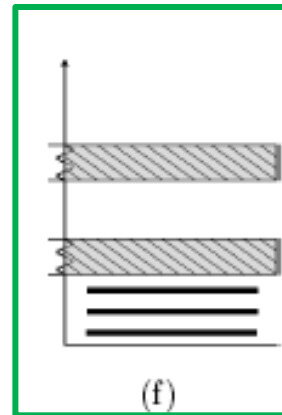
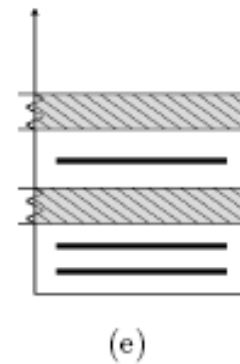
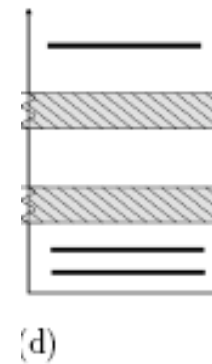
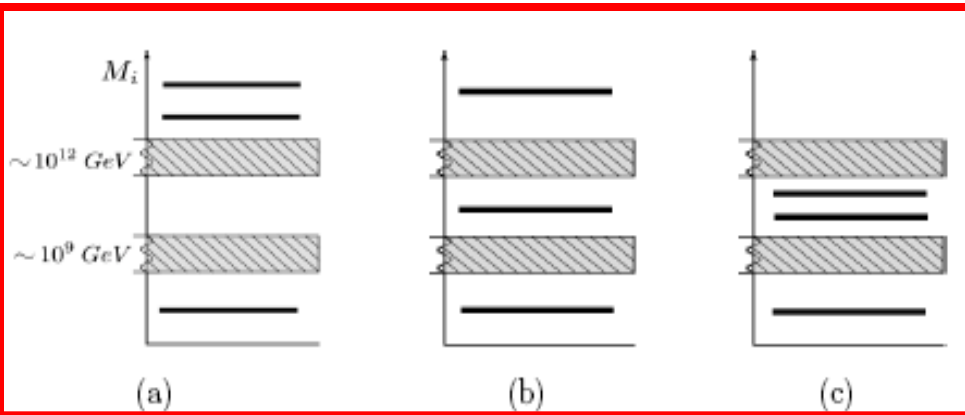
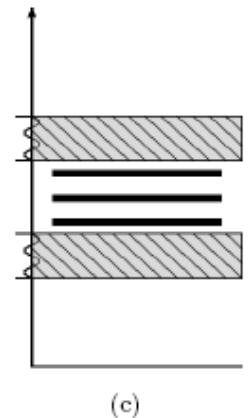
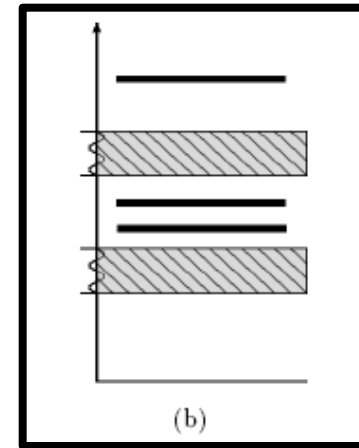
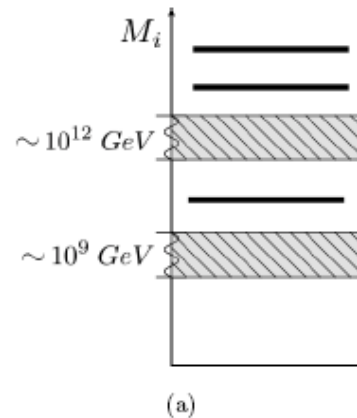
Heavy neutrino lepton flavour effects: 10 scenarios

Heavy neutrino flavored scenario



Typically rising in discrete flavour symmetry models

2 RH neutrino scenario

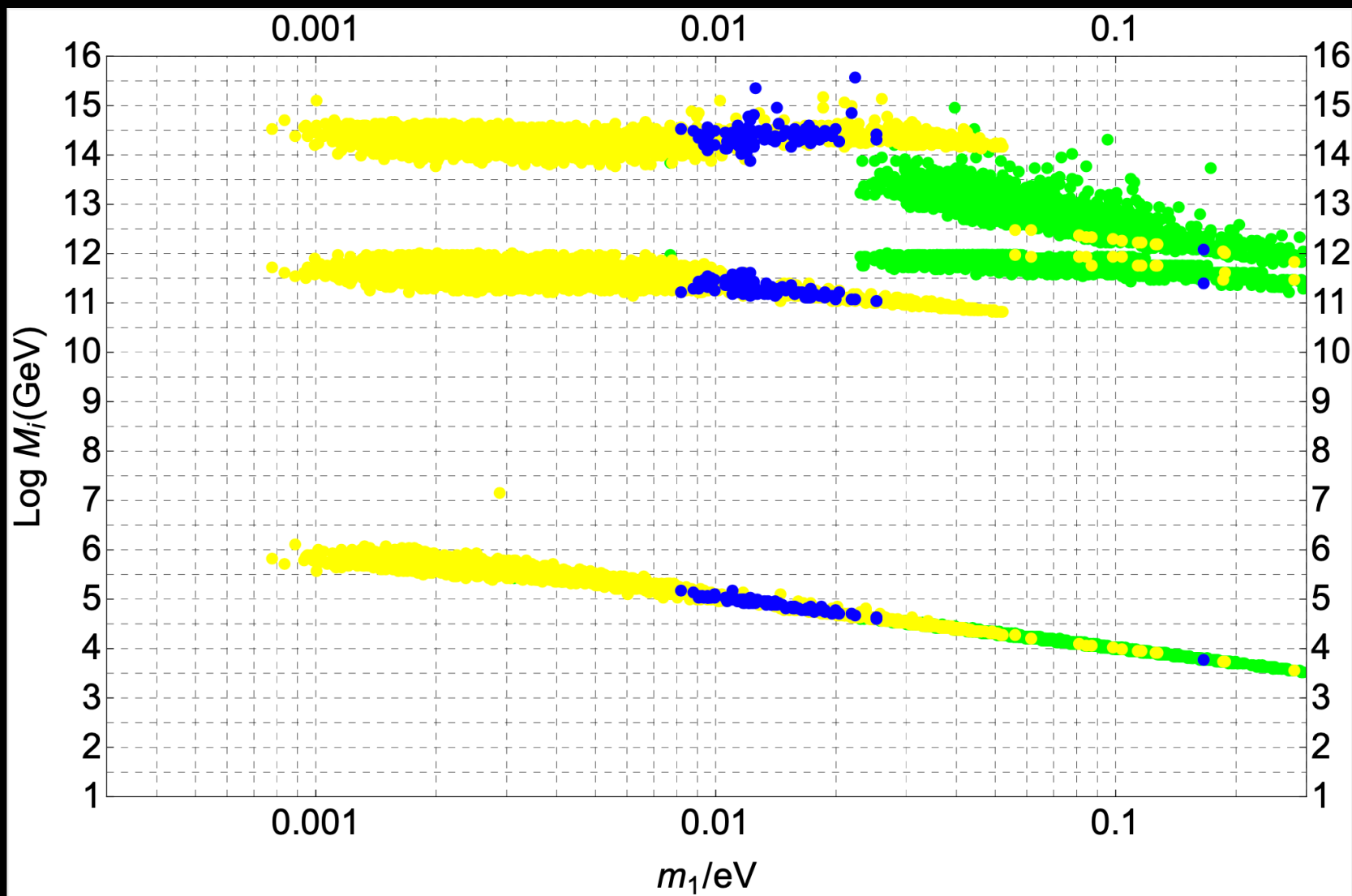


N_2 -dominated scenario:

■ N_1 produces negligible asymmetry;

Low scale leptogenesis

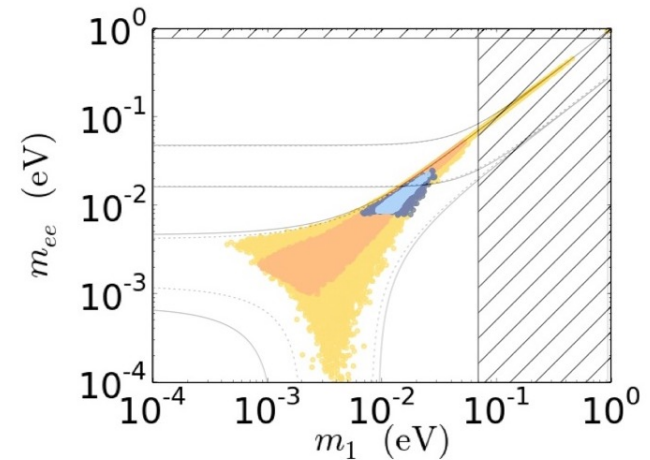
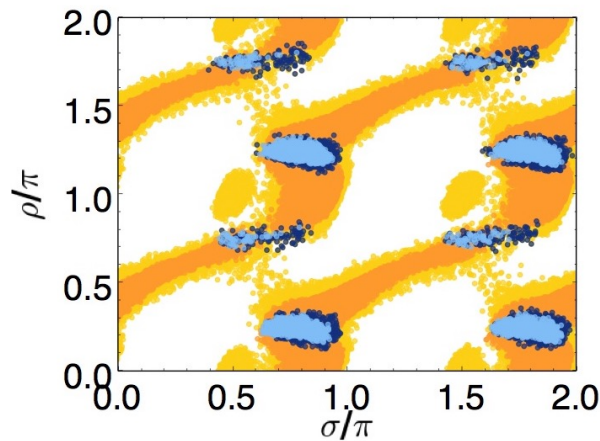
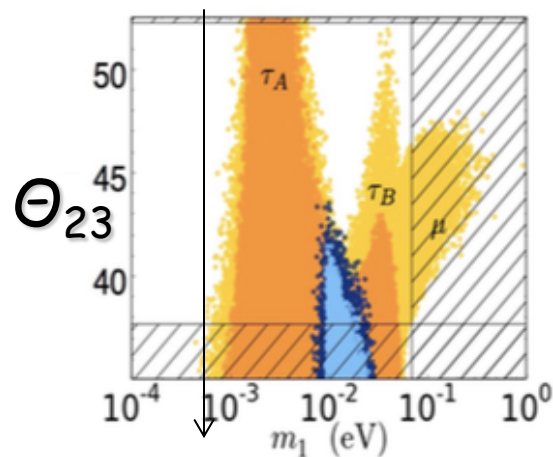
Examples: Resonant+ARS leptogenesis



N_2 -leptogenesis rescues $SO(10)$ -inspired leptogenesis

(PDB, Riotto 0809.2285;1012.2343;He,Lew,Volkas 0810.1104)

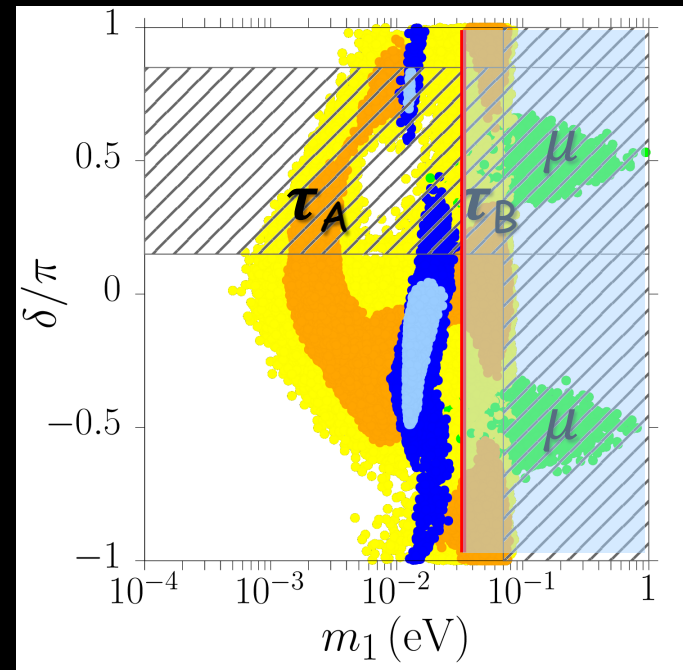
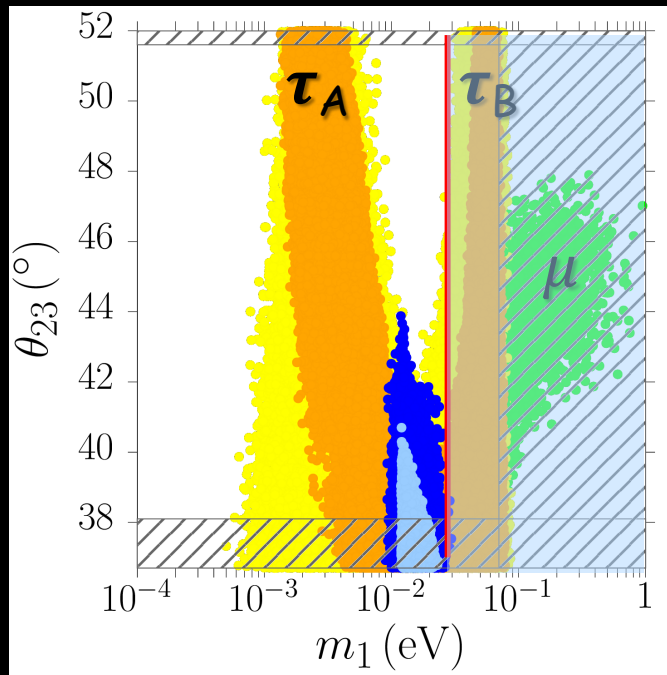
- dependence on α_1 and α_3 cancels out \Rightarrow
the asymmetry depends only on $\alpha_2 \equiv m_{D2}/m_{\text{charm}}$: $\eta_B \propto \alpha_2^2$
- $\alpha_2=5$ NORMAL ORDERING $I \leq V_L \leq V_{\text{CKM}}$ $V_L = I$



- Lower bound $m_1 \gtrsim 10^{-3} \text{ eV}$
- θ_{23} upper bound
- Majorana phases constrained in specific regions
- Effective $0\nu\beta\beta$ mass can still vanish but bulk of points above meV
- **INVERTED ORDERING IS EXCLUDED** (it requires too large sum of neutrino masses + too large θ_{23})
- Tauon + muon-dominated solutions
- Strong thermal leptogenesis is realised for a subset of tauon solutions (blue points)

SO(10)-inspired leptogenesis confronting long baseline and absolute neutrino mass experiments

$$\alpha_2=5$$

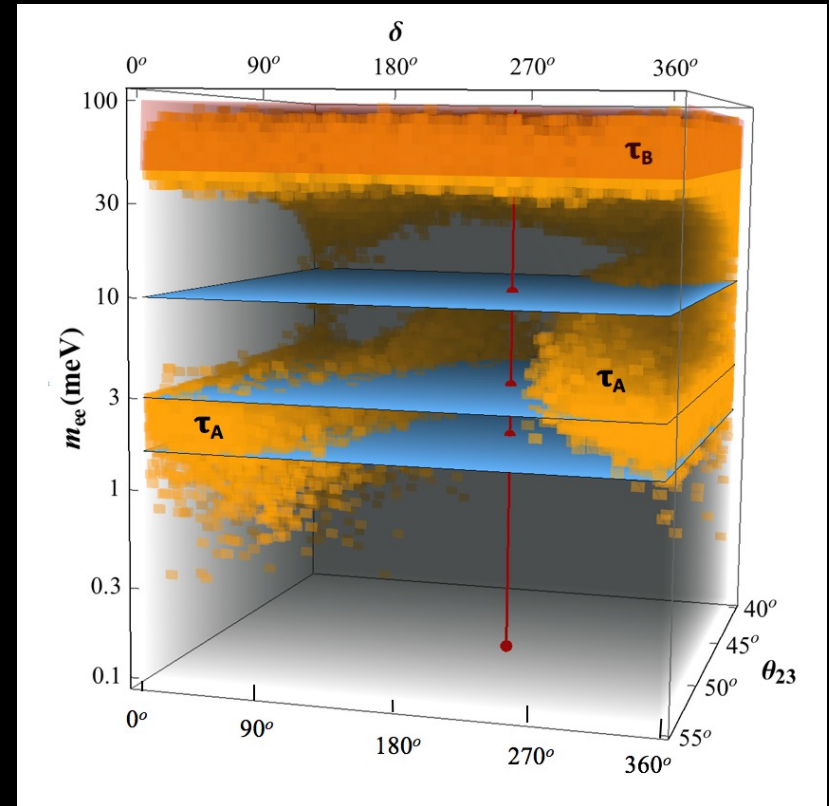
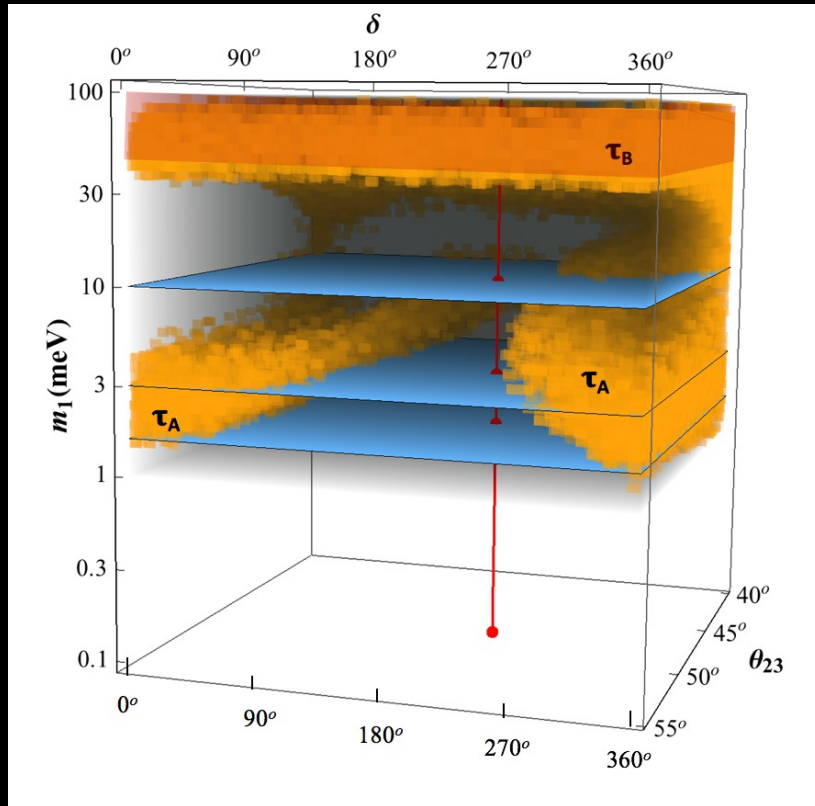


Projecting the allowed region (an hypersurface in the space of neutrino parameters) on planes can hide a more complex structure corresponding potentially to stronger predictions.

SO(10)-inspired leptogenesis confronting long baseline and absolute neutrino mass experiments.....in 3D

(PDB, R. Samanta 2005.03057)

$$\alpha_2=5$$

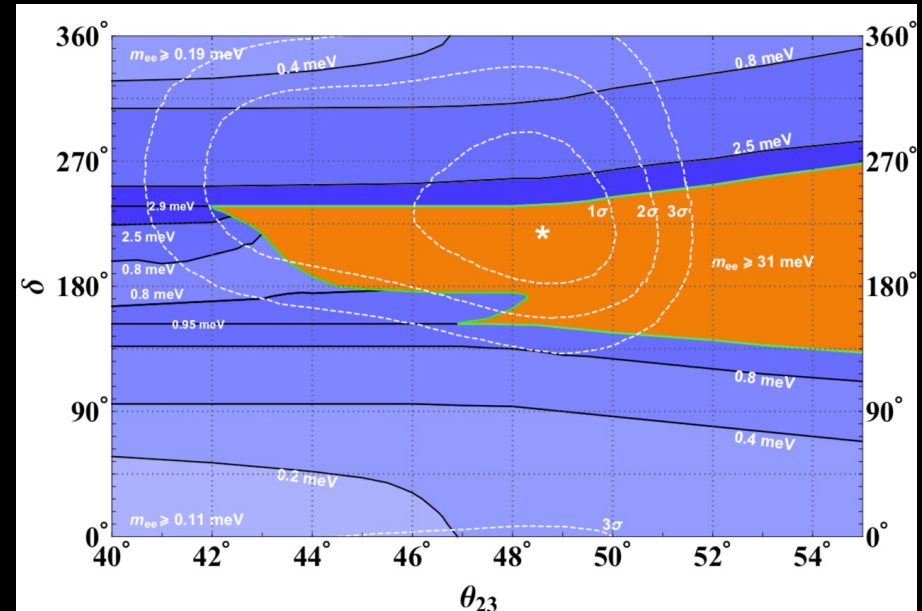
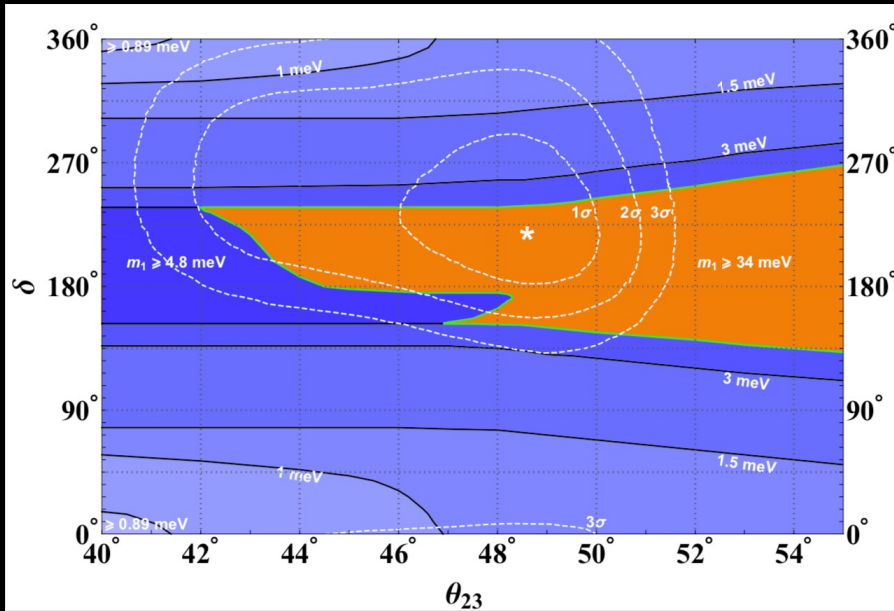


For certain values of δ and θ_{23} the lower bound on the absolute neutrino mass scale is much more stringent: $m_1, m_{ee} \gtrsim 30$ meV

SO(10)-inspired leptogenesis: lower bound on the absolute neutrino mass scale as a function of δ and θ_{23}

(PDB, R. Samanta 2005.03057)

$$\alpha_2 = 5$$



Future precise measurements of δ and θ_{23} will have an important impact on SO(10)-inspired leptogenesis, in particular a precise determination of δ might be crucial. Ultimately if measured neutrino mixing parameters will lie on the hypersurface (implying $0\nu\beta\beta$ discovery) a strong case for discovery can be made (this has to take into account also $\theta_{13}, \theta_{12}, m_{\text{sol}}, m_{\text{atm}}$)

Notice that CP conserving values of δ are possible since CP violation comes from high energy phases (they can be identified with those in the orthogonal matrix)