High Resolution Space-Time Ozone Modeling for Assessing Trends

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ABSTRACT

This paper proposes a space-time model for daily 8-hour maximum ozone levels to provide input for regulatory activities: detection, evaluation, and analysis of spatial patterns and temporal trend in ozone summaries. The model is applied to the analysis of data from the state of Ohio which contains a mix of urban, suburban, and rural ozone monitoring sites. The proposed space-time model is auto-regressive and incorporates the most important meteorological variables observed at a collection of ozone monitoring sites as well as at several weather stations where ozone levels have not been observed. This misalignment is handled through spatial modeling. In so doing we adopt a computationally convenient approach based on the successive daily increments in meteorological variables. The resulting hierarchical model is specified within a Bayesian framework and is fitted using MCMC techniques. Full inference with regard to model unknowns as well as for predictions in time and space, evaluation of annual summaries and assessment of trends are presented.

Key Words: Dynamic model; forecasting/prediction; Markov chain Monte Carlo; misalignment; spatial variability; stationarity.

1 Introduction

In this paper, we develop a new spatial-temporal model for predicting spatial patterns and associated uncertainties in ozone concentrations and for detecting long term trends. Here, we use data observed from 1997-2004 for the state of Ohio at ozone monitoring sites located in a variety of urban, suburban, and rural settings. We use several important meteorological variables observed at some of the ozone monitoring sites and also at sites where ozone has not been observed, e.g., several airports in Ohio and neighboring states. We address the

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spatial and temporal misalignment of the pollution and meteorological data through spatial modeling. This allows us to develop a disaggregated model that takes a novel form by relating current day ozone concentration to previous day ozone (auto-regressive part), an annual intercept term, an incremental effect due to meteorology, and a spatially correlated error term. As we clarify in Section 3.1, this avoids the potentially contentious issue of direct modeling of meteorology and focuses on modeling successive daily increments for a set of meteorological variables, a more straightforward task. In all of this we infer about latent "true" ozone levels used to define the ozone standard (see below), recognizing that observed levels may introduce missingness, bias error and measurement error. The current ozone standard is met if the 3-year rolling average of the annual 4th highest daily maximum 8-hour true average ozone concentration is less than 80 parts per billion (ppb), see e.g. epa.gov/air/criteria.html.

By modeling daily ozone concentrations, we can easily aggregate to any desired temporal summary of ozone, particularly the summary underlying the ozone air quality standard and hence study trends in such summaries. Note that, unlike other models that seek to examine trends (see below), we learn about trend without having to assume any functional form for it. By using space-time modeling, we can interpolate or predict ozone levels at any location in the state, again to whatever desired temporal summary. As a result, we achieve the most highly resolved (with regard to both space and time) analysis of ozone yet developed. A byproduct of our high resolution modeling is the potential to link predicted true ozone concentrations to adverse health outcomes (see, e.g. Bell et al., 2004). Daily predictions of true average ozone at arbitrary locations, which we can provide, offer a source of information for modeling such linkage. Moreover, by capturing uncertainty at such resolution and implementing inference within the Bayesian framework, we immediately obtain the uncertainty associated with any aggregation.

Lastly, space-time process modeling for ozone levels achieves a, perhaps less appreciated, benefit with regard to investigating extremes, such as the annual fourth highest daily average. Non-model based interpolation of extremes, as would be done with monitoring data using standard software packages to create spatial surfaces, will tend to smooth them out, resulting in underestimation of the extent of noncompliance. The space-time dependence structure associated with process modeling is more effective in retaining the extremes of the latent ozone surfaces. (See Section 5 in this regard.)

More specifically, this paper develops and illustrates several notions of site-specific summaries and trend surfaces over a large spatial domain. We consider spatial patterns in the annual 4th highest daily maxima 8-hour ozone concentrations and in the 3-year rolling averages defined above, across Ohio. Spatial patterns for the 3-year rolling averages can be examined for overall changes across the period 1997-2004 to assess trends in the ozone surface over time periods when emission reductions have been in place. Further, our modeling approach can be used to study site-specific trends by adjusting predicted ozone concentrations for meteorological effects where those have been observed. In this regard, we could

attempt direct spatio-temporal modeling of extreme levels and for instance, in recent work of Gilleland and Nychka (2005) using generalized extreme value distributions. However, extremes need not be our only interest; the proposed high resolution modeling enables more general assessment of ozone patterns in space and time.

Space-time modeling of air pollutants, ground level ozone concentrations in particular, has attracted recent attention, see, e.g., Guttorp et al. (1994), and Carroll et al. (1997). In recent years, hierarchical Bayesian approaches for spatial prediction of air pollution have been developed, see, e.g. Brown et al., (1994), Sahu and Mardia (2005), Sahu et al. (2006) and references therein. McMillan et al. (2005) propose a regime switching model for ozone forecasting using meteorological variables as covariates and they illustrate using data from April to September in 1999 over a spatial domain covering Lake Michigan. They do not explicitly model the meteorological variables but their method requires them as input possibly obtained from weather forecast data. They work with data projected to a grid and then introduce a "nearest-neighbor" spatial model; as a result, interpolation is precluded. With one year of data, their methodology is suitable for short-term forecasting of ozone but they are unable to investigate trends.

Cox and Chu (1992) used a generalized linear model approach, assuming a conditional Weibull distribution for ozone concentrations given meteorology, to estimate trends in daily maximum ozone levels. Porter et al. (2001) reported on the estimation of trends in ozone concentrations adjusted for meteorological variables at individual monitoring sites. These authors used a moving average, Kolmogorov-Zurbenko filter, to separate a baseline component of log transformed ozone consisting of long-term trend and seasonal variation from short-term weather variation. Cocchi et al. (2005) followed the approach of Huang and Smith (1999) by using a tree based partitioning of daily maxima ozone concentrations and assumed these maxima are Weibull distributed. Trend of ozone maxima is evaluated at a single site in Italy in terms of the sequence of yearly variations of medians within groups having homogeneous meteorology. A comprehensive overview of statistical methods for the statistical adjustment of ground-level ozone is given by Thompson et al. (2001). Huerta et al. (2004) model hourly readings of concentrations of ozone jointly with air temperature for data from Mexico City. Their approach uses a dynamic linear model with seasonal harmonics which enables simultaneous forecasting of ozone and air temperature. Zhu et al. (2003) relate ambient ozone and pediatric asthma ER visits in Atlanta using hierarchical regression methods for spatially misaligned data. Finally, Wikle (2003) provides an overview of hierarchical modeling in environmental science.

The remainder of this paper is organized as follows. Section 2 presents pertinent exploratory analyses of the data in order to facilitate model development. Our proposed model is developed in Section 3. Bayesian prediction methods and development of trend analysis are detailed in Section 4. Model based analyses are provided in Section 5. A brief summary and future issues to explore are given in Section 6. An appendix contains the computational details.

2 Exploratory Analysis

We model daily maximum 8-hour ozone concentration data obtained from n = 53 sites in the state of Ohio for our analysis. We have ozone data from $n_1 = 50$ National Air Monitoring Stations/State and Local Air Monitoring Stations (NAMS/SLAMS),

epa.gov/cludygxb/programs/namslam.html, and $m_1 = 3$ Clean Air Status and Trends Network (CASTNET), epa.gov/castnet, sites. Most of the NAMS/SLAMS sites are located in or around the big cities whereas the CASTNET sites operate in mostly rural areas. The NAMS/SLAMS network does not record meteorological data whereas the CASTNET sites do. In addition, we have meteorological data from $m_2 = 9$ weather stations which are mostly located near airports. Thus we have ozone data from $n = n_1 + m_1 = 53$ sites and meteorological data from $n_2 = m_1 + m_2 = 12$ sites. All these 62 sites are plotted in Figure 1, (3 CASTNET sites numbered 1, 2, and 3 in the figure are overlapping). Note that there is at least one meteorological station near every cluster of ozone monitoring sites. In fact, two meteorological stations outside the state of Ohio have been kept precisely to achieve this purpose.

We consider data for r=8 years from 1997 to 2004, inclusive. In each year we have data for T=169 days covering the high ozone season from April 15 to September 30. However, 7,832 (=10.93%) of the total N=nrT=71,656 are missing. In particular, about 50% of the data (roughly 4 years) were missing in eight sites; some of these sites started gathering data from 2001. In fact in the years 1997-2000 the percentages of missing values were 22.94, 19.73, 16.70, and 13.61, respectively.

The boxplot of ozone values by year are plotted in Figure 2 which shows the overall levels. The overall level goes up in 1998, comes down to the lowest levels in 2000 and then rises again, but comes down in the year 2004. This pattern is also seen in the annual 4th highest daily maximum 8-hour average concentration levels as well, see top panel of Figure 3. The bottom panel of Figure 3 plots the 3-year rolling averages and we observe evidence of non-attainment (true ozone values greater than 80) in most of the sites in our study period.

Standard multiple regression methods (stepwise, forward and backward selection) were used to choose the most important meteorological variables to include in our model. The four (=p) most important variables are found to be maximum daily temperature in degree centigrade, relative average humidity, wind speeds in the morning and in the afternoon. McMillan et al. (2004) also included these four and the additional variables: average station pressure and wind direction in their work. However, given the four variables above, we did not find these additional variables to be significant in our spatio-temporal analysis for data taken over the eight years, 1997-2004. All the $n_2rTp = 64,896$ values of the successive daily increments of the four meteorological variables were used for our analysis. The time series plots (not included) of these variables are all centered around zero and they do not show any auto-correlation, making those amenable to the independence assumption made

in Section 3.1.

Data from 15 sites (in addition to the 53 modeling sites) have been set aside for validation purposes; these sites are also plotted in Figure 1. They are not included for modeling since about 70.46% observations were missing. In particular, there were only 5,991 available values out of the possible $20,282 \ (=15rT)$ observations.

Histograms and normal QQ plots were plotted on the three measurement scales: original, logarithmic, and square-root. The data on the original scale are surprisingly symmetric, but high variability would lead to negative fitted and predicted ozone concentrations. The log-scale introduces negative skewness. The square-root scale seems most attractive both in terms of symmetry and stabilizing the variance so that there are no negative fitted or predicted ozone values. This is in accord with other work in modeling air pollutants, see e.g. Sahu et al. (2006).

3 Model Development

We use the notation $Z_l(\mathbf{s},t)$ to denote the observed square-root ozone concentration at location \mathbf{s} , in year l on day t. We have $t=1,\ldots,T=169$ and $l=1,\ldots,8$. We model data from n=53 stations denoted by $\mathbf{s}_1,\ldots,\mathbf{s}_n$, all within Ohio. Further, let $O_l(\mathbf{s},t)$ denote the true value corresponding to $Z_l(\mathbf{s},t)$. Let $x_{lj}(\mathbf{s},t)$ and $\delta_{lj}(\mathbf{s}_i,t)$ denote respectively the value of the jth meteorological variable and the increment, $j=1,\ldots,p$ in year l on day t. That is, $\delta_{lj}(\mathbf{s}_i,t)=x_{lj}(\mathbf{s}_i,t)-x_{lj}(\mathbf{s}_i,t-1)$. We shall use the following vector notations: $\mathbf{Z}_{lt}=(Z_l(\mathbf{s}_1,t),\ldots,Z_l(\mathbf{s}_n,t))'$, $\mathbf{O}_{lt}=(O_l(\mathbf{s}_1,t),\ldots,O_l(\mathbf{s}_n,t))'$, $\mathbf{x}_l(\mathbf{s}_i,t)=(x_{l1}(\mathbf{s}_i,t),\ldots,x_{lp}(\mathbf{s}_i,t))'$, and $\delta_l(\mathbf{s}_i,t)=\mathbf{x}_l(\mathbf{s}_i,t)-\mathbf{x}_l(\mathbf{s}_i,t-1)$.

To handle missingness along with potential bias and measurement error, we assume:

$$Z_l(\mathbf{s}_i, t) = O_l(\mathbf{s}_i, t) + \epsilon_l(\mathbf{s}_i, t), \quad i = 1, \dots, n, \quad t = 1, \dots, T, \tag{1}$$

where $\epsilon_l(\mathbf{s}_i,t)$ is a white noise process, specifically assumed to follow $N(0,\sigma_{\epsilon}^2)$ independently. Thus σ_{ϵ}^2 is the so called nugget effect. The Gaussian error assumption may be a concern due to occasional large excursions in ozone concentration levels. The use of square root transformation helps in this regard. However, it is possible to use a non-Gaussian error model for the $\epsilon_l(\mathbf{s}_i,t)$'s such as a t-process. Regardless, preliminary residual analysis suggests that it is plausible to take σ_{ϵ}^2 to be homogeneous in space and time.

Next, we turn to the modeling for $O_l(\mathbf{s},t)$. There is high auto-correlation between ozone measurements on successive days, hence, we include an auto-regressive term in our model. We also introduce a global (not site specific) annual intercept parameter. However, the residuals after fitting such a model will show significant local variation. From the Introduction, we anticipate that this arises primarily due to changes in local meteorological conditions. However, we also introduce space-time random effects to allow for other unobserved but consequential local variables, enabling spatio-temporally varying intercepts.

Thus, we assume that,

$$O_l(\mathbf{s}, t) = \rho O_l(\mathbf{s}, t - 1) + \xi_l + \delta_l'(\mathbf{s}, t)\beta + \eta_l(\mathbf{s}, t), \quad t = 2, \dots, T,$$
(2)

where $\eta_l(\mathbf{s},t)$ is a spatially correlated error term, $\rho O_l(\mathbf{s},t-1)$ is the auto-regressive term with $0 < \rho < 1$, ξ_l is the global annual intercept in year l, and $\delta'_l(\mathbf{s},t)\boldsymbol{\beta}$ is the local adjustment to $O_l(\mathbf{s},t)$ arising due to the increments in meteorological variables $\mathbf{x}_l(\mathbf{s},t)$. In principle, nonlinear functions of change in meteorology could be employed. However, these may be hard to interpret and, furthermore, out of sample model validation suggests that our flexible model is adequate.

Clarification of the dynamic model defined by (1) and (2) may be helpful. We are modeling true ozone dynamically to suggest that ozone differentials are explained by meteorology differentials. The meteorology differentials are not modeled dynamically. Another approach, arguably more demanding and more open to criticism, would be to build a dynamic weather model and then treat true ozone at time t to be conditionally independent given the weather at time t. Expressed in different terms, for us, $O_l(\mathbf{s}, t-1)$ serves as a proxy for many other unobserved explanatory variables for ozone concentration levels.

The auto-regressive models require an initial condition for $O_l(\mathbf{s}, 1)$, the first value in year l. We assume the following model:

$$O_l(\mathbf{s}, 1) = \mu_l + \gamma_l(\mathbf{s}) \tag{3}$$

where $\gamma_l(\mathbf{s})$ is the additional regional effect in year l at site \mathbf{s} over a global level μ_l . Note that we could instead adopt a "random walk" model for $O_l(\mathbf{s}, t)$, e.g.,

$$O_l(\mathbf{s},t) - \mathbf{x}'_l(\mathbf{s},t)\boldsymbol{\beta} = O_l(\mathbf{s},t-1) - \mathbf{x}'_l(\mathbf{s},t-1)\boldsymbol{\beta} + \eta_l(\mathbf{s},t)$$
i. e. $O_l(\mathbf{s},t) = O_l(\mathbf{s},t-1) + \boldsymbol{\delta}'_l(\mathbf{s},t-1)\boldsymbol{\beta} + \eta_l(\mathbf{s},t)$. (4)

This model corresponds to setting $\rho = 1$ in (2) and eliminates the need for the ξ_l 's. However, we find the fixing of ρ to be unsatisfactory. (Indeed, model comparison using model choice and validation showed considerably poorer performance for (4) compared with (2).) In essence, the $\rho = 1$ model is nonstationary, yielding prediction/forecasting that is explosive in time. As a noteworthy aside, inference regarding the β 's is essentially the same in (2) and (4). Intuitively, using $O_l(\mathbf{s}, t - 1)$ to explain $O_l(\mathbf{s}, t)$ with a 45° line through the origin or with a more flexible line would not be expected to much affect how the meteorology variables explain $O_l(\mathbf{s}, t)$. Empirically, it is observed in comparing the two fitted models.

A second alternative is to change the right side of (4) to $\rho(O_l(\mathbf{s}, t-1) - \mathbf{x}'_l(\mathbf{s}, t-1)\boldsymbol{\beta})$ in the spirit of (2). However, we can see that this model does not permit us to work with incremental meteorology; it would force us to model the meteorology which we seek to avoid. (Again, see Section 3.1.) So, in the sequel, we confine ourselves to the specifications in (2) and (3).

Now we write the above models using vectors and matrices to facilitate computation. The first model equation is obtained from (1):

$$\mathbf{Z}_{lt} = \mathbf{O}_{lt} + \boldsymbol{\epsilon}_{lt}, l = 1, \dots, r, \ t = 1, \dots, T, \tag{5}$$

where $\epsilon_{lt} = (\epsilon_l(\mathbf{s}_1, t), \dots, \epsilon_l(\mathbf{s}_n, t))'$. Let **1** be the vector of dimension n with all elements unity and $\boldsymbol{\gamma}_l = (\gamma_l(\mathbf{s}_1), \dots, \gamma_l(\mathbf{s}_n))'$. From (3) and (2) we have, respectively

$$\mathbf{O}_{l1} = \boldsymbol{\gamma}_l + \mu_l \mathbf{1}, \ l = 1, \dots r, \tag{6}$$

$$\mathbf{O}_{lt} = \xi_l \mathbf{1} + \rho \, \mathbf{O}_{lt-1} + F_{lt} \boldsymbol{\beta} + \boldsymbol{\eta}_{lt}, \ l = 1, \dots, t = 2, \dots, T.$$
 (7)

where $\boldsymbol{\beta} = (\beta_1, \dots, \beta_p)', \, \boldsymbol{\eta}_{lt} = (\eta_l(\mathbf{s}_1, t), \dots, \eta_l(\mathbf{s}_n, t))'$ and

$$F_{lt} = \left(egin{array}{c} oldsymbol{\delta_l'(\mathbf{s}_1,t)} \ oldsymbol{\delta_l'(\mathbf{s}_2,t)} \ dots \ oldsymbol{\delta_l'(\mathbf{s}_n,t)} \end{array}
ight) = \left(egin{array}{cccc} \delta_{l1}(\mathbf{s}_1,t) & \delta_{l2}(\mathbf{s}_1,t) & \cdots & \delta_{lp}(\mathbf{s}_1,t) \ \delta_{l1}(\mathbf{s}_2,t) & \delta_{l2}(\mathbf{s}_2,t) & \cdots & \delta_{lp}(\mathbf{s}_2,t) \ dots & dots & dots & dots \ \delta_{l1}(\mathbf{s}_n,t) & \delta_{l2}(\mathbf{s}_n,t) & \cdots & \delta_{lp}(\mathbf{s}_n,t) \end{array}
ight).$$

For the measurement error in (5) we assume that $\epsilon_{lt} \sim N(\mathbf{0}, \sigma_{\epsilon}^2 I_n)$, $l = 1, \ldots, r$, $t = 1, \ldots, T$, independently, where $\mathbf{0}$ is the vector with all elements zero and I_n is the identity matrix of order n. For the spatially correlated error we assume that $\boldsymbol{\eta}_{lt} \sim N(\mathbf{0}, \Sigma_{\eta})$, $l = 1, \ldots, r$, $t = 2, \ldots, T$ independently, where Σ_{η} has elements $\sigma_{\eta}(i, j) = \sigma_{\eta}^2 \rho(\mathbf{s}_i - \mathbf{s}_j; \phi_{\eta})$. We take $\rho(\mathbf{s}_i - \mathbf{s}_j; \phi_{\eta}) = \rho(d_{ij}, \phi_{\eta}) = \exp(-\phi_{\eta} d_{ij})$ where d_{ij} is the distance between sites \mathbf{s}_i and \mathbf{s}_j , $i, j = 1, \ldots, n$. We acknowledge the simplification associated with choosing the exponential covariance structure, however, other members of the Matèrn family of covariance functions can be chosen.

Finally we assume that $\gamma_l \sim N(\mathbf{0}, \ \Sigma_l), \ l=1,\ldots,r$ independently, where $\Sigma_l = \sigma_l^2 \Sigma_{\gamma}$ and Σ_{γ} has elements $\Sigma_{\gamma}(i,j) = \rho_{\gamma}(\mathbf{s}_i - \mathbf{s}_j; \phi_{\gamma})$. As before we assume that, $\rho_{\gamma}(\mathbf{s}_i - \mathbf{s}_j; \phi_{\gamma}) = \exp(-\phi_{\gamma}d_{ij})$. The parameters ϕ_{η} and ϕ_{γ} are determined using cross-validation as discussed in Section 5.1.

3.1 Specification for $\delta_l(\mathbf{s},t)$

It is a highly complex problem to model a multi-dimensional meteorological variable over a large spatial domain for a number years. Numerical models based on a large number of input parameters are often implemented in a super-computer to produce many aspects of climate forecasting. It is beyond a reasonable scope for our work to attempt to replicate such climate models, to attempt dynamic modeling of the meteorological variables $\mathbf{x}_l(\mathbf{s},t)$ at the un-observed sites. Instead, we specify spatially correlated but temporally independent models for the increments $\boldsymbol{\delta}_l(\mathbf{s},t)$.

¹The use of an isotropic covariance function for the residual process in an autoregressive, local meteorology adjusted model seems reasonable. Of course, alternate choices could be examined.

In particular, recall that we have only observed the p-dimensional increments in meteorological variables, $\delta_l(\mathbf{s},t)$, in each year l and on each day t in n_2 sites of which m_1 are CASTNET sites and m_2 weather stations. We order the sites so that first n_1 are NAMS/SLAMS sites where $\delta_l(\mathbf{s},t)$ has not been observed, the next m_1 sites are the CASTNET sites and the last m_2 sites are weather stations.

Based on our exploratory analysis, as mentioned in Section 2, we assume that each of these $\delta_l(\mathbf{s},t)$ are independently normally distributed with zero mean. The p components of $\delta_l(\mathbf{s},t)$'s, however, will have correlation with each other. In addition, we expect them to be spatially associated with spatial decay that may vary with component. Hence, we need to specify and estimate correlation structures between components, $k \neq k' = 1, \ldots, p$, $\delta_{lk}(\mathbf{s}_i,t)$ and $\delta_{lk'}(\mathbf{s}_j,t)$ for any given year l and day t. We assume that the correlation structure is not influenced by the true ozone values (or their transformations), $O_l(\mathbf{s},t)$. Hence, in order to estimate the parameters describing the correlation structure of $\delta_l(\mathbf{s},t)$ we only use the observations $\delta_l(\mathbf{s},t)$ observed at n_2 sites over all the years, $l=1,\ldots,r$ and the days $t=1,\ldots,T$. We now specify the correlation structure and discuss its estimation.

The correlation structure within the p-components of $\delta_l(\mathbf{s},t)$ at any given \mathbf{s} , l and t can be described, without loss of generality, by a $p \times p$ lower-triangular matrix A, say, where $A = (\mathbf{a}_1, \mathbf{a}_2, \cdots, \mathbf{a}_p)$. (This is the so-called coregionalization matrix discussed in, e.g., Gelfand et al., 2004.) Let $\rho_k(\mathbf{s}_i - \mathbf{s}_j; \phi_k)$ denote the correlation between $\delta_{lk}(\mathbf{s}_i, t)$ and $\delta_{lk}(\mathbf{s}_j, t)$. For convenience, we adopt the exponential covariance structure, i.e. $\rho_k(\mathbf{s}_i - \mathbf{s}_j; \phi_k) = \exp(-\phi_k d_{ij}), k = 1, \ldots, p$ where d_{ij} is the distance between the sites \mathbf{s}_i and \mathbf{s}_j . As a result, we obtain the cross-covariance function between $\delta_l(\mathbf{s}_i, t)$ and $\delta_l(\mathbf{s}_j, t)$, $\operatorname{Cov}(\delta_l(\mathbf{s}_i, t), \delta_l(\mathbf{s}_j, t)) \equiv C(\mathbf{s}_i - \mathbf{s}_j) = \sum_{k=1}^p \rho_k(\mathbf{s}_i - \mathbf{s}_j; \phi_k) T_k$ where $T_k = \mathbf{a}_k \mathbf{a}_k'$. Let $\delta_{lt} = \left(\left(\delta_{lt}^{(1)}\right)', \left(\delta_{lt}^{(2)}\right)'\right)'$ where $\delta_{lt}^{(1)} = \left(\delta_l'(\mathbf{s}_1, t), \ldots, \delta_l'(\mathbf{s}_{n_1}, t)\right)'$ and $\delta_{lt}^{(2)} = \left(\delta_l'(\mathbf{s}_{n_1+1}, t), \ldots, \delta_l'(\mathbf{s}_{n_1+n_2}, t)\right)'$. The covariance matrix of δ_{lt} is:

$$\Sigma(\boldsymbol{\delta}) = \left(egin{array}{cccc} AA' & C(\mathbf{s}_1 - \mathbf{s}_2) & \cdots & C(\mathbf{s}_1 - \mathbf{s}_{n_1 + n_2}) \ C(\mathbf{s}_2 - \mathbf{s}_1) & AA' & \cdots & C(\mathbf{s}_2 - \mathbf{s}_{n_1 + n_2}) \ dots & dots & dots & dots \ C(\mathbf{s}_{n_1 + n_2} - \mathbf{s}_1) & C(\mathbf{s}_{n_1 + n_2} - \mathbf{s}_2) & \cdots & AA' \end{array}
ight)$$

By partitioning,

$$\Sigma(oldsymbol{\delta}) = \left(egin{array}{cc} \Sigma_{11}(oldsymbol{\delta}^{(1)}) & \Sigma_{12}(oldsymbol{\delta}^{(1)},oldsymbol{\delta}^{(2)}) \ \Sigma_{21}(oldsymbol{\delta}^{(2)},oldsymbol{\delta}^{(1)}) & \Sigma_{22}(oldsymbol{\delta}^{(2)}) \end{array}
ight),$$

we have that:

$$\boldsymbol{\delta}_{lt}^{(2)} \sim N\left(\mathbf{0}, \ \Sigma_{22}\right),$$
 (8)

$$\boldsymbol{\delta}_{lt}^{(1)} | \boldsymbol{\delta}_{lt}^{(2)} \sim N \left(\Sigma_{12} \Sigma_{22}^{-1} \, \boldsymbol{\delta}_{lt}^{(2)}, \, \, \Sigma_{11} - \Sigma_{12} \Sigma_{22}^{-1} \Sigma_{21} \right), \tag{9}$$

for l = 1, ..., r, and t = 1, ..., T, where we have dropped the arguments for Σ for ease of notation. We also note that from (9) it is easy to obtain the distribution of $\boldsymbol{\delta}_l(\mathbf{s}', t) | \boldsymbol{\delta}_{lt}^{(2)}$ for any arbitrary location \mathbf{s}' , which we shall require for prediction purposes in Section 4.

Equation (8) provides the likelihood specification for estimating the elements in the lower triangular matrix A and the parameters, $\phi_k, k = 1, ..., p$. Let ν denote these parameters and \mathbf{u} denote the observations $\boldsymbol{\delta}_{lt}^{(2)}, l = 1, ..., r, t = 1, ..., T$. We assume $N(0, 10^4)$ for each element in the lower triangle of A and the uniform prior distribution U(0.001, 0.1) for each ϕ_k . (This range was adequate to capture the rates of decay in $\boldsymbol{\delta}_{lk}(\mathbf{s},t), k = 1, ..., p$.) The likelihood (8) and these prior specifications are used to obtain the posterior distribution of ν given \mathbf{u} .

We run the Metropolis-Hastings algorithm to sample from this posterior distribution of ν as follows. Let S_{22} denote the sample covariance matrix of order $n_2p \times n_2p$ obtained from the $rT=8\times 169=1352$ realizations $\delta_{lt}^{(2)}$. The starting values for the elements of A are obtained by taking the first 4×4 sub-matrix of Cholesky decomposition of S_{22} . The starting values of the ϕ parameters are all chosen to be 0.005. The jump sizes for the Metropolis algorithm are tuned to have 40-50% acceptance rates. For our data the proposal variance of the normal proposal distribution for the elements of A is found to be 0.5 to have the desired acceptance rate. (Actual observed rate was 47.45%.) The ϕ parameters are sampled on the log-scale with a uniform proposal distribution with jump size 0.02. Note that this algorithm can be run both before or with the main Gibbs sampler for ozone model fitting. Finally, we can compare the model based estimate (say, the posterior mean) of Σ_{22} with the observed covariance matrix S_{22} to check the quality of model fit. Omitting details, whether we use a histogram of differences or conventional trace or determinant criteria, the suggestion is that the model fits very well. Moreover, we validate the ozone model extensively in Section 5 again producing very satisfactory results.

3.2 Joint Posterior Details

Define N = nrT and M = nr(T-1) and let $\boldsymbol{\vartheta}_{lt} = \xi_l \mathbf{1} + \rho \mathbf{O}_{lt-1} + F_{lt}\boldsymbol{\beta}$, for $l = 1, \ldots, r$ and $t = 2, \ldots T$. Further, let $\boldsymbol{\theta}$ denote all the parameters, $\mu_l, \sigma_l^2, \xi_l, \ l = 1, \ldots, r, \ \boldsymbol{\beta}, \ \rho, \ \sigma_\epsilon^2$, and σ_η^2 . Let \mathbf{w} denote all the augmented data, $\mathbf{o}_{lt}, \ \boldsymbol{\delta}_{lt}^{(1)}$ and the missing data, denoted by $z_l^*(\mathbf{s}_i, t)$, for $i = 1, \ldots, n, \ l = 1, \ldots, r, \ t = 1, \ldots, T$, and \mathbf{z} denote all the non-missing data $z_l(\mathbf{s}_i, t)$, for $i = 1, \ldots, n, \ l = 1, \ldots, r, \ t = 1, \ldots, T$. The log of the posterior distribution, denoted by $\log \pi(\boldsymbol{\theta}, \mathbf{w} | \mathbf{u}, \mathbf{z})$, is written as:

$$\begin{split} &-\frac{N}{2}\log(\sigma_{\epsilon}^{2}) - \frac{1}{2\sigma_{\epsilon}^{2}}\sum_{l=1}^{r}\sum_{t=1}^{T}(\mathbf{Z}_{lt} - \mathbf{O}_{lt})'(\mathbf{Z}_{lt} - \mathbf{O}_{lt}) \\ &-\frac{M}{2}\log(\sigma_{\eta}^{2}) - \frac{1}{2\sigma_{\eta}^{2}}\sum_{l=1}^{r}\sum_{t=2}^{T}(\mathbf{O}_{lt} - \boldsymbol{\vartheta}_{lt})'\Sigma_{\eta}^{-1}(\mathbf{O}_{lt} - \boldsymbol{\vartheta}_{lt}) \\ &-\frac{rT}{2}\log|\Sigma(\boldsymbol{\delta})| - \frac{1}{2}\sum_{l=1}^{r}\sum_{t=1}^{T}\boldsymbol{\delta}_{lt}'\Sigma(\boldsymbol{\delta})^{-1}\boldsymbol{\delta}_{lt} + \log\left(\pi(\rho, \boldsymbol{\beta}, \sigma_{\epsilon}^{2}, \sigma_{\eta}^{2})\right) \\ &+\sum_{l=1}^{r}\left[\log\left(\pi(\mu_{l})\right) + \log\left(\pi(\sigma_{l}^{2})\right) + \log\left(\pi(\xi_{l})\right) - \frac{1}{2}\log|\Sigma_{l}| - \frac{1}{2}\boldsymbol{\gamma}_{l}'\Sigma_{l}^{-1}\boldsymbol{\gamma}_{l}\right] \end{split}$$

where $\pi(\mu_l), \pi(\sigma_l^2), \pi(\xi_l)$, and $\pi(\rho, \boldsymbol{\beta}, \sigma_{\epsilon}^2, \sigma_{\eta}^2)$ are the prior distributions. We assume that a-priori μ_l and ξ_l are independent normally distributed with means 0 and variances 10^4 . The auto-regressive coefficient ρ is specified the $N(0, 10^4)I(0 < \rho < 1), \boldsymbol{\beta} \sim N(\mathbf{0}, 10^4 I_p),$ $\frac{1}{\sigma_{\epsilon}^2} \sim G(a, b), \frac{1}{\sigma_{\eta}^2} \sim G(a, b), \text{ and } \frac{1}{\sigma_l^2} \sim G(a, b), \ l = 1, \ldots, r \text{ independently, where the}$

distribution G(a, b) has mean a/b. In our implementation we take a = 2 and b = 1 to have a proper prior specification for each of these variance components.

4 Prediction Details

4.1 Predicting Ozone at a New Location

Spatial prediction at location \mathbf{s}' and time t' is based upon the predictive distribution of $Z_l(\mathbf{s}',t')$ given in the model equations (1), (2), and (3). These models allow us to interpolate the spatial surface at any time point $t' \geq 1$ in a given year. According to (1), for a new location \mathbf{s}' at time t' $Z_l(\mathbf{s}',t')$, has the distribution:

$$Z_l(\mathbf{s}', t') \sim N\left(O_l(\mathbf{s}', t'), \sigma_{\epsilon}^2\right)$$
 (10)

where, for t'=1,

$$O_l(\mathbf{s}', 1) = \gamma_l(\mathbf{s}') + \mu_l \tag{11}$$

and for t' > 1, $O_l(\mathbf{s}', t') = \rho O_l(\mathbf{s}', t' - 1) + \boldsymbol{\delta}'_l(\mathbf{s}', t')\boldsymbol{\beta} + \eta_l(\mathbf{s}', t')$. From this it is clear that $O_l(\mathbf{s}', t')$ can only be sequentially determined using all the previous $O_l(\mathbf{s}', t)$ up to time t'. Hence, we introduce the notation $\mathbf{O}_l(\mathbf{s}, [t])$ to denote the vector $(O_l(\mathbf{s}, 1), \dots, O_l(\mathbf{s}, t))'$ for $t \ge 1$.

The posterior predictive distribution of $Z_l(\mathbf{s}', t')$ is obtained by integrating over the unknown quantities in (10) with respect to the joint posterior distribution, i.e.,

$$\pi \left(Z_{l}(\mathbf{s}', t') | \mathbf{u}, \mathbf{z} \right) = \int \pi \left(Z_{l}(\mathbf{s}', t') | O_{l}(\mathbf{s}', [t']), \sigma_{\epsilon}^{2} \right) \pi \left(O_{l}(\mathbf{s}', [t']) | \gamma_{l}(\mathbf{s}'), \boldsymbol{\delta}'_{l}(\mathbf{s}', t'), \boldsymbol{\theta}, \mathbf{w} \right)$$

$$\pi \left(\boldsymbol{\delta}'_{l}(\mathbf{s}', t') | \mathbf{u}, \boldsymbol{\nu} \right) \pi \left(\gamma_{l}(\mathbf{s}') | \boldsymbol{\theta} \right) \pi(\boldsymbol{\theta}, \mathbf{w} | \mathbf{u}, \mathbf{z}) \pi(\boldsymbol{\nu} | \mathbf{u})$$

$$dO_{l}(\mathbf{s}', [t']) d\boldsymbol{\delta}'_{l}(\mathbf{s}', t') d\gamma_{l}(\mathbf{s}') d\boldsymbol{\theta} d\mathbf{w} d\boldsymbol{\nu}. \tag{12}$$

When using MCMC methods to draw samples from the posterior, the predictive distribution (12) is sampled by composition; draws from the posterior distributions, $\pi(\boldsymbol{\theta}, \mathbf{w}|\mathbf{u}, \mathbf{z})$ and $\pi(\boldsymbol{\nu}|\mathbf{u})$, enable draws from the above component densities, details are provided below.

In (12) we need to generate the random variables $\gamma_l(\mathbf{s}')$, $\delta_l(\mathbf{s}',t')$, and $\mathbf{O}_l(\mathbf{s}',t')$ conditional on the posterior samples at the observed locations $\mathbf{s}_1, \ldots, \mathbf{s}_n$ and at the time points $1, \ldots, T$. To draw samples from $\delta_l(\mathbf{s}',t')$ we use the conditional distribution $\pi\left(\delta_l(\mathbf{s}',t')|\mathbf{u},\boldsymbol{\nu}\right)$. This distribution is similar to (9), see Section 3.1 for more details. Once $\delta_l(\mathbf{s}',t')$ has been drawn we draw $O_l(\mathbf{s}',t')$ from its conditional distribution given all the parameters, data and $O_l(\mathbf{s}',[t'-1])$. For t'=1 we need to sample $\gamma_l(\mathbf{s}')$ for each l. For this we have

$$\left(\begin{array}{c} \gamma_l(\mathbf{s'}) \\ \boldsymbol{\gamma}_l \end{array}\right) \sim N \left[\left(\begin{array}{c} 0 \\ \mathbf{0} \end{array}\right), \sigma_l^2 \left(\begin{array}{cc} 1 & \Sigma_{\gamma,12} \\ \Sigma_{\gamma,21} & \Sigma_{\gamma} \end{array}\right) \right],$$

where $\Sigma_{\gamma,12}$ is $1 \times n$ with the *i*th entry given by $\sigma_{\gamma}(\mathbf{s}_i - \mathbf{s}') = \exp(-\phi_{\gamma}d(\mathbf{s}_i, \mathbf{s}'))$ where $d(\mathbf{s}_i, \mathbf{s}')$ is the distance between the sites \mathbf{s}_i and \mathbf{s}' and $\Sigma_{\gamma,21} = \Sigma'_{\gamma,12}$. Therefore,

$$\gamma_l(\mathbf{s}')|\boldsymbol{\theta} \sim N\left(\Sigma_{\gamma,12}\Sigma_{\gamma}^{-1}\boldsymbol{\gamma}_l, \sigma_l^2\left(1 - \Sigma_{\gamma,12}\Sigma_{\gamma}^{-1}\Sigma_{\gamma,21}\right)\right).$$
 (13)

Analogous to (7), we obtain for t' > 1

$$\begin{pmatrix} O_l(\mathbf{s}',t') \\ \mathbf{O}_{lt'} \end{pmatrix} \sim N \begin{bmatrix} \begin{pmatrix} \xi_l + \rho O_l(\mathbf{s}',t'-1) + \boldsymbol{\delta}'_l(\mathbf{s}',t')\boldsymbol{\beta} \\ \xi_l \mathbf{1} + \rho \mathbf{O}_{lt'-1} + F_{lt'}\boldsymbol{\beta} \end{pmatrix}, \ \sigma_{\eta}^2 \begin{pmatrix} 1 & \Sigma_{\eta,12} \\ \Sigma_{\eta,21} & \Sigma_{\eta} \end{pmatrix} \end{bmatrix}$$

where $\Sigma_{\eta,12}$ is $1 \times n$ with the *i*th entry given by $\sigma_{\eta}(\mathbf{s}_i - \mathbf{s}') = \exp(-\phi_{\eta}d(\mathbf{s}_i, \mathbf{s}'))$ where $d(\mathbf{s}_i, \mathbf{s}')$ is the distance between the sites \mathbf{s}_i and \mathbf{s}' and $\Sigma_{\eta,21} = \Sigma'_{\eta,12}$. Hence,

$$O_l(\mathbf{s}', t')|\gamma_l(\mathbf{s}'), \boldsymbol{\delta}'_l(\mathbf{s}', t'), \mathbf{O}_{lt'}, \boldsymbol{\theta}, \mathbf{w} \sim N(\chi, \Lambda)$$
 (14)

where $\Lambda = \sigma_{\eta}^2 \left(1 - \Sigma_{\eta,12} \Sigma_{\eta}^{-1} \Sigma_{\eta,21} \right)$ and

$$\chi = \xi_l + \rho O_l(\mathbf{s}', t'-1) + \boldsymbol{\delta}'_l(\mathbf{s}', t') \boldsymbol{\beta} + \Sigma_{\eta, 12} \Sigma_{\eta}^{-1} \left(\mathbf{O}_{lt'} - \xi_l \mathbf{1} - \rho \mathbf{O}_{lt'-1} - F_{lt'} \boldsymbol{\beta} \right).$$

In summary, we implement the following algorithm to predict $Z_l(\mathbf{s}', t')$.

- 1. Draw a sample $\theta^{(j)}, \boldsymbol{\nu}^{(j)}, j \geq 1$ from the posterior distribution.
- 2. Draw $\gamma_l^{(j)}(\mathbf{s}')$ using (13).
- 3. Draw $\boldsymbol{\delta}_{l}^{(j)}(\mathbf{s}',t')$ from the distribution $\pi\left(\boldsymbol{\delta}_{l}(\mathbf{s}',t')|\mathbf{u},\boldsymbol{\nu}^{(j)}\right)$.
- 4. Draw $\mathbf{O}_l^{(j)}(\mathbf{s},[t'])$ sequentially, i.e. first obtain $O_l^{(j)}(\mathbf{s}',1)$ from (11) and then draw $O_l^{(j)}(\mathbf{s}',2)$ using (14) and iterate.
- 5. Finally draw $Z_l^{(j)}(\mathbf{s}',t')$ from $N\left(O_l^{(j)}(\mathbf{s}',t'), \ \sigma_{\epsilon}^{2(j)}\right)$.

The ozone concentration on the original scale is the square of $Z_l^{(j)}(\mathbf{s}',t')$. If we want the predictions of the smooth ozone concentration process without the nugget term we simply omit the last step in the above algorithm and square the realizations $\mathbf{O}_l^{(j)}(\mathbf{s},t')$. We use the median of the MCMC samples and the lengths of the 95% intervals to summarize the predictions. The median as a summary measure preserves the one-to-one relationships between summaries for O and Z, and for O^2 and Z^2 .

4.2 Ozone Summaries

We now develop methodology for assessing trend in ozone summaries. We investigate these trends using the true ozone process $O_l(\mathbf{s},t)$. Recall that we model ozone levels on the square-root scale, hence to return to the original scale we use $O_l^2(\mathbf{s},t)$ where appropriate.

The true annual 4th highest daily maximum 8-hour average ozone concentration, denoted by $f_l(\mathbf{s})$, is given by the 4th highest value of the series $O_l^2(\mathbf{s},1),\ldots,O_l^2(\mathbf{s},T)$ in any given year $l,l=1,\ldots,r$. The summaries of the posterior predictive realizations $f_l^{(j)}(\mathbf{s}), j \geq 1$ are used for predictions of the annual 4th highest daily maximum 8-hour average ozone concentration (and to obtain their uncertainties).

The 3-year rolling average of the annual 4th highest daily maximum 8-hour average ozone concentration is obtained by averaging $f_l(\mathbf{s})$ over three successive years and assigning

the average to the final year of averaging. Thus the three year rolling average of the annual 4th highest daily maximum 8-hour average ozone concentration in year l is given by

$$g_l(\mathbf{s}) = \frac{f_{l-2}(\mathbf{s}) + f_{l-1}(\mathbf{s}) + f_l(\mathbf{s})}{3}, l = 3, \dots, r.$$

Again we obtain posterior predictive samples $g_l^{(j)}(\mathbf{s})$ from MCMC iterations and thereby get the prediction summary values along with their uncertainties. We can also estimate the probability of non-attainment at a site \mathbf{s} and in year l, denoted by $P(g_l(\mathbf{s}) > 80)$, by averaging the indicator functions $I\left(g_l^{(j)}(\mathbf{s}) > 80\right)$ over j.

We can obtain the meteorology-adjusted levels only for the sites where we have observed the values, $\mathbf{x}_l(\mathbf{s},t)$, of the meteorological variables. These levels are obtained from the residuals $O_l(\mathbf{s},t) - \mathbf{x}'_l(\mathbf{s},t)\boldsymbol{\beta}$ using:

$$h_l(\mathbf{s}) = \frac{1}{T} \sum_{t=1}^T \left\{ O_l(\mathbf{s},t) - \mathbf{x}_l'(\mathbf{s},t) \boldsymbol{\beta} \right\}^2, l = 1, \dots, r.$$

The posterior predictive realizations $h_l^{(j)}(\mathbf{s})$ are summarized to obtain the adjusted levels at site \mathbf{s} in year l. Note that $O_l(\mathbf{s},t) - \mathbf{x}_l'(\mathbf{s},t)\boldsymbol{\beta}$ is the natural definition of the locally adjusted level though, in the presence of $O_l(\mathbf{s},t-1)$ as in (2) this become less clear. However, since the $\boldsymbol{\beta}$'s obtained under the model in (2) and (3) are very similar to those that are obtained under the model in (4) and since adjusting for meteorology in (4) immediately takes the natural form, we propose the use of this summary. The unadjusted levels are given by $u_l(\mathbf{s}) = \frac{1}{T} \sum_{t=1}^T O_l^2(\mathbf{s},t), l = 1, \ldots, r$.

We evaluate relative percentage change between 1997 and 2004 as:

$$c_{97,04}^{\mathrm{adj}}(\mathbf{s}) = 100 \times \frac{h_8(\mathbf{s}) - h_1(\mathbf{s})}{h_1(\mathbf{s})}, \text{ and } c_{97,04}^{\mathrm{un-adj}}(\mathbf{s}) = 100 \times \frac{u_8(\mathbf{s}) - u_1(\mathbf{s})}{u_1(\mathbf{s})}.$$

Again averaging over posterior predictive realizations produces the desired inference. Percent change for any other pair of years can be handled similarly.

5 Analysis

5.1 Model Checking

Under weak prior distributions it is not possible to estimate all the parameters in the covariance structure, σ_{ϵ}^2 , σ_{η}^2 , ϕ_{η} and ϕ_{γ} consistently, see e.g. Zhang (2004), Sahu et al. (2006) and the references therein. Hence, we use the set-aside validation data from 15 stations to select the two decay parameters ϕ_{η} and ϕ_{γ} . The variance components are estimated using MCMC. Let $\hat{Z}_l^2(\mathbf{s}_i^*,t)$ denote the model based validation estimate for $Z_l^2(\mathbf{s}_i^*,t)$ where \mathbf{s}_i^* denote the *i*th validation site. Again recall that we model ozone in the square root scale. The validation mean-square error is given by

$$VMSE = \frac{1}{n_v} \sum_{i=1}^{15} \sum_{l=1}^{r} \sum_{t=1}^{T} \left(Z_l^2(\mathbf{s}_i^*, t) - \hat{Z_l^2}(\mathbf{s}_i^*, t) \right)^2 I(Z_l(\mathbf{s}_i^*, t))$$

where $I(Z_l(\mathbf{s}_i^*,t))=1$ if $Z_l(\mathbf{s}_i^*,t)$ has been observed and 0 otherwise, and n_v is the total number of available observations at the 15 validation sites. For our data set $n_v=5,991$ as mentioned in Section 2. We searched for the optimal values in a two dimensional grid formed of the values 0.004, 0.005, 0.01 and 0.05. The pair of values $\phi_{\eta}=0.005$ and $\phi_{\gamma}=0.05$, provided the smallest estimated VMSE. The VMSE increases hugely if the values of ϕ_{η} and ϕ_{γ} are interchanged. However, the VMSE is not sensitive to the choice of the decay parameters near these best values. As a result, although it is possible to further refine the grid in a neighborhood of the best value we do not explore beyond our grid here.

As mentioned above we have performed validation for all 5,991 available observations in the fifteen hold-out sites. Overall, 94.73% of the 95% prediction intervals contain the actual observations and about 50.4% of the predictions are greater than the actual observations. Figure 4 shows the validation plot for a randomly chosen site. To enhance readability we only show the validations for once in every fourteen days. The validations indicate that the model does not appear to introduce any bias in prediction and performs very well for out of sample predictions. The predicted annual surfaces discussed in the next subsection also validate the model.

We have performed the usual model diagnostics for checking model adequacy using various residual plots. For example, the fitted versus residual plot (not shown) does not show any curvature or pattern and confirms that the homoscedasticity assumption is acceptable; there were only a few extreme values. The residuals plotted against the year (not shown) do not reveal any anomalies. The variability of the residuals for different years are approximately constant and, in fact, the ratio of the maximum to the minimum variance is less than two.

5.2 Results and Interpretation

The point and interval estimates of the model parameters are given in Tables 1-2. We found strong dependence among successive day ozone concentrations (estimate of $\rho = 0.7783$). Except for wind speed, all meteorological variables were found to be significantly related to ozone concentrations. The estimates of the variance components σ_{ϵ}^2 and σ_{η}^2 show that more variation is explained by the spatio-temporal effects than the pure error process $\epsilon_l(\mathbf{s}, t)$.

The estimates of μ_1, \ldots, μ_8 , see Table 2, show that changes in the global ozone level as defined in our model are similar to that in Figure 2. Due to the inclusion of the autoregressive term $\rho O_l(\mathbf{s}, t-1)$ for t > 1 in equation (2), the estimates of ξ_1, \ldots, ξ_8 (see Table 2) do not show this pattern. The estimates of $\sigma_1^2, \ldots, \sigma_8^2$ (see Table 2) capture (significantly) differing levels of variability between years. The ratio of the maximum variance in 1998 to the minimum in 2001 is more than 3; this is also evident in the boxplots provided in Figure 2.

We now summarize the different types of trend information that can be realized from this modeling approach as described in Section 4.2. The annual 4th highest daily maximum true

ozone values are plotted by linearly interpolating the predictions at 289 gridded locations in Ohio (see Figure 5) with the observed 4th highest daily maxima at the monitoring sites superimposed on the predictive surface. We find excellent agreement among the predicted and observed maxima values. Quantification of this agreement can be found by calculating the root mean square error (RMSE) between the observations and predictions closest to the monitoring sites. The RMSE's, in units of ppb, for the years 1997-04 are: 3.4, 5.1, 4.9, 4.3, 3.7, 4.6, 5.0, and 4.5, respectively. Thus, the model is predicting the maxima within a range of 3-5 ppb on average. Figure 6 shows the lengths of the 95% prediction intervals. As expected these intervals are larger in non-monitored areas compared with monitored areas. The majority of NOx and VOC emissions in the eastern U.S. come from three sources: mobile sources, industrial processes, and large electric utilities. Mobile sources and electric utilities accounted for 78 percent of annual NOx emissions in 2004, see U.S. Environmental Protection Agency (2005). From 1997-2004, annual NOx emissions have decreased by 25% in the eastern U.S., and similarly VOC emissions have decreased by 21%. Figure 5 shows decreasing patterns of true ozone levels across time that might be attributed to reduced levels of ozone precursor emissions.

Model based interpolated maps of the 3-year rolling averages of the annual 4th highest daily maximum 8-hour true ozone concentrations (Figure 7) are given for the years 1999-2004. We define the year 1999 as the rolling average for 1997-1999, and similarly for the other rolling averages. As with the annual patterns, we find good agreement with the data superimposed on the plot. The RMSE's are 3.7, 4.2, 3.6, 3.7, 3.6, and 3.5 respectively. These RMSE's show somewhat better predictions for the 3-yr averages in comparison to the annual maxima. Also, these patterns reflect the reduced emission levels over this time period. The increase in the 3-year rolling averages that include 2002 can be attributed to the above normal ozone-forming conditions for that year. In 2002, temperatures were above normal and precipitation was below normal in the northeast. These maps of true ozone concentrations (O in our model), suggest regions of non-attainment with the current NAAQS for ozone standard of 80 ppb based on the 3-year rolling averages. Uncertainty in this inference is given by the lengths of the prediction intervals (Figure 8). To quantify the extent of non-attainment across Ohio, we developed maps of the probabilities of exceeding the ozone NAAQS. Using a nominal probability level of 0.8, almost all of Ohio was found to exceed this probability level for all rolling averages except for 2004 where we see improved air quality conditions in southern Ohio (Figure 9).

Trends in meteorology-adjusted ozone predictions at 12 monitoring sites in Ohio, along with trends in unadjusted predictions, are shown in Figure 10. Again, we see high ozone unadjusted predictions in 2002, in comparison to the smoother adjusted predictions at and around this time period. From the adjusted predictions, we see an overall decreasing pattern in ozone, that is not easily discerned in the plot of the unadjusted predictions. Figure 11 illustrates the spatial pattern of trend at monitoring sites defined as a relative difference (%) of adjusted and unadjusted predictions for 1997-2004. These trends are all

negative, some significant, according to the 95% predictive intervals based upon the MCMC replications. Given our definition of trend, we see more significant reductions based on the meteorology-adjusted ozone predictions. Only 6 of 12 sites show significant reductions on the unadjusted scale, while 11 out of 12 show significant reductions on the adjusted scale. While, from a public health perspective, all that matters is realized ozone concentration levels, clarification of trends in the non-meteorological component is informative.

6 Discussion

We have formulated a model for assessing ozone levels at point-level spatial resolution and daily temporal resolution. We have shown how to use this model to do standard prediction but, more interestingly, to provide summaries of annual fourth highest daily average ozone levels and also summaries in the form of three year rolling averages of these fourth highest daily averages. Moreover, we can attach uncertainty to all of these predictions, derived from the model fitting. We are also able to demonstrate the benefit of fitting models when interpolating extremes as opposed to interpolating the observations themselves. This contrasts with the case for summarizing averages.

As the U.S. EPA continues with emission control program of ozone, it will be necessary to further refine and update statistical analyses of trend. In future work, we plan to investigate spatially varying coefficients, see e.g. Gelfand et al. (2003), in the incremental meteorology model, imagining that the effect of different meteorological variables might be different for different parts of the state. We also plan to extend the analysis to, at the least, the eastern portion of the United States. This will dramatically increase the number of sites for both ozone measurements and meteorology data. (The current paper handles 142,543 observations altogether.) Approximate computation will be required. In particular, approximate process representations (see for example, Xia and Gelfand (2006) or Paciorek and Ryan, 2006) will be employed.

Disclaimer:

The U.S. Environmental Protection Agency's Office of research and Development partially collaborated in the research described here. Although it has been reviewed by EPA and approved for publication, it does not necessarily reflect the Agency's policies or views.

Appendix: Distributions for Gibbs sampling

Conditional Distributions for: σ_{ϵ}^2 , σ_{η}^2 , O_{lt} , ρ and β

Any missing value, $Z_l(\mathbf{s},t)$ is to be sampled from $N(O_l(\mathbf{s},t),\sigma_{\epsilon}^2),\ l=1,\ldots,r,\ t=1,\ldots,r$

 $1, \ldots, T$. Straightforward calculation yields the following complete conditional distributions:

$$\frac{1}{\sigma_{\epsilon}^{2}} \sim G\left(\frac{N}{2} + a, b + \frac{1}{2}\sum_{l=1}^{r}\sum_{t=1}^{T}(\mathbf{Z}_{lt} - \mathbf{O}_{lt})'(\mathbf{Z}_{lt} - \mathbf{O}_{lt})\right),$$

$$\frac{1}{\sigma_{\eta}^{2}} \sim G\left(\frac{M}{2} + a, b + \frac{1}{2}\sum_{l=1}^{r}\sum_{t=2}^{T}(\mathbf{O}_{lt} - \boldsymbol{\vartheta}_{lt})'\Sigma_{\eta}^{-1}(\mathbf{O}_{lt} - \boldsymbol{\vartheta}_{lt})\right).$$

Note that we do not need to sample from \mathbf{O}_{l1} since we have the identity (6). Let $Q_{\eta} = \Sigma_{\eta}^{-1}$. The full conditional distribution of \mathbf{O}_{lt} is $N(\Lambda_{lt}\chi_{lt}, \Lambda_{lt})$ where

$$\Lambda_{lt}^{-1} = \frac{I_n}{\sigma_{\epsilon}^2} + (1 + \rho^2)Q_{\eta}, \boldsymbol{\chi}_{lt} = \frac{\mathbf{Z}_{lt}}{\sigma_{\epsilon}^2} + Q_{\eta} \left\{ \rho \mathbf{O}_{lt-1} + F_{lt}\boldsymbol{\beta} + \xi_l \mathbf{1} + \rho \left(\mathbf{O}_{lt+1} - F_{lt+1}\boldsymbol{\beta} - \xi_l \mathbf{1} \right) \right\}$$

when 1 < t < T, and for t = T

$$\Lambda_{lt}^{-1} = \frac{I_n}{\sigma_{\epsilon}^2} + Q_{\eta}, \ \boldsymbol{\chi}_{lt} = \frac{\mathbf{Z}_{lt}}{\sigma_{\epsilon}^2} + Q_{\eta}(\xi_l \mathbf{1} + \rho \mathbf{O}_{lt-1} + F_{lt}\boldsymbol{\beta}).$$

The full conditional distribution of ξ_l is $N(\Lambda \chi, \Lambda)$ where

$$\Lambda^{-1} = (T-1)\mathbf{1}'Q_{\eta}\mathbf{1} + 10^{-4} \chi = \sum_{t=2}^{T} \mathbf{1}'Q_{\eta}(\mathbf{O}_{lt} - \rho \mathbf{O}_{lt-1} - F_{lt}\boldsymbol{\beta}),$$

The full conditional distribution of ρ is $N(\Lambda \chi, \Lambda)$ where

$$\Lambda^{-1} = \sum_{l=1}^{r} \sum_{t=2}^{T} \mathbf{O}'_{lt-1} Q_{\eta} \mathbf{O}_{lt-1} + 10^{-4}, \ \chi = \sum_{l=1}^{r} \sum_{t=2}^{T} \mathbf{O}'_{lt-1} Q_{\eta} (\mathbf{O}_{lt} - \xi_{l} \mathbf{1} - F_{lt} \boldsymbol{\beta}),$$

restricted in the interval (0, 1). The full conditional distribution of β is $N(\Lambda \chi, \Lambda)$ where

$$\Lambda^{-1} = \sum_{l=1}^{r} \sum_{t=2}^{T} F'_{lt} Q_{\eta} F_{lt} + 10^{-4} I_{p}, \ \boldsymbol{\chi} = \sum_{l=1}^{r} \sum_{t=2}^{T} F'_{lt} Q_{\eta} (\mathbf{O}_{lt} - \xi_{l} \mathbf{1} - \rho \mathbf{O}_{lt-1}).$$

Conditional Distribution of $\delta_{lt}^{(1)}$

We obtain the likelihood contribution for $\delta(\mathbf{s}_i, t), i = 1, ..., n_1$ as follows. We have, $F_{lt}\boldsymbol{\beta} =$

$$\begin{pmatrix} \boldsymbol{\beta}'\boldsymbol{\delta}_{l}(\mathbf{s}_{1},t) \\ \boldsymbol{\beta}'\boldsymbol{\delta}_{l}(\mathbf{s}_{2},t) \\ \vdots \\ \boldsymbol{\beta}'\boldsymbol{\delta}_{l}(\mathbf{s}_{n},t) \end{pmatrix} = \begin{pmatrix} \boldsymbol{\beta}' & \mathbf{0} & \cdots & \mathbf{0} \\ \mathbf{0} & \boldsymbol{\beta}' & \cdots & \mathbf{0} \\ \vdots & \vdots & \vdots & \vdots \\ \mathbf{0} & \mathbf{0} & \cdots & \boldsymbol{\beta}' \end{pmatrix} \begin{pmatrix} \boldsymbol{\delta}_{l}(\mathbf{s}_{1},t) \\ \boldsymbol{\delta}_{l}(\mathbf{s}_{2},t) \\ \vdots \\ \boldsymbol{\delta}_{l}(\mathbf{s}_{n},t) \end{pmatrix} = \begin{pmatrix} X_{1} & 0 \\ 0 & X_{2} \end{pmatrix} \boldsymbol{\delta}_{lt},$$

where X_1 is $n_1 \times n_1 p$ and X_2 is $(n - n_1) \times (n - n_1) p$. Let $\boldsymbol{\delta}_{lt}^{(12)} = (\boldsymbol{\delta}_l'(\mathbf{s}_{n_1+1}, t), \boldsymbol{\delta}_l'(\mathbf{s}_{n_1+2}, t), \cdots, \boldsymbol{\delta}_l'(\mathbf{s}_n, t))'$. Let us partition Q_{η} as follows:

$$Q_{\eta} = \left(egin{array}{cc} Q_{11} & Q_{12} \ Q_{21} & Q_{22} \end{array}
ight),$$

where Q_{11} is $n_1 \times n_1$ and Q_{22} is $n_2 \times n_2$ and we suppress the symbol η for convenience. Define $\mathbf{a}_{lt} = \mathbf{O}_{lt} - \xi_l \mathbf{1} - \rho \mathbf{O}_{lt-1}$ and partition $\mathbf{a}_{lt} = \left(\left(\mathbf{a}_{lt}^{(1)} \right)', \left(\mathbf{a}_{lt}^{(2)} \right)' \right)'$ where $\mathbf{a}_{lt}^{(1)}$ is $n_1 p \times 1$.

Now

$$\begin{aligned} \mathbf{(a}_{lt} - F_{lt}\boldsymbol{\beta})Q_{\eta}(\mathbf{a}_{lt} - F_{lt}\boldsymbol{\beta}) &= \left(\begin{array}{c} \mathbf{a}_{lt}^{(1)} - X_{1}\boldsymbol{\delta}_{lt}^{(1)} \\ \mathbf{a}_{lt}^{(2)} - X_{2}\boldsymbol{\delta}_{lt}^{(2)} \end{array}\right)'Q_{\eta} \left(\begin{array}{c} \mathbf{a}_{lt}^{(1)} - X_{1}\boldsymbol{\delta}_{lt}^{(1)} \\ \mathbf{a}_{lt}^{(2)} - X_{2}\boldsymbol{\delta}_{lt}^{(2)} \end{array}\right) \\ &= \left(\mathbf{a}_{lt}^{(1)} - X_{1}\boldsymbol{\delta}_{lt}^{(1)}\right)'Q_{11} \left(\mathbf{a}_{lt}^{(1)} - X_{1}\boldsymbol{\delta}_{lt}^{(1)}\right) + 2\left(\mathbf{a}_{lt}^{(1)} - X_{1}\boldsymbol{\delta}_{lt}^{(1)}\right)'Q_{12} \left(\mathbf{a}_{lt}^{(2)} - X_{2}\boldsymbol{\delta}_{lt}^{(2)}\right) + C, \end{aligned}$$

where C is free of $\boldsymbol{\delta}_{lt}^{(1)}$. Now from (9) we have:

$$m{\delta}_{lt}^{(1)} | m{\delta}_{lt}^{(2)} \sim N\left(\Sigma_{12}\Sigma_{22}^{-1}m{\delta}_{lt}^{(2)}, \; \Sigma_{11} - \Sigma_{12}\Sigma_{22}^{-1}\Sigma_{21}\right) \equiv N(m{\zeta}_{lt}, \Sigma_{\delta}), \; ext{say}.$$

Thus the conditional posterior distribution of $\boldsymbol{\delta}_{lt}^{(1)}$ is $N\left(\Lambda \boldsymbol{\chi}_{lt}, \Lambda\right)$ where

$$\Lambda^{-1} = \Sigma_{\delta}^{-1} + X_1' Q_{11} X_1 \text{ and } \boldsymbol{\chi}_{lt} = \Sigma_{\delta}^{-1} \boldsymbol{\zeta}_{lt} + X_1' \left\{ Q_{11} \mathbf{a}_{lt}^{(1)} + Q_{12} \left(\mathbf{a}_{lt}^{(2)} - X_2 \boldsymbol{\delta}_{lt}^{(12)} \right) \right\}.$$

Conditional Distributions for: γ_l , μ_l and σ_l^2

The conditional posterior distribution of γ_l will come from

$$\mathbf{Z}_{l1} = \boldsymbol{\gamma}_l + \mu_l \mathbf{1} + \boldsymbol{\epsilon}_{l1}, \ \mathbf{O}_{l2} = \rho \left(\boldsymbol{\gamma}_l + \mu_l \mathbf{1} \right) + F_{l2} \boldsymbol{\beta} + \boldsymbol{\eta}_{l2}, \ \text{and} \ \boldsymbol{\gamma}_l \sim N(\mathbf{0}, \ \Sigma_l).$$

Hence, the conditional posterior distribution of γ_l is $N(\Lambda_l \chi_l, \Lambda_l)$ where

$$\Lambda_l^{-1} = I_n/\sigma_{\epsilon}^2 + \Sigma_l^{-1} + \rho^2 Q_{\eta}, \text{ and } \boldsymbol{\chi}_l = \rho Q_{\eta}(\mathbf{O}_{l2} - \rho \mu_l \mathbf{1} - \xi_l \mathbf{1} - F_{l2}\boldsymbol{\beta}) + (\mathbf{Z}_{l1} - \mu_l \mathbf{1})/\sigma_{\epsilon}^2.$$

We also have the conditional distribution:

$$\frac{1}{\sigma_l^2} \sim G\left(\frac{n}{2} + a, b + \frac{1}{2} \boldsymbol{\gamma}_l' \Sigma_{\gamma} \boldsymbol{\gamma}_l\right).$$

The conditional posterior distribution of μ_l is $N(\chi_l, \lambda_l)$ where

$$\chi_l = \lambda_l^{-1} \left(\frac{\mathbf{1}'(\mathbf{Z}_{l1} - \boldsymbol{\gamma}_l)}{\sigma_{\epsilon}^2} + \rho \mathbf{1}' Q_{\eta} (\mathbf{O}_{l2} - \rho \boldsymbol{\gamma}_l - \xi_l \mathbf{1} - F_{l2} \boldsymbol{\beta}) \right),$$
and
$$\lambda_l^{-1} = \frac{n}{\sigma_{\epsilon}^2} + \rho^2 \mathbf{1}' Q_{\eta} \mathbf{1} + 10^{-4}.$$

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Table 1: Estimation of the parameters. CI stands for equal tailed credible intervals.

	mean	sd	95%CI
ρ	0.7783	0.0030	(0.7723, 0.7842)
$\beta_1(\text{temp})$	0.1069	0.0021	$(0.1029,\ 0.1109)$
$eta_2(ext{humidity})$	-0.0126	0.0004	$(-0.0134,\!-0.0118)$
$\beta_3({ m wind \; speed \; am})$	-0.0025	0.0030	$(-0.0083,\ 0.0033)$
$\beta_3({ m wind\ speed\ pm})$	-0.0120	0.0025	$(-0.0170,\!-0.0074)$
σ_ϵ^2	0.0486	0.0007	$(0.0460,\ 0.0487)$
σ_{η}^2	0.3235	0.0046	$(0.3149,\ 0.3326)$

Table 2: Estimation of μ_l, σ_l^2 and $\xi_l, l = 1, \dots, 8$. CI stands for equal tailed credible intervals.

μ_l			σ_l^2			ξ_l		
mean	sd	$95\%\mathrm{CI}$	mean	sd	95%CI	mean	sd	95%CI
7.30	0.10	(7.10, 7.51)	0.24	0.06	(0.15, 0.37)	1.52	0.04	(1.45, 1.59)
6.28	0.14	$(5.98,\ 6.56)$	0.42	0.10	$(0.27,\ 0.65)$	1.61	0.04	$(1.54,\ 1.68)$
6.18	0.14	(5.88, 6.44)	0.40	0.09	$(0.25,\ 0.61)$	1.60	0.04	$(1.52,\ 1.66)$
7.17	0.09	$(6.98,\ 7.35)$	0.20	0.05	$(0.12,\ 0.31)$	1.53	0.04	$(1.46,\ 1.60)$
6.55	0.08	$(6.39,\ 6.70)$	0.13	0.03	(0.08, 0.20)	1.58	0.04	$(1.51,\ 1.65)$
7.35	0.09	(7.17, 7.54)	0.20	0.05	$(0.12,\ 0.30)$	1.63	0.04	$(1.56,\ 1.70)$
8.42	0.08	$(8.26,\ 8.58)$	0.15	0.04	$(0.10,\ 0.23)$	1.52	0.04	$(1.46,\ 1.59)$
7.09	0.11	$(6.88,\ 7.32)$	0.28	0.06	(0.18, 0.42)	1.48	0.04	$(1.41,\ 1.55)$

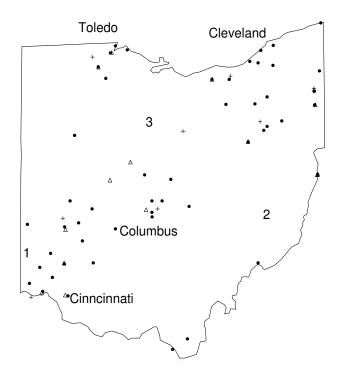


Figure 1: The ozone monitoring sites and meteorological sites in Ohio. The 50 NAMS/SLAMS sites are plotted as points; the sites numbered 1, 2 and 3 are three CAST-NET sites; sites denoted by '+' are meteorological sites (two are outside Ohio); 15 validation sites are shown by the symbol \triangle .

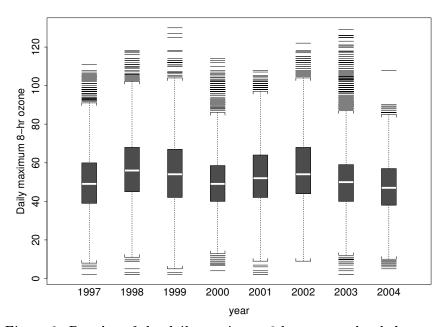


Figure 2: Boxplot of the daily maximum 8-hour ozone levels by years.

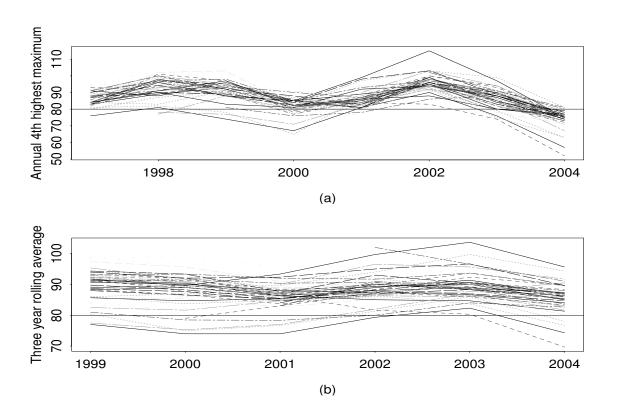


Figure 3: Annual 4th highest daily maxima ozone levels at 53 data sites in panel (a) and 3-year rolling averages in panel (b).

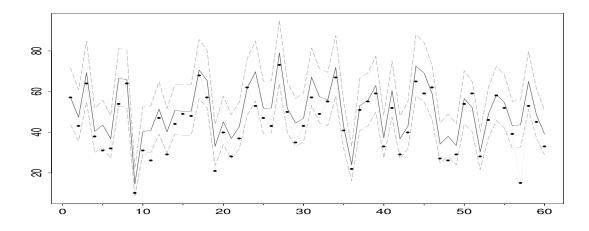


Figure 4: Validation plot for a randomly chosen hold-out site. The observed data are plotted as points. The validation predictions are plotted as solid lines and the 95% equal tailed prediction intervals are plotted as broken line.

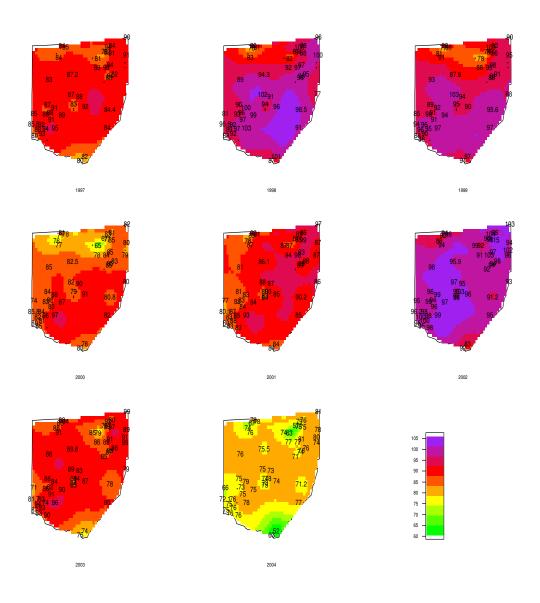


Figure 5: Model based interpolation of the true annual 4th highest maximum ozone levels for 8 years. Observed data are superimposed on the plots.

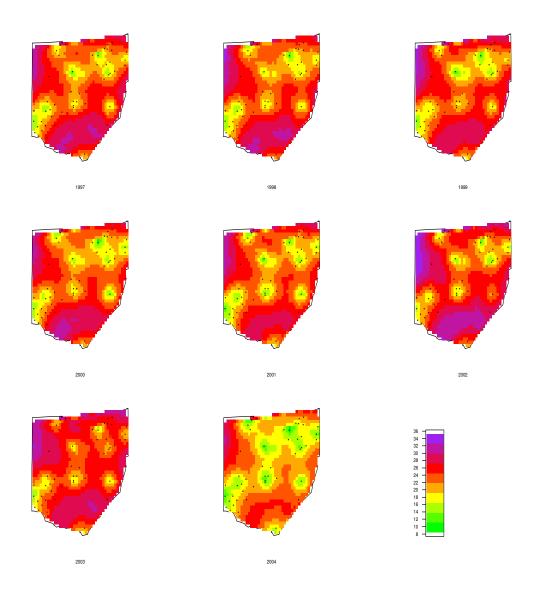


Figure 6: Lengths of 95% intervals of the true annual 4th highest maximum ozone levels for 8 years.

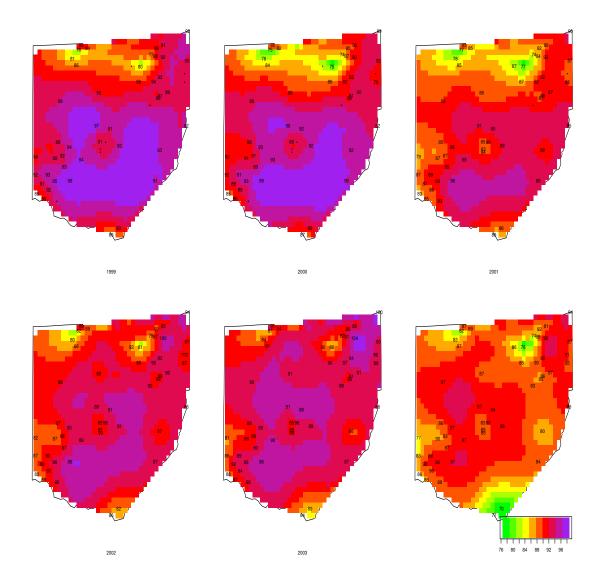


Figure 7: Model based interpolation of the 3-year rolling averages of the true annual 4th highest maximum ozone levels. Observed data are superimposed.

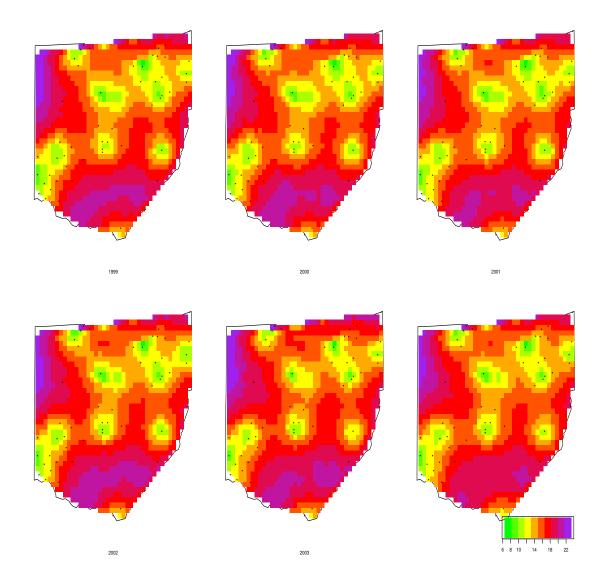


Figure 8: Lengths of 95% intervals of the 3-year rolling averages of the true annual 4th highest maximum ozone levels.

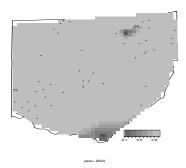


Figure 9: The probability that 3-year rolling average of the true annual 4th highest maximum ozone levels exceed 80 for the year 2004. Observed 3-year averages which are less than 80 are superimposed on the plot.

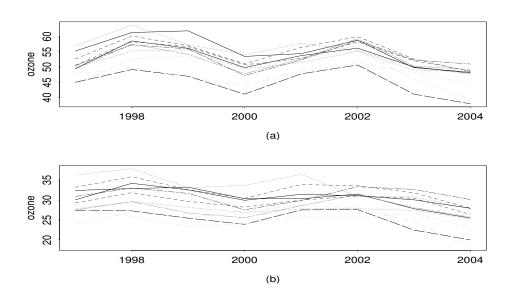


Figure 10: Trends in ozone levels at the 12 sites where meteorological variables have been observed: panel (a) for the un-adjusted and (b) for the adjusted trends.

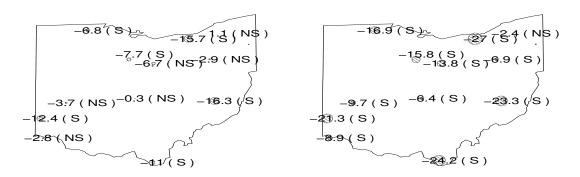


Figure 11: Relative percentage trends (RPT)in the year 2004 (base year =1997) at the 12 sites where meteorological variables have been observed, significant values are labeled by (S) and non-significant values are labeled by (NS). The radius of the plotted circles are proportional to the RPT's labeled in the plots. Left panel is for the un-adjusted ones and right panel is for the meteorology-adjusted ones.