Distributed Irregular Codes Relying on Decode-and-Forward Relays as Code Components

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Abstract-A near-capacity distributed coding scheme is con-5 6 ceived by incorporating multiple relay nodes (RNs) for con-7 structing a virtual irregular convolutional code (IRCC). We first 8 compute the relay channel's capacity and then design IRCCs for 9 the source and relay nodes. Extrinsic information transfer (EXIT) 10 charts are utilized to design the codes for approaching the achiev-11 able capacity of the relay channels. Additionally, we improve 12 the transmit power efficiency of the overall system by invoking 13 both power allocation and relay selection. We found that even a 14 low-complexity repetition code or a unit-memory convolutional 15 code is capable of forming a near-capacity virtual IRCC. The 16 performance of the proposed distributed IRCC (DIRCC) scheme 17 is shown to be perfectly consistent with that predicted from the 18 EXIT chart. More specifically, the DIRCC scheme is capable of 19 operating within 0.68 dB from the corresponding lower bound of 20 the relay channel capacity, despite the fact that each RN is exposed 21 to realistic decoding errors due to communicating over imperfect 22 source-relay channels.

Index Terms-Cooperative communications, cooperative diver-23 25 sity, distributed coding, irregular convolutional codes (IRCCs), relay selection.

I. INTRODUCTION

ULTIPLE-input multiple-output (MIMO) techniques 28 [1], [2], which employ multiple antennas at both the 29 30 transmitter and the receiver, are capable of providing reliable 31 transmissions at high data rates or at low transmit power. How-32 ever, the correlation of signals transmitted from a small mobile 33 unit equipped with multiple antennas degrades the attainable 34 performance. As a remedy, cooperative communications [3], 35 [4] constitutes an attractive solution by forming a distributed 36 MIMO system with the aid of user cooperation, where each user 37 node may be equipped with just a single antenna. More explic-38 itly, user cooperation is invoked for the sake of achieving reli-39 able and efficient transmission. The broadcast nature of wireless 40 transmission makes reception at relay terminals possible at

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no extra cost. Furthermore, relaying typically benefits from a 41 reduced path loss, which makes cooperative communications 42 power efficient. The most popular cooperative protocols are 43 the decode-and-forward (DAF) and the amplify-and-forward 44 (AAF) schemes. However, a strong channel code is required 45 for mitigating potential error propagation in the DAF scheme 46 or for avoiding noise enhancement of the AAF scheme. 47

Distributed coding [5], which involves joint coding design 48 between the source node (SN) and relay nodes (RNs), is one of 49 the promising coding techniques conceived for approaching the 50 achievable capacity of the relay channel with the aid of itera-51 tive detection at the destination node (DN). More specifically, 52 distributed turbo codes [6]-[9], distributed low-density parity- 53 check codes [10]-[12], distributed turbo trellis coded modula- 54 tion [13], distributed space-time codes [14]-[17], distributed 55 self-concatenated convolutional codes [18], distributed rateless 56 codes [19], and distributed soft coding [20] have been proposed 57 for cooperative communications. Furthermore, selecting benefi- 58 cial RNs that exhibit high-quality source-to-relay and relay-to- 59 destination links is capable of significantly reducing the overall 60 transmission power of the relay network [21], [22]. On the 61 other hand, irregular convolutional codes (IRCCs) [23], [24] 62 constitute a powerful outer code family conceived for assisting 63 serially concatenated channel coding schemes in approaching 64 the corresponding channel capacity [25]-[27]. More explicitly, 65 $K \ge 1$ out of N component codes are chosen to produce an 66 encoded sequence having a length of N_c bits. The *p*th subcode 67 produces a subsequence having a length of $\alpha_p N_c$ bits, where 68 α_p is the *p*th IRCC weighting coefficient. The K component 69 codes and their weighting coefficients are chosen to create an 70 IRCC extrinsic information transfer (EXIT) [23], [28] curve 71 for matching that of the inner code. Near-capacity performance 72 is achieved, when the area between the inner and outer code's 73 EXIT curves is minimized. 74

In this contribution, we propose a distributed IRCC (DIRCC) 75 scheme, where the IRCC component codes are distributed to 76 appropriately selected RNs, for the sake of approaching the 77 relay channel capacity. First, an IRCC is designed at the SN 78 for approaching the capacity of the source-to-relay links. Then, 79 K RNs are chosen to form a virtual K-component IRCC for ap- 80 proaching the overall relay channel capacity. Iterative decoding 81 is performed at all RNs and DN. As another potential benefit, 82 the specific RNs that have more battery charge may be used for 83 encoding and transmitting the longer bit sequences, whereas 84 those having limited power can be invoked for encoding and 85 relaying shorter bit sequences. Hence, the required processing 86 and transmission power can be distributed to RNs having 87

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Fig. 1. Schematic of the DIRCC scheme.

88 different power constraints, instead of heavily exploiting a 89 single RN during the entire DAF process. This is particularly 90 beneficial when energy-harvesting nodes (EHNs) [29] are uti-91 lized as our RNs. More explicitly, there may be several EHNs 92 available that have sufficient battery charge for carrying out 93 partial encoding while there may not be a single EHN that 94 has the battery charge required to carry out the entire IRCC 95 encoding. Both relay selection and power allocation are also 96 considered for improving the transmission power efficiency of 97 the overall system.

98 The rest of this paper is organized as follows. The system 99 model is described in Section II, whereas the system design is 100 detailed in Section III. Our simulation results are discussed in 101 Section IV, whereas our conclusions are offered in Section V.

II. System Model

We considered a two-hop half-duplex relaying model, in-104 volving a single SN, multiple RNs, and a DN. The schematic 105 of the proposed DIRCC scheme is shown in Fig. 1, where the 106 SN *s* broadcasts a frame of coded symbols \mathbf{x}_s during the first 107 transmission phase T_1 , which is received by the DN *d* and all 108 the RNs. The carefully selected *K* out of *N* RNs decode \mathbf{x}_s 109 and reencode a portion of the decoded bits to form the virtual 110 IRCC coded symbols $\mathbf{x}_r = [\mathbf{x}_{r_1} \mathbf{x}_{r_2} \dots \mathbf{x}_{r_k} \dots \mathbf{x}_{r_K}]$, where 111 the subsequence \mathbf{x}_{r_k} is transmitted by the *k*th RN, r_k , during 112 the *k*th timeslot of the second transmission phase T_2 . Each 113 selected RN transmits its encoded symbol sequence in different 114 timeslots¹ to the DN.

115 The *j*th signal received at the RN during T_1 , when N_s 116 symbols are transmitted from the SN, can be written as

$$y_{r_k,j}^{(T_1)} = \sqrt{G_{sr_k}} h_{sr_k,j}^{(T_1)} x_{s,j} + n_{r_k,j}^{(T_1)}$$
(1)

117 where $j \in \{1, ..., N_s\}$, and $h_{ab,j}^{(T_l)}$ is the complex-valued fast 118 Rayleigh fading channel coefficient between node a and node b119 at instant j during the lth transmission phase T_l , whereas $n_{b,j}^{(T_l)}$ 120 is zero-mean complex additive white Gaussian noise at node 121 b having a variance of $N_0/2$ per dimension during T_l . Note 122 that we consider a free-space path-loss model having a path-123 loss exponent of 2. Hence, the reduced-distance-related path-124 loss reduction (or geometrical gain) of the SN-to-RN link with 125 respect to the SN-to-DN link [6], [18], [30] is given by

$$G_{sr_k} = \left(\frac{d_{sd}}{d_{sr_k}}\right)^2 \tag{2}$$

¹It is possible to extend the scheme to have simultaneous transmissions from all RNs at the cost of more complex detection at the DN.

where d_{ab} stands for the distance between node a and node b. 126 Similarly, the *j*th signal received at the DN during T_1 can be 127 expressed as 128

$$y_{d,j}^{(T_1)} = \sqrt{G_{sd}} h_{sd,j}^{(T_1)} x_{s,j} + n_{d,j}^{(T_1)}$$
(3)

where we have $G_{sd} = 1$. Each RN decodes the received signal 129 for retrieving the original information sequence. Only a portion 130 of the information sequence is reencoded at each RN using the 131 corresponding component encoder for transmission to the DN. 132

The *j*th symbol from the *k*th RN received at the DN during 133 the second transmission phase T_2 can be written as 134

$$y_{r_k d, j}^{(T_2)} = \sqrt{G_{r_k d}} h_{r_k d, j}^{(T_2)} x_{r_k, j} + n_{d, j}^{(T_2)}$$
(4)

where the modulated symbol sequence of the k RN is given 135 by $\mathbf{x}_{r_k} = [x_{r_k,1} \dots x_{r_k,j} \dots x_{r_k,L_k}]$, L_k is the number of 136 modulated symbols, and the geometrical gain of the RN-to-DN 137 link with respect to the SN-to-DN link is given by 138

$$G_{r_kd} = \left(\frac{d_{sd}}{d_{r_kd}}\right)^2 \,. \tag{5}$$

The total number of coded symbols of the virtual IRCC formed 139 by the K RNs is given by 140

$$N_r = \sum_{k=1}^{K} L_k . (6)$$

In general, each RN will transmit a different number of coded 141 and modulated symbols, i.e., $L_k \neq L_p$ for $k \neq p$. 142

If $x_{a,j}$ is the *j*th symbol transmitted from node *a*, the average 143 receive signal-to-noise power ratio (SNR) at node *b* is given by 144

$$\Gamma_{r} = \frac{\mathrm{E}\{G_{ab}\}\mathrm{E}\{|h_{ab,j}|^{2}\}\mathrm{E}\{|x_{a,j}|^{2}\}}{N_{0}} = \frac{G_{ab}}{N_{0}} \qquad (7)$$

where $E\{|h_{ab,j}|^2\} = 1$ when communicating over fast Rayleigh 145 fading channels and $E\{|x_{a,j}|^2\} = 1$. For convenience, we de- 146 fine the average *transmit SNR* as the ratio of the average power 147 transmitted from node *a* to the noise power encountered at the 148 receiver of node b^2 as 149

$$\Gamma_{t} = \frac{E\{|x_{a,j}|^{2}\}}{N_{0}} = \frac{1}{N_{0}}.$$
(8)

Hence, we have

Ι

$$\Gamma_{\rm r} = \Gamma_{\rm t} \ G_{ab}$$

$$\gamma_{\rm r} = \gamma_{\rm t} + g_{ab} \ [\rm dB] \tag{9}$$

where $\gamma_r = 10 \log_{10}(\Gamma_r)$, $\gamma_t = 10 \log_{10}(\Gamma_t)$, and the geomet- 151 rical gain in decibels is given by $g_{ab} = 10 \log_{10}(G_{ab})$. Hence, 152 we can achieve the desired receive SNR by simply changing 153 the transmit power (which governs γ_t) or by selecting an RN 154 at an appropriate geographical location (which defines g_{ab}). In 155 other words, the channel state information (CSI) is not required 156



²This definition is in line with [6] and [30], but it is unconventional, because it relates the transmit power to the receiver noise measured at two distinct locations.



Fig. 2. Schematic of the equivalent DIRCC encoder when perfect decoding is achieved at RNs. The bit-based interleavers at the SN and the relay network are denoted as π_s and π_r , respectively.

157 for computing the average receive SNR at each transmission 158 symbol period.

159 A. Encoder Structure

160 We consider employing a powerful serial concatenation of an 161 IRCC and a recursive unity-rate code (URC) [31] at the SN. 162 The serially concatenated IRCC and URC scheme has been 163 beneficially used in various near-capacity designs [25]–[27], 164 [32]–[34]. More specifically, URCs were proposed by 165 Divsalar *et al.* [31] for the sake of extending the overall sys-166 tem's impulse response to an infinite duration, which efficiently 167 spreads the extrinsic information between the decoders for 168 improving the achievable iterative detection gain. At the SN, we 169 employ an IRCC as the outer code (IRCC_s), a recursive unity-170 rate code (URC) as the inner code (URC_s), and a simple phase-171 shift keying (PSK) modulator (PSK_s), as shown in Fig. 2, to 172 approach the capacity of the source-to-relay channels.

173 We invoke the DAF protocol for all RNs. At each RN, 174 the $IRCC_s$ -URC_s-PSK_s decoder, shown in the upper part of 175 Fig. 3, is used for generating the estimate of the information bit 176 sequence $\{u_1\}$, before it is fed to the interleaver π_r in Fig. 2. In 177 the absence of decoding errors at the RNs, the input sequence (or the decoded bit sequence) of the "distributed" relay network 178 would be exactly the same as that of the SN. Hence, the 179 180 equivalent DIRCC encoder structure can be simplified, as seen 181 in the schematic in Fig. 2. The "selector" block shown in Fig. 2 182 assigns the IRCC code-component weights based on an EXIT-183 curve-matching procedure to be detailed in Section III-B. We 184 will demonstrate that near-error-free decoding is achieved at 185 channel SNRs close to the SNR limit at the capacity of the 186 relay channels. The IRCC weight of the specific $IRCC_s$ at 187 the SN is also designed based on an EXIT-curve-matching 188 procedure to be detailed in Section III-B for approaching the 189 capacity of the source-to-relay channels. The kth RN would 190 produce an encoded sequence of $\tilde{\mathbf{c}}_{1}^{r_{k}} = [\tilde{c}_{1,1}^{r_{k}} \tilde{c}_{1,2}^{r_{k}} \dots \tilde{c}_{1,j}^{r_{k}} \dots],$ 191 which is part of the virtual IRCC-encoded sequence $\tilde{c}_1 =$ 192 $[\tilde{\mathbf{c}}_1^{r_1} \ \tilde{\mathbf{c}}_1^{r_2} \ \dots \ \tilde{\mathbf{c}}_1^{r_k} \ \dots]$. Sequence $\tilde{\mathbf{c}}_1$ is mapped onto the PSK 193 symbol sequence \mathbf{x}_r for transmission to the DN during the 194 second transmission phase T_2 .



Fig. 3. Schematic of the DIRCC decoder at the DN.

B. Decoder Structure

The equivalent DIRCC decoder at the DN is shown in Fig. 3, 196 where the upper IRCC_s-URC_s-PSK_s decoder corresponds to 197 the upper encoder in Fig. 2, whereas the lower IRCC_r-PSK_s 198 decoder corresponds to the lower encoder in Fig. 2. Iterative 199 decoding is used both within the IRCC_s-URC_s-PSK_s decoder 200 as well as between the upper and lower decoders, as shown 201 in Fig. 3. 202

The maximum a posteriori probability (MAP) algorithm 203 [25] is invoked by each decoder. Note that the extrinsic log- 204 likelihood ratio (LLR) of a bit c is given by the subtraction of 205 the *a priori* LLR from the *a posteriori* LLR [25] as $L_{i,e}(c) = 206$ $L_{i,p}(c) - L_{i,a}(c)$, where subscript i is used for identifying the 207 specific detection block, which is labeled with (i) on the top- 208 left corner of its block diagram, as shown in Fig. 3. More 209 specifically, each of the *a priori* LLR $L_{2,a}(c_2)$ corresponding to 210 the URC_s-encoded bit c_2 is produced by the PSK demapper, as 211 shown in Fig. 3. The inner decoding iteration is performed be- 212 tween the URCs decoder and the IRCCs decoder, based on the 213 a priori or extrinsic LLRs of the IRCC_s-encoded bits $\{c_1\}$ or 214 its π_s -interleaved version, namely, the input bits of URC_s { u_2 }. 215 By contrast, the outer iteration between the upper and lower 216 decoders is based on the LLRs of the source bits $\{u_1\}$ and on its 217 π_r -interleaved version $\{u'_1\}$. Note that only one IRCC_r decoder 218 is needed for decoding all transmitted symbols from the K-RN- 219 assisted relay network. Iterative detection between the upper 220 and lower decoder blocks makes information exchange possible 221 between the two detection phases, namely, T_1 and T_2 , for the 222 sake of approaching the overall relay channel capacity. 223

III. NEAR-CAPACITY SYSTEM DESIGN 224

Let us now consider the relay channel capacity and the design 225 of our near-capacity DIRCC. 226

A. Relay Channel Capacity 227

The two-hop half-duplex relay channel capacity can be cal- 228 culated by modifying the full-duplex relay channel capacity 229 computation derived in [35]. More specifically, the upper bound 230 $C^{\rm U}$ and lower bound $C^{\rm L}$ of our half-duplex relay channel 231 capacity can be computed by considering the capacity of the 232 channel between the SN, RNs, and DN as follows: 233

$$C^{\cup} = \min\left\{\lambda C_{(s \to r,d)}, \ \lambda C_{(s \to d)} + (1 - \lambda)C_{(r \to d)}\right\}$$
(10)

$$C^{\mathsf{L}} = \min\left\{\lambda C_{(s \to r)}, \ \lambda C_{(s \to d)} + (1 - \lambda)C_{(r \to d)}\right\}$$
(11)

195

1.0 bps 1.0 0000000000000 C (bit/symbol) 0.5 bp $+ C_0$ 0.5 0.0' ○ C^U CL 4PSK .84 dE 4.68 dE G_{sr}=4.50 G_{rd}=3.57 0.0 6 -4 8 -2 SNR_a [dB]

Fig. 4. 4PSK-based DCMC capacity curves of the relay channel.

234 where $C_{(a \rightarrow b,c)}$ is the capacity of the channel between the 235 transmitter at node a and the receivers at both node b and 236 node c. Similarly, $C_{(a \rightarrow b)}$ is the capacity of the channel be-237 tween the transmitter at node a and the receiver at node b. 238 Note that the capacity term $C_{(a \to b,c)}$ or $C_{(a \to b)}$ can be ei-239 ther continuous-input-continuous-output memoryless channel 240 capacity or modulation-dependent discrete-input-continuous-241 output memoryless channel (DCMC) capacity [2], [36]. The 242 DCMC capacity is also referred to as the constrained infor-243 mation rate. The ratio of the first transmission period to the 244 total transmission period is given by $\lambda = N_s/(N_s + N_r)$. In 245 this contribution, we consider $N_s = N_r$, where N_r is given by 246 (6). This gives $\lambda = 1/2$. Note furthermore that the term $C_{(s \to r,d)}$ 247 considered in the upper bound of (10) assumes that the RN and 248 the DN are capable of perfectly sharing their received signals 249 for joint detection, which is not possible when the RN and the 250 DN are not colocated or linked. By contrast, the lower bound is 251 a more practical measure, since it treats the signals received at 252 the RN and the DN independently.

253 The upper and lower bounds of the relay channel capacity 254 curves, which are based on 4PSK DCMC, are shown in Fig. 4 255 for $\lambda = 0.5$, $G_{sr_k} = 4.50$, and $G_{r_k d} = 3.57$, where SNR_a is 256 the average transmit SNR defined in (8). The geometrical gains 257 G_{sr_k} and G_{r_kd} are chosen based on the relay selection mech-258 anism explained in Section III-C. The 4PSK-based DCMC 259 capacity C^0 of the direct link is also shown in Fig. 4 for 260 comparison. As seen in Fig. 4, a half-rate 4PSK-based scheme 261 has an SNR limit of 1.84 dB, where an error-free throughput 262 of 1 bit per symbol (BPS) is achieved. By contrast, the relay 263 channel capacity of the half-duplex 4PSK-based scheme has 264 SNR limits of -4.68 and -6.15 dB for its lower and upper 265 bounds, respectively, when aiming for a throughput of 0.5 BPS. 266 Note that the capacity of the relay channel (both C^{U} and C^{L}) is 267 higher than that of the direct link (C^0), when SNR_a ≤ -1 dB 268 due to the reduced path loss introduced by the RNs. However, 269 the asymptotic capacity of the relay channel is lower than that 270 of the direct link due to the half-duplex constraint.

271 B. Irregular Code Design

According to the so-called area property of the EXIT chart 273 [23], [24], it can be shown that the area under the normal-



Fig. 5. EXIT chart of the IRCCs-URCs-4PSK decoder at each RN.

ized EXIT curve of an inner decoder/demapper is related to 274 the achievable DCMC capacity. On the other hand, the area 275 under the inverted EXIT curve of an outer decoder is equal 276 to its coding rate R. Based on these EXIT chart properties, 277 a near-capacity concatenated coding scheme can be designed 278 by matching the corresponding inner and outer decoder EXIT 279 curves, so that a narrow but marginally open EXIT chart tunnel 280 exists between them all the way to the (x, y) = (1, y) point, 281 where $x = I_{E(u_2)} = I_{A(c_1)}$, and $y = I_{A(u_2)} = I_{E(c_1)} \in \{0, 1\}$ 282 for the EXIT chart in Fig. 5. Note that $I_{A(b)}$ and $I_{E(b)}$ denote the 283 a priori and extrinsic information, respectively, of $b \in \{c_1, u_2\}$, 284 which is either the outer encoder's output bit c_1 or the inner 285 encoder's input bit u_2 . The design of the IRCC is normally 286 carried out offline, particularly when communicating over fast 287 Rayleigh fading channels. However, when transmitting over 288 slow-fading channels, it may be more beneficial to design 289 the IRCC in real time, by adapting the IRCC coefficients 290 to the prevalent channel conditions. For simplicity, we only 291 consider transmissions over fast Rayleigh fading channels in 292 this paper. 293

1) Code Design for SN: For the IRCC_s design at the SN, 294 we consider an IRCC that consists of P = 17 memory-4 295 convolutional codes (CCs) given in [23] and [24]. A total 296 encoded sequence length of $N_c = 120\,000$ bits and an effective 297 coding rate of R = 0.5 are considered. The *p*th subcode has 298 a coding rate of R_p , and it encodes a fraction of $\alpha_p R_p N_c$ 299 information bits to $\alpha_p N_c$ encoded bits. More specifically, α_p 300 is the *p*th IRCC weighting coefficient satisfying the following 301 constraints [23], [24]: 302

$$\sum_{p=1}^{P} \alpha_p = 1, \quad R = \sum_{p=1}^{P} \alpha_p R_p, \quad \alpha_p \in [0, 1] \qquad \forall p \quad (12)$$

1.5

303 which can be conveniently represented in the following matrix 304 form:

$$\begin{bmatrix} 1 & 1 & \dots & 1 \\ R_1 & R_2 & \dots & R_P \end{bmatrix} \begin{bmatrix} \alpha_1 & \alpha_2 & \dots & \alpha_P \end{bmatrix}^T = \begin{bmatrix} 1 \\ R \end{bmatrix}$$
$$\mathbf{C} \ \alpha = \mathbf{d} . \tag{13}$$

305 The EXIT function of the IRCC is given by

$$I_{E(c_1)} = T_{c_1} \left[I_{A(c_1)} \right] = \sum_{p=1}^{P} \alpha_p T_{c_1,p} \left[I_{A(c_1)} \right]$$
(14)

306 where $T_{c_1,p} \left[I_{A(c_1)} \right] = I_{E(c_1),p}$ is the EXIT function of the *p*th 307 subcode. More explicitly, the inverted EXIT curves of the P = 308 17 subcodes having different coding rates ranging from 0.1 to 309 0.9 are shown in Fig. 5. The vertical difference between the 310 inner and outer code's EXIT curves at a given $I_{A(u_2)}$ value is 311 given by

$$e(I_{A(u_2)}) = I_{E(u_2)} - I_{A(c_1)}$$
(15)

$$= T_{u_2} \left[I_{A(u_2)}, C_* \right] - \sum_{p=1}^{P} \alpha_p T_{c_1, p}^{-1} \left(I_{E(c_1)} \right) \quad (16)$$

312 where the EXIT function of the inner decoder depends on both 313 $I_{A(u_2)}$ and on the DCMC capacity C_* . Fig. 5 shows that it is 314 possible to design an IRCC_s for the SN to have an EXIT curve 315 that matches the EXIT curve of the URC_s-4PSK inner encoder 316 at a receive SNR of 2 dB. Here, c_1 is the coded bit of the IRCC_s 317 outer encoder, and u_2 denotes the interleaved version of c_1 , 318 which is fed to the URC_s-4PSK inner encoder. We found that 319 IRCC_s only requires seven out of the 17 available component 320 codes, i.e., there are only seven nonzero IRCC weights. The 321 corresponding IRCC weight vector is given by

$$\widetilde{\alpha}_{s} = \begin{bmatrix} 0.2356z_{0.30}^{5} & 0.2052z_{0.35}^{6} & 0.0859z_{0.40}^{7} & 0.2114z_{0.55}^{10} \\ 0.1284z_{0.70}^{13} & 0.0630z_{0.85}^{16} & 0.0705z_{0.90}^{17} \end{bmatrix}$$
(17)

322 where the exponent and the subscript of the dummy variable 323 z denote the component code index p and its coding rate R_p , 324 respectively, whereas the pth IRCC weight α_p is the value in 325 front of $z_{R_p}^p$.

According to the capacity curve C^0 in Fig. 4, the corre-326 327 sponding transmit SNR at a capacity of 1 BPS is 1.84 dB. 328 Hence, the IRCC_s-URC_s-4PSK scheme is capable of operating 329 within (2 - 1.84) = 0.16 dB from the SNR limit of the source-330 to-relay channel. However, the narrow gap between the two 331 EXIT curves shown in Fig. 5 would require an impractically 332 high number of decoding iterations at the RN. Hence, we 333 aim for attaining a receive SNR of $\gamma_r^{sr} = 2.5$ dB instead of 334 2 dB at the RN to achieve a wider gap between these EXIT 335 curves for attaining lower decoding complexity. Note that these 336 two EXIT curves are generated semianalytically to predict 337 the actual performance of the IRCC_s-URC_s-4PSK scheme. A 338 Monte-Carlo-simulation-based staircase-shaped decoding tra-339 jectory of the IRCC_s-URC_s-4PSK scheme at $\gamma_r^{sr} = 2.5$ dB is 340 shown in Fig. 5 to satisfy the EXIT chart prediction, where it



Fig. 6. EXIT chart of the DIRCC-4PSK decoder at the DN.

traverses within the gap between the two EXIT curves up to the 341 top-right corner. 342

2) Code Design for RNs: The design of DIRCC involves 343 the IRCC_s-URC_s-4PSK scheme as the upper decoder and the 344 IRCC_r-4PSK scheme as the lower decoder in Fig. 3. Once 345 the IRCC_s has been designed for the source-to-relay channel, 346 the next task is to design the IRCC_r. However, the design of 347 IRCC_r for the relay network is more challenging, because the 348 EXIT curves of both the upper and lower decoders are SNR 349 dependent. The EXIT curve of the IRCC_s-URC_s-4PSK upper 350 decoder at the DN is shown in Fig. 6 when the receive SNR 351 is $\gamma_x^{sd} = -3.5$ dB,³ where eight inner decoding iterations⁴ are 352 considered. An IRCC_r is designed to have an EXIT curve that 353 can closely match the EXIT curve of the IRCC_s-URC_s-4PSK 354 decoder. 355

We found that the memory-4 17-component IRCC in [23] 356 fails to ensure a good match to the steep $IRCC_s$ - URC_s -4PSK 357 EXIT curve shown in Fig. 6. On the other hand, a simple 358 repetition code (RC) would give a vertical EXIT curve that can 359 match the vertical part of the $IRCC_s$ - URC_s -4PSK EXIT curve. 360 Hence, we have created nine RCs having coding rates ranging 361 from 0.1 to 0.5 with a step size of 0.05. Their EXIT curves 362 are shown by the nine vertical dashed lines in Fig. 6, where 363 the rightmost vertical curve has the lowest coding rate of 0.1 364 and the leftmost vertical curve has the highest coding rate of 365 0.5. To match the gradually sloping part of the $IRCC_s$ - URC_s - 366 4PSK EXIT curve, we have created nine further component 367 CCs, having coding rates ranging from 0.5 to 0.9 with a step 368 size of 0.05. The mother code of these CCs is a half-rate 369 unit-memory CC having a generator polynomial of [2 1] in octal 370

³The rationale of considering $\gamma_r^{sd} = -3.5$ dB is explained in Section III-C. ⁴It was found that having more than eight inner iterations will only marginally increase the area under the EXIT curve of the IRCC_s-URC_s-4PSK decoder.

371 format. The same puncturing patterns of the 17-component 372 IRCC in [23] are used for creating CCs having coding rates 373 higher than 0.5. The corresponding nine EXIT curves are shown 374 by the gradually sloping EXIT curves in Fig. 6, where the 375 rightmost curve has the lowest coding rate of 0.5, and the 376 leftmost curve has the highest coding rate of 0.9. Based on these 377 18 newly created component codes, an IRCC_r-4PSK lower 378 encoder was designed. Its EXIT curve is also shown in Fig. 6. 379 The corresponding IRCC weight vector is given by

$$\widetilde{\alpha}_r = [0.60z_{0.60}^8 \ 0.30z_{0.50}^9 \ 0.10z_{0.85}^{17}] \tag{18}$$

380 where the eighth and ninth subcodes are from the RC family, 381 while the 17th subcode is from the unit-memory CC family. 382 Hence, we only need three RNs for our system with only a low-383 complexity RC or a unit-memory CC needed as the RN encoder. 384 The proposed design was based on a conventional EXIT 385 chart, where a sufficiently long interleaver is required for the 386 Monte Carlo simulation to warrant a good match between the 387 EXIT chart prediction and the actual simulation. We found that 388 an interleaver length of 120 000 bits is sufficient for the inter-389 leaver between the IRCC $_s$ and URC $_s$ encoders. The encoded bit 390 sequence can be stored in a buffer for transmission over several 391 frame periods, if the transmission frame duration is shorter than 392 the encoded sequence length. However, if the system requires 393 a short interleaver, we should redesign the proposed scheme 394 based on EXIT band charts [37], while using the same design 395 principle.

396 C. Power Allocation and Relay Selection

397 The receive SNR required at the RN during T_1 is given by 398 $\gamma_r^{sr} = 2.5$ dB, as shown in Fig. 5, whereas the receive SNR 399 needed at the DN during T_2 is given by $\gamma_r^{rd} = 1.5$ dB, as shown 400 in Fig. 6. The idea of the design is to simultaneously achieve 401 these two receive SNRs at the RN and the DN, respectively, 402 to achieve a bit error rate (BER) lower than 10^{-6} at all RNs 403 and DN at the same time. When this is achieved, there will be 404 minimal error propagation from the DAF-based RNs. Since the 405 receive SNR depends on the geometrical gain as shown in (9), 406 we may achieve the required receive SNR with the aid of relay 407 selection, which determines the geometrical gains based on the 408 location of the RN according to (2) and (5). When communi-409 cating over fast Rayleigh fading channels, RN selection can be 410 predetermined based on the RN locations, without the need for 411 CSI knowledge at each transmission symbol period, because the 412 average power of the fast Rayleigh channel coefficients is unity. 413 By contrast, RN selection is a dynamic process, depending on 414 the instantaneous channel variations when transmitting over 415 slow-fading channels. We consider fast Rayleigh fading chan-416 nels in this contribution. Since the receive SNR also depends on 417 the transmit SNR according to (9), we may calculate the mini-418 mum required transmission power and then appropriately share 419 it between the SN and RNs. CSI knowledge is not required⁵ 420 for the power allocation mechanism either when transmitting over fast Rayleigh fading channels. We assumed that a base 421 station or a central node carries out the RN selection and/or 422 power allocation, followed by broadcasting this information to 423 the participating nodes. 424

1) Power Allocation: When the number of available RNs is 425 limited and their locations are fixed, power allocation/control 426 can be used for improving power efficiency. Assuming for 427 simplicity that all RNs are located midway between the SN 428 and the DN, we have geometrical gains of $G_{sr_k} = G_{r_kd} = 4.429$ To achieve $\gamma_r^{sr} = 2.5$ dB at the RN, the corresponding trans- 430 mit SNR at the SN is given by $\gamma^s_t = 2.5 - 10 \log_{10}(G_{sr_k}) = 431$ -3.5 dB according to (9). Since we have $G_{sd} = 1$, the cor- 432 responding receive SNR at the DN during T_1 is given by 433 $\gamma_{r}^{sd} = \gamma_{t}^{s} = -3.5$ dB. The EXIT curve of the IRCC_s-URC_s-434 4PSK scheme at $\gamma_r^{sd} = \gamma_t^s = -3.5$ dB is shown in Fig. 6.435 Furthermore, the required receive SNR at the DN during T_2 436 is given by $\gamma_r^{rd} = 1.5$ dB, and the corresponding transmit SNR 437 at the RN is given by $\gamma^r_{\rm t} = 1.5 - 10 \log_{10}(G_{r_k d}) = -4.5$ dB 438 when $G_{r_k d} = 4$. Hence, the transmit power at the SN has to be 439 $\gamma_t^s - \gamma_t^r = 1$ dB higher than that of the RN, to simultaneously 440 achieve an infinitesimally low BER at all RNs and the DN. The 441 average transmit SNR of the power-allocation-based DIRCC 442 scheme is given by 443

$$\widetilde{\gamma}_{t} = 10 \log_{10} \left(\lambda 10^{\gamma_{t}^{s}/10} + (1-\lambda) 10^{\gamma_{t}^{r}/10} \right)$$
(19)

which is equal to $\tilde{\gamma}_t = -4 \text{ dB}$ for $\gamma_t^s = -3.5 \text{ dB}$ and $\gamma_t^r = 444 -4.5 \text{ dB}$, where $\lambda = 0.5$, as discussed in Section III-A. The 445 simulation-based decoding trajectory of the DIRCC-4PSK 446 scheme is shown to verify the EXIT chart predictions in Fig. 6, 447 when $\tilde{\gamma}_t = -4 \text{ dB}$.

2) Relay Selection: Alternatively, if the transmit power of 449 the SN and of all the RNs is fixed to a constant value of $\gamma_t^r = 450 \gamma_t^s$, we may select RNs at appropriate geographical locations for 451 achieving different G_{sr_k} and G_{r_kd} values, to simultaneously 452 maintain $\gamma_x^{sr} = 2.5$ dB and $\gamma_x^{rd} = 1.5$ dB. Assuming that all 453 RNs are relatively close to each other and are located in the 454 direct SN-to-DN path, where we have $d_{sd} = d_{sr_k} + d_{r_kd}$, it can 455 be shown that the geometrical gains are related to each other as 456 follows:

$$G_{r_k d} = \left(\frac{1}{1 - 1/\sqrt{G_{sr_k}}}\right)^2.$$
 (20)

Furthermore, since we have $\gamma_t^s = \gamma_t^r$, it can be shown based on 458 (9) that 459

$$\frac{G_{r_k d}}{G_{sr_k}} = 10^{(\gamma_r^{rd} - \gamma_r^{sr})/10}$$
(21)

where we have $\gamma_{r}^{rd} - \gamma_{r}^{sr} = 1.5 - 2.5 = -1$ dB in our example. 460 Based on (20) and (21), we have the following relationship: 461

$$G_{sr_k} = \left(1 + 10^{-(\gamma_r^{rd} - \gamma_r^{sr})/20}\right)^2$$
(22)

which gives $G_{sr_k} = 4.50$ for our case, and from (20), we have 462 $G_{r_kd} = 3.58$. Once G_{sr_k} and G_{r_kd} are identified, we may 463 find the corresponding relay distances from (2) and (5), which 464 are given by $d_{sr_k} = 0.47d_{sd}$ and $d_{sr_k} = 0.53d_{sd}$, respectively. 465

⁵CSI knowledge is only needed at the receiver for decoding purposes, where each RN only has to know the CSI between the SN and itself, whereas the DN only has to know the CSI between the corresponding RNs/SN and itself.



Fig. 7. Relay selection schematic for the DIRCC scheme.

466 The average transmit SNR of the relay-selection-based DIRCC 467 scheme is given by

$$\widetilde{\gamma}_{t} = \gamma_{t}^{r} = \gamma_{t}^{s} = \gamma_{r}^{sr} - 10\log_{10}(G_{sr_{k}})$$
(23)

468 where we have $\tilde{\gamma}_t = -4 \text{ dB}$ for our example, which is the same 469 value as that of the power-allocation-based scenario.

3) Joint Power Allocation and Relay Selection: In the nontideal case, when the RNs are not located in the direct SN-to-DN transformation invoke the following approach, which employs transformation and power allocation for minimizing the transmission power.

- 475
- 1) Calculate the minimum required receive SNR at the RN during T_1 , $\gamma_{r,\min}^{sr}$, and at the DN during T_2 , $\gamma_{r,\min}^{rd}$, based on the EXIT chart analysis described in Section III-B.
- 479 2) For a given SN transmit SNR γ_{t}^{s} , select those specific 480 RNs that can satisfy the SNR requirement of $\gamma_{r}^{sr} \geq \gamma_{r,\min}^{sr}$ for ensuring a low BER at each RN. Normally, 481 the geographical range is within a circle having the SN 483 at its center, as shown in Fig. 7. More explicitly, we have 484 $d_{sr_{k}} \leq \sqrt{G_{sr_{k}}} d_{sd}$, where $G_{sr_{k}}$ is given by (22).
- 3) From the appropriately chosen set of RNs, select K RNs
 that have high-SNR RN-to-DN links to form a virtual
 IRCC that consists of K component codes. Normally,
 the geographical range is within the quarter of the circle
 facing the DN, as shown in Fig. 7.
- 490 4) If the number of available RNs $(K_r \ge 1)$ is less than 491 the number of IRCC_r component codes, i.e., $K_r < K$, 492 some of the RNs will have to perform several IRCC 493 component encoding operations. Again, the number of 494 symbols transmitted by each RN is different.
- Each RN takes turns in transmitting, while using the 495 5) minimum power that can satisfy the following RN trans-496 mit SNR: $\gamma_{t,\min}^r = \gamma_{r,\min}^{rd} - g_{r_kd}$ according to (9). When communicating over slow- or shadow-fading channels, 497 498 499 (9) would have to take into consideration the instantaneous channel gain h_{r_kd} . Hence, the RN transmission 500 power may change with its location or with time, where 501 the average transmit SNR of the DIRCC scheme is given 502 503 by (19).



Fig. 8. BER-versus-SNR_a performance of the proposed DIRCC-4PSK scheme in comparison with perfect DIRCC-4PSK, IRCC-URC-4PSK, DSECCC-ID, and DTTCM schemes, when communicating over fast Rayleigh fading channels using a frame length of $60\,000$ 4PSK symbols.

Furthermore, relay selection should also take into account 504 the battery life of each RN, if this information is available. 505 More specifically, an RN with insufficient battery life should 506 not be chosen as part of the virtual IRCC. Since each IRCC 507 component encoder produces a different number of modulated 508 symbols, RNs having a longer battery life should be assigned 509 to the specific component code that produces the longest 510 coded/modulated sequence, i.e., the highest L_k value given in 511 (6), which is normally related to a higher IRCC weight or a 512 lower coding rate. In the following simulation study, we only 513 consider the ideal case where all RNs have sufficient battery 514 life for the whole transmission process.

IV. RESULTS AND DISCUSSIONS 516

Let us first investigate the performance of the proposed 517 scheme, when perfect CSI is available at each receiver. The 518 BER-versus-average-transmit-SNR performance of the pro-519 posed DIRCC-4PSK scheme is compared with both that of 520 perfect⁶ DIRCC-4PSK and that of the noncooperative IRCC- 521 URC-4PSK schemes in Fig. 8, based on the simulation param- 522 eters of Table I. The noncooperative IRCC-URC-4PSK scheme 523 has 30 decoding iterations at the DN. It operates approximately 524 0.65 dB away from its channel capacity at BER = 10^{-6} . Both 525 DIRCC-4PSK schemes have eight inner iterations and four 526 outer iterations at the DN. Relay selection was considered in 527 the simulations, and all three RNs considered are assumed 528 to be located in the direct SN-to-DN path. Hence, we have 529 $G_{sr_k} = 4.50$ and $G_{r_kd} = 3.57$ for all three RNs according to 530 (22) and (20), respectively, with the aid of the relay selection 531 mechanism detailed in Section III-C2. As seen in Fig. 8, the 532 proposed DIRCC-4PSK scheme has negligible performance 533 difference to that of the perfect DIRCC-4PSK scheme for 534

⁶The perfect DIRCC-4PSK scheme assumes that there are no decoding errors at each RN, whereas the actual DIRCC-4PSK scheme considers a realistic SN-to-RN transmission and actual decoding with potential decoding errors at each RN.

SN-to-RN geometrical gain, G_{sr_k}

RN-to-DN geometrical gain, $G_{r_k d}$

Modulation	4PSK
Number of modulated symbols/frame	60,000
Interleaver	Random and bit-based
IRCC weights, $\tilde{\alpha}_s$	See (17)
DIRCC weights, $\tilde{\alpha}_r$	See (18)
Coding rate of IRCC	0.5
Coding rate of DIRCC	0.5
Number of IRCC-URC-4PSK iterations	30
Number of DIRCC inner iterations	8
Number of DIRCC outer iterations	4
Decoding algorithm	Approximated Log-MAP [25]
Channel type	Fast Rayleigh fading

4.50 (6.53 dB)

3.57 (5.53 dB)

TABLE I SIMULATION PARAMETERS

535 BER $< 10^{-2}$. This is due to the efficient relay selection mecha-536 nism. The proposed scheme is also capable of operating within 537 0.68 dB from the lower bound of the channel capacity. This 538 near-capacity performance is achieved with the advent of an 539 effective system design, as detailed in Section III, with the aid 540 of powerful iterative decoding at all of the RNs and at the DN. Let us now investigate the performance of the proposed 541 542 DIRCC scheme in comparison to both the distributed TTCM 543 (DTTCM) [13] and the distributed self-concatenated convolu-544 tional coding relying on iterative detection (SECCC-ID) [18] 545 schemes, when perfect CSI is assumed. All schemes employ a 546 frame length of 60 000 4PSK symbols for transmission over fast 547 Rayleigh fading channels. The throughput of the 4PSK-based 548 SECCC-ID scheme is 0.5 BPS, which is exactly identical to 549 that of the proposed 4PSK-based DIRCC scheme. However, the 550 throughput of the 4PSK-based DTTCM⁷ scheme is 0.667 BPS, 551 because it only transmits parity bits from the RN to the DN. As 552 seen in Fig. 8, the DIRCC scheme outperforms the DSECCC-553 ID and DTTCM schemes by approximately 0.5 and 2.0 dB,⁸ 554 respectively, at a BER of 10^{-6} . We found that the proposed 555 DIRCC scheme performs the closest to the relay channel's 556 capacity, when aiming for a throughput of 0.5 BPS, compared 557 with existing DAF-based distributed coding schemes found in

559 channels using a single antenna at each node. When the CSI is not perfectly known at the receiver, our co-560 561 herently detected scheme would suffer from some performance 562 erosion. To investigate the robustness of our DIRCC scheme 563 to imperfect CSI, we model the channel estimation errors by 564 a Gaussian process superimposed on each channel coefficient 565 at the receiver, where the noise variances of 0.01 and 0.1 566 are used. The corresponding performance curves of DIRCC-567 4PSK and IRCC-URC-4PSK are shown in Fig. 8, where a CSI 568 estimation error with a variance of 0.01 would only cause a 569 marginal loss of approximately 0.2 dB at a BER of 10^{-6} . By 570 contrast, an error with a variance of 0.1 would impose a more

558 the literature, when communicating over fast Rayleigh fading



Fig. 9. EXIT chart of the low-complexity DIRCC-4PSK decoder at the DN.

substantial but still moderate SNR loss of approximately 1.3 dB 571 on the DIRCC scheme. This loss is lower than the 3-dB loss 572 incurred by conventional noncoherent schemes [38]. Hence, 573 our DIRCC scheme may be deemed robust to CSI estimation 574 errors. In both imperfect-CSI cases, we ensured that appropriate 575 RN selection (or power allocation) was invoked for the DIRCC 576 scheme for ensuring that the decoders at both the RNs and DN 577 are capable of simultaneously achieving a low BER, according 578 to the mechanism described in Section III-C.

However, the decoding complexity at the DN is rather high 580 due to the high number of inner iterations between the memory- 581 4-based IRCC_s decoder and the unit-memory URC_s decoder. 582 Let us denote the number of decoding trellis states per iteration 583 of the upper IRCC_s-URC_s-4PSK decoder as $I_U = 2^4 + 2^1 = 584$ 18 states and that of the unit-memory CC (or RC)-based lower 585 IRCC_r-4PSK decoder as $I_L = 2^1 = 2$ states. The total number 586 of trellis states invoked for the DIRCC-4PSK scheme would be 587 $I = 4 \times (8I_U + I_L) = 584$ states. We found that the decoding 588 complexity at the DN can be significantly reduced if a slightly 589 higher value than the minimum transmit power is used. More 590 explicitly, let us consider the scheme shown in Fig. 9, where 591 $G_{r_kd} = G_{sr_k} = 4$. The transmit SNR at the SN and the RN 592 is $3 - 10 \log_{10}(4) = -3 \text{ dB}$ and $2.5 - 10 \log_{10}(4) = -3.5 \text{ dB}$, 593 respectively. Hence, the corresponding average transmit SNR 594 is given by -3.24 dB according to (19). As seen in Fig. 9, 595 two inner iterations and three outer iterations are sufficient for 596 achieving an infinitesimally low BER at this setting. In other 597 words, when operating at -3.24 - (-4) = 0.76 dB higher 598 average transmit SNR, the DIRCC-4PSK decoder would only 599 incur $I = 3 \times (2I_U + I_L) = 114$ trellis states, which is only 600 19.5% of the original decoding complexity. A higher reduction 601 of the decoding complexity can be achieved, when operating 602 further away from the SNR limit of the channel capacity. 603 Furthermore, based on the EXIT chart in Fig. 5, we found that 604

⁷The original DTTCM scheme in [13] employed 2/3-rate TTCM-8PSK at the SN and uncoded-4PSK at the RN. The DTTCM scheme considered here uses 1/2-rate TTCM-4PSK at the SN and uncoded-4PSK at the RN to make its throughput as close as possible to the proposed DIRCC scheme for a fair comparison.

⁸In terms of SNR per information bit, the gain of DIRCC over DTTCM is given by 2.0 dB +10 $\log_{10}(0.667) - 10 \log_{10}(0.50) = 0.76$ dB.

605 the average number of decoding iterations at each RN is given 606 by 97, 25, or 17 when the receive SNRs are given by 2, 2.5, 607 or 3 dB, respectively. The receive SNR at each RN is given by 608 2.5 or 3 dB, when the average transmit SNR is given by -4 or 609 -3.24 dB, respectively. Hence, the total number of decoding 610 states at each RN is also reduced by 32%, i.e., from $25I_U =$ 611 450 to $17I_U = 306$ states, when a 0.76-dB higher average 612 transmit SNR is employed. In summary, the proposed DIRCC 613 scheme can be designed according to the target transmit power, 614 where a high-complexity scheme is invoked when aiming for 615 approaching the channel capacity, whereas a lower complexity 616 scheme can be designed when operating slightly further away 617 from the SNR limit of the channel capacity.

V. CONCLUSION

A near-capacity DIRCC scheme has been proposed for as-619 620 sisting DAF-based cooperative communications. The potential 621 decoding errors at each RN may be avoided by the proposed 622 relay selection mechanism, whereas the transmission power 623 of the DIRCC scheme can be reduced by invoking the pro-624 posed power allocation method. Furthermore, a low-complexity 625 encoder was used by each RN for yielding a variable-length 626 coded/modulated symbol sequence. The semianalytical EXIT-627 chart-based performance predictions were verified by simula-628 tion results. It was shown that the proposed DIRCC scheme is 629 capable of operating close to the relay channel's capacity, and it 630 outperforms the existing distributed coding schemes operating 631 in a similar simulation environment at a similar throughput. It 632 was also shown that the DIRCC scheme is robust to channel 633 estimation errors at the receiver. The proposed DIRCC scheme 634 can be further developed for supporting communications over 635 shadow-fading channels. It can also be adapted according to the 636 battery life of the RNs. More advanced modulation schemes, in-637 cluding hierarchical modulation and superposition modulation, 638 may also be utilized in the proposed DIRCC scheme.

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